

Section 8.4 Day 2

$\|\mathbf{v}\|$ represents the magnitude of vector \mathbf{v} .

Properties: a) $\|\mathbf{v}\| \geq 0$

b) $\|\mathbf{v}\| = 0$ if and only if $\mathbf{v} = \mathbf{0}$

c) $\|-\mathbf{v}\| = \|\mathbf{v}\|$

d) $\|\alpha\mathbf{v}\| = |\alpha| \cdot \|\mathbf{v}\|$

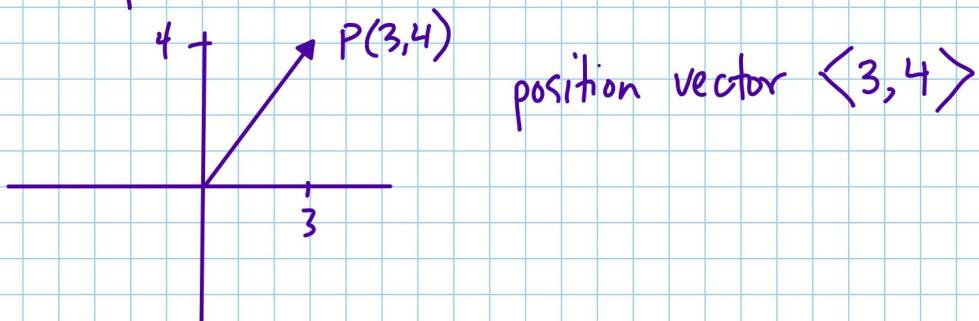
A vector \mathbf{u} for which $\|\mathbf{u}\| = 1$ is called a unit vector.

We can represent vectors algebraically by breaking them down into components.

$\mathbf{v} = \langle a, b \rangle$ a and b are real numbers and are called the components of \mathbf{v} .

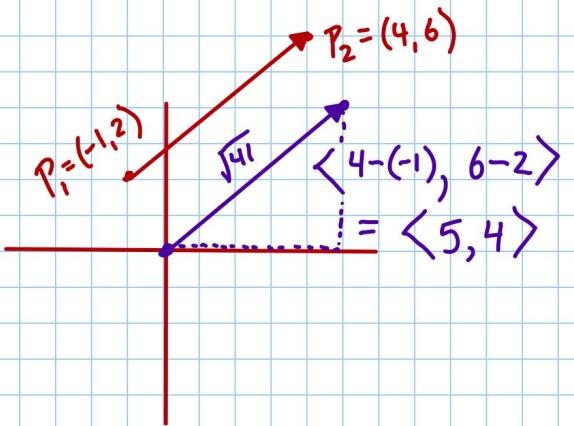
We use the coordinate plane to represent algebraic vectors.

If $\mathbf{v} = \langle a, b \rangle$ has its initial point at the origin, then \mathbf{v} is a position vector.



Any vector whose initial point is not at the origin is equal to a position vector.

Suppose \mathbf{v} is a vector with initial point $P_1(x_1, y_1)$ and terminal point $P_2(x_2, y_2)$



If $\mathbf{v} = \overrightarrow{P_1 P_2}$, then \mathbf{v} is equal to the position vector $\langle x_2 - x_1, y_2 - y_1 \rangle$

We can also ^{write} any algebraic vector as $a\mathbf{i} + b\mathbf{j}$ where $\mathbf{i} = \langle 1, 0 \rangle$ and $\mathbf{j} = \langle 0, 1 \rangle$ \mathbf{i} and \mathbf{j} are unit vectors

In other words $\mathbf{v} = \langle a, b \rangle = a\mathbf{i} + b\mathbf{j} = a\langle 1, 0 \rangle + b\langle 0, 1 \rangle$

Let $\mathbf{v} = a_1\mathbf{i} + b_1\mathbf{j} = \langle a_1, b_1 \rangle$ and $\mathbf{w} = a_2\mathbf{i} + b_2\mathbf{j} = \langle a_2, b_2 \rangle$

and α is a scalar.

$$\mathbf{v} + \mathbf{w} = (a_1 + a_2)\mathbf{i} + (b_1 + b_2)\mathbf{j} = \langle a_1 + a_2, b_1 + b_2 \rangle$$

$$\mathbf{v} - \mathbf{w} = (a_1 - a_2)\mathbf{i} + (b_1 - b_2)\mathbf{j} = \langle a_1 - a_2, b_1 - b_2 \rangle$$

$$\alpha\mathbf{v} = (\alpha a_1)\mathbf{i} + (\alpha b_1)\mathbf{j} = \langle \alpha a_1, \alpha b_1 \rangle$$

$$\|\mathbf{v}\| = \sqrt{a_1^2 + b_1^2}$$

ex 3 p 624 If $\mathbf{v} = 2\mathbf{i} + 3\mathbf{j} = \langle 2, 3 \rangle$

$$\mathbf{w} = 3\mathbf{i} - 4\mathbf{j} = \langle 3, -4 \rangle$$

$$a) \mathbf{v} + \mathbf{w} = \underbrace{\langle 2, 3 \rangle}_{+} \underbrace{\langle 3, -4 \rangle}_{=} = \langle 5, -1 \rangle = 5\mathbf{i} - \mathbf{j}$$

$$b) \mathbf{v} - \mathbf{w} = \langle 2, 3 \rangle - \langle 3, -4 \rangle = \langle -1, 7 \rangle = -\mathbf{i} + 7\mathbf{j}$$

$$c) 3\mathbf{v} = 3\langle 2, 3 \rangle = \langle 6, 9 \rangle = 6\mathbf{i} + 9\mathbf{j}$$

$$\begin{aligned} d) \quad 2\mathbf{v} - 3\mathbf{w} &= 2\langle 2, 3 \rangle - 3\langle 3, -4 \rangle \\ &= \langle 4, 6 \rangle - \langle 9, -12 \rangle \\ &= \langle -5, 18 \rangle = -5\mathbf{i} + 18\mathbf{j} \end{aligned}$$

$$e) \quad \|\mathbf{v}\| = \sqrt{2^2 + 3^2} = \sqrt{13}$$

$$\begin{array}{c} p628-629 \\ 19-37 \text{ odd} \end{array}$$

$$\begin{array}{ll} u) \quad P_2(3, 2) & \mathbf{v} = \langle 5-3, 6-2 \rangle \\ G = \langle 5, 6 \rangle & \mathbf{v} = \langle 2, 4 \rangle = 2\mathbf{i} + 4\mathbf{j} \end{array}$$