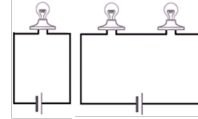


## Combining Light Bulbs in Series

1. Build a circuit with one light bulb and observe its brightness. The brightness of a bulb is a measure of...



2. Then add a second bulb in series. Observe or infer what happens to the: *Increase, Decrease, or Remain the same*

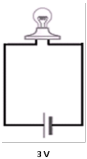
Power of an individual bulb (= brightness)		↓ x4
Total power of the circuit		↓
Resistance of an individual bulb		same
Total resistance of the circuit		↑
Total potential difference across the circuit		Same
Potential difference across an individual bulb		↓ x2
Total current in the circuit		↓
Current through an individual bulb		↓ x2

3. Unscrew one light bulb from its base (but leave the base in the circuit). What happens to the other light bulb? Why?

goes out - incomplete circuit

## Combining Light Bulbs in Series

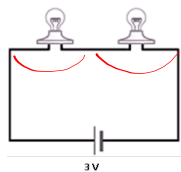
4. Assume each light bulb has a resistance of  $10\Omega$ . Analyze each circuit.



R	$10\Omega$
V	3v
I	.3A
P	.9W

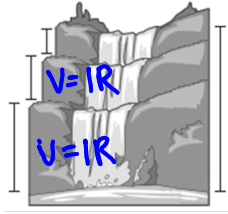
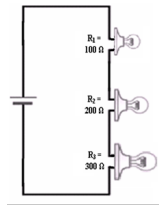
$$I = \frac{V}{R}$$

$$P = IV$$



	Bulb #1	Bulb #2	Circuit Total
R	$10\Omega$	$10\Omega$	$20\Omega$
V	1.5v	1.5v	3v
I	.15A	.15A	.15A
P	.225w	.225w	.45w

## Analyzing Series Circuits



1. **Current:** Current is the same at all points in a series circuit. Current is the same through each resistor.

$$I_T = I_1 = I_2 = I_3 = \dots$$

NOTE: this does NOT mean the current stays the same if you change the circuit

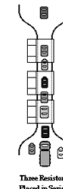
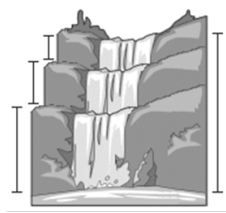
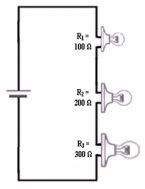
2. **Voltage:** The increase in potential provided by the battery is equal to the sum of the potential drops across each resistor.

$$V_T = V_1 + V_2 + V_3 + \dots$$

NOTE: conservation of energy

Kirchhoff's Second Law ( Voltage law, Loop Rule)- **Around any closed loop, the sum of the emf's (voltage rises) equals the sum of the potential differences (voltage drops).**

## Analyzing Series Circuits



3. **Resistance:** The total resistance of the circuit is the sum of the individual resistances.

$$R_T = R_1 + R_2 + R_3 + \dots$$

**Equivalent resistance** – the single resistance that could replace the several resistors in a circuit

NOTE: The total resistance is higher than any of the individual resistances.

4. **Power:** The total power used in the circuit is the sum of the power used by the individual resistors.

$$P_T = P_1 + P_2 + P_3 + \dots$$

NOTE: Conservation of energy principle

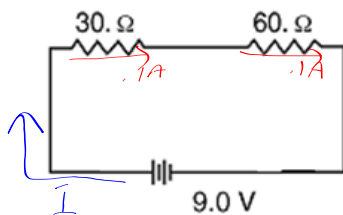
## Analyzing Series Circuits

- Series relationships**
5. In a series circuit, which resistor, if any, will . . .
- have the greatest potential difference across it?  
highest
  - have the most current running through it?  
all the same
  - dissipate the most power?  
highest
  - shine brightest (if it is a light bulb)?  
highest

$$\frac{V_1}{V_2} = \frac{R_1}{R_2} = \frac{P_1}{P_2}$$

$$P = IV$$

6. Determine the current through each resistor, the potential drop across each resistor, and the power dissipated by each resistor in the circuit below.



$$R_T = R_1 + R_2 = 90\Omega$$

$$I_T = V_T / R_T = 9V / 90\Omega = .1A$$

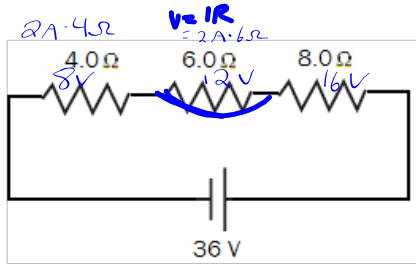
$$V_{30} = IR_{30} = .1A \cdot 30\Omega = 3V$$

$$V_{60} = IR_{60} = .1A \cdot 60\Omega = 6V$$

$$P_{30} = IV_{30} = .1A \cdot 3V = .3W$$

$$P_{60} = IV_{60} = .1A \cdot 6V = .6W$$

7. Find the potential difference across each resistor, the current through each resistor, and the power used by each resistor.



$R_T = 18 \text{ ohms}$

$2A$

$I_T = V_T / R_T = 36V / 18\Omega = 2A$

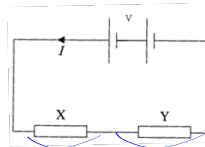
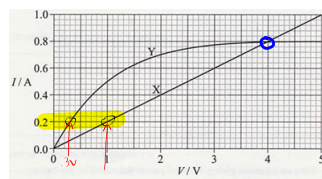
$V_4 = IR = 2A \cdot 4\Omega = 8V$

$V_6 = IR = 2A \cdot 6\Omega = 12V$

$V_8 = IR = 2A \cdot 8\Omega = 16V$

I-V Characteristics

1. The graph below shows the I-V characteristics of two conductors, conductors are connected in series to a battery whose voltage is such that the power dissipated in each of the two resistors is the same.



a) Determine the resistance of each resistor.

$R = V/I = 4V / 0.8A = 5\Omega$

b) Determine the total voltage of the battery.

$8V$

c) Determine the total power dissipated in the circuit.

$I_T V_T = (0.8A)(8V) = 6.4W$

d) The battery is replaced by another one such that the current through X is 0.2 amps. Determine the voltage of this battery.

$V_T = 1.3V$