

WARMUP

Calculate $f'(x)$ using $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$

for $f(x) = 3x^2 + 5x - 7$

$$f'(x) = \lim_{h \rightarrow 0} \frac{(3(x+h)^2 + 5(x+h) - 7) - (3x^2 + 5x - 7)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{3(x^2 + 2xh + h^2) + 5x + 5h - 7 - 3x^2 - 5x + 7}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\cancel{3x^2} + 6xh + 3h^2 + \cancel{5x} + 5h - \cancel{7} - \cancel{3x^2} - \cancel{5x} + \cancel{7}}{h}$$

$$= \lim_{h \rightarrow 0} \frac{\cancel{h}(6x + 3h + 5)}{\cancel{h}}$$

$$= 6x + 5$$

$$\lim_{h \rightarrow 0} \frac{(4\sqrt{x+h} - 4\sqrt{x})}{h} \cdot \frac{(4\sqrt{x+h} + 4\sqrt{x})}{(4\sqrt{x+h} + 4\sqrt{x})}$$

$$= \lim_{h \rightarrow 0} \frac{16(x+h) - 16x}{h(4\sqrt{x+h} + 4\sqrt{x})} = \lim_{h \rightarrow 0} \frac{\cancel{16x} + 16h - \cancel{16x}}{\cancel{h}(4\sqrt{x+h} + 4\sqrt{x})}$$

$$= \frac{16}{4\sqrt{x} + 4\sqrt{x}} = \frac{16}{8\sqrt{x}} = \frac{2}{\sqrt{x}}$$

Section 2.5 Interpretations of the Derivative

One notation for derivative of a function is $f'(x)$.

There are other notations:

$$\text{If } y = f(x), \text{ then } \frac{dy}{dx} = f'(x)$$

↑ derivative of y
with respect to x

If s is the position function of an object,

then $\frac{ds}{dt}$ is instantaneous, or velocity so $v = \frac{ds}{dt}$

$$h(t) = -16t^2 + v_0 t + h_0$$

$$v(t) = -32t + v_0 \Rightarrow v_f = at + v_i$$

$$\frac{d}{dx}(f(x)), \quad \frac{d}{dx}(y), \quad \frac{dy}{dx} \Big|_{x=2}$$

↑ derivative evaluated
at $x=2$, so it
means $f'(2)$

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$$T = f(t)$$

time in minutes
temperature in $^{\circ}\text{F}$

a) What is the sign of $f'(t)$?

$$\frac{dT}{dt} > 0$$

T is increasing so $T' > 0$

b) $f'(20) = \left. \frac{dT}{dt} \right|_{t=20}$ units are $\frac{^{\circ}\text{F}}{\text{min}}$

$f'(20) = 2$ At 20 mins yam's temp is increasing at $2^{\circ}\text{F}/\text{min}$

$$f(20) = 150$$

In 20 min, temp = 150°F

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price = $\$p$

quantity = q

$$q = f(p)$$

$$\frac{dq}{dp} = f'(p)$$

a) $f(150) = 2000$

At $\$150$, sell 2000 units

$$b) f'(150) = -25$$

$$\frac{dq}{dp} = \frac{\text{\# of items}}{\$}$$

At \$150, quantity
sold decreases by
 $25 \frac{\text{items}}{\$}$

p88-89 1, 3, 11, 14, 17