
(1)

$$
\begin{aligned}
& \text { Solve for } n \\
& 2 m-(3+n)=100 \mathrm{~m} \\
& -2 m \quad-2 m \\
& -(3+n)=98 m \\
& -3-n=98 m \\
& +3
\end{aligned}
$$

$$
-n=98 m+3
$$

$$
\text { So } n=-98 m-3
$$

(2) $\frac{1}{3}|10-x|=5+x$
multiply all three terms by 3

$$
|10-x|=15+3 x
$$

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multiply all three terms by 3

$$
|10-x|=15+3 x
$$

$$
\begin{aligned}
\text { onsite } & =r e g h t \text { ste } \\
10-x & =15+3 x \\
+x & +x
\end{aligned}
$$

$$
\left.\right|_{-15}=1_{-15} 5+4 x
$$

$$
\begin{aligned}
-5 & =4 x \\
x & =-\frac{5}{4}
\end{aligned}
$$

$$
\begin{array}{r}
\text { inside }=\text { opp of right side } \\
10-x=-(15+3 x) \\
10-x=-15-3 x \\
+3 x \\
10+3 x \\
10+2 x=-15 \\
2 x=-25 \\
2 x=-25
\end{array}
$$

(3) Solve the inequality direoly

$$
\begin{aligned}
& 2\left|\frac{x-5 \mid}{2}\right| \geq \frac{13}{2} \\
& |x-5| \geq 6.5
\end{aligned}
$$


inside $\geq$ los inside

$$
\begin{array}{ll}
x-5 \geq 6.5 & x-5 \leqslant-6.5 \\
+5 & +5 \\
x \geq 11.5 & x \leq-1.5
\end{array}
$$

(4) $4 m^{5} \cdot 3 m^{-7}=\frac{12}{m^{2}}$
(5) $\frac{x^{2}}{w^{-7}} \cdot \frac{x^{3} w^{2}}{x}=x^{4} w^{9}$
(6) $\left(\frac{m^{5} n^{-3}}{y}\right)^{-2}=\frac{y^{2} n^{6}}{m^{10}}$


4-22. Solve $(x-3)^{2}-2=x+1$ graphically

4-23. Graph a system of equations to solve $2|x-4|-3=\frac{2}{3} x-3$.

$$
\begin{aligned}
& y=2|x-4|-3 \\
& y=\frac{2}{3} x-3
\end{aligned}
$$

$y=|x|$


4-24. Solve each of the following equations using any method.
a. $-3 \sqrt{2 x-5}+7=-8$

$$
\text { b. } 2|3 x+4|-10=12
$$

4-27. Solve the following equations. Be sure to check your answers for any extraneous solutions.

$$
\text { a. } \sqrt{2 x-1}-x=-8
$$

$$
\begin{aligned}
& (\sqrt{2 x-1})^{2}=(x-8)^{2} \\
& 2 x-1=(x-8)(x-8)
\end{aligned}
$$

b. $\sqrt{2 x-1}-x=0$

4-28. Find the value of $x$.
a.

b.


## Use the solutions to check your answers carefully.

You have 5 minutes.<br>-Use a pen, record your scores

## AIM today:

- Determine the meaning of the solutions of systems ( as they relate to their graphs )
- Find solutions to complex systems

What do solutions to

- Systems look like?

What do solutions look like?

$$
\frac{2}{x}=5 \sqrt{x+5}-6
$$

$$
\begin{aligned}
& x+2 y=7 \\
& 3 x-y^{2}=18
\end{aligned}
$$

Not a system
A complex system

$$
x=
$$

$$
\begin{aligned}
& x= \\
& y= \\
& =
\end{aligned},
$$

The solution of a system of equations will be a pair of values

$$
\begin{aligned}
& x+2 y=7 \\
& 3 x-y^{2}=18
\end{aligned}
$$



$$
\begin{aligned}
& x^{2}+y^{2}=25 \\
& y=x^{2}-13
\end{aligned}
$$



You will be given 4 systems. (a,b,c,d)
Follow the instructions on the hand out

INSTRUCTIONS: Solve each of the four SYSTEMS of the equations the following way.

1. • Solve algebraically first.
2. Then graph the system (and make a quick sketch)
3. Explain what the meaning of the algebraic solution tells you about the graph.

## You can do the work on the hand out or

 in your own notes. This work will be a good resource for tonight's assignment and upcoming work.b $y=\frac{1}{2} x^{2}+1$

$$
y=2 x-1
$$



(a)

$$
\begin{gathered}
y=-3 x+5 \\
y=-3 x-1 \\
-3 x+5=-3 x-1 \\
5=-1
\end{gathered}
$$

a false statement which means....
NO SOLUTIONS
(a)

$$
\begin{aligned}
& y=-3 x+5 \\
& y=-3 x-1 \\
&-3 x+5=-3 x-1 \\
& 5=-1
\end{aligned}
$$

a false statement which means....
NO SOLUTIONS
(a)

$$
\begin{gathered}
y=-3 x+5 \\
y=-3 x-1 \\
-3 x+5=-3 x-1 \\
5=-1
\end{gathered}
$$

a false statement which means....
NO SOLUTIONS

b

$$
\begin{aligned}
& y=\frac{1}{2} x^{2}+1 \\
& y=2 x-1
\end{aligned}
$$

$$
\text { (b) } \begin{aligned}
& y=\frac{1}{2} x^{2}+1 \\
& y=2 x-1 \\
& \frac{1}{2} x^{2}+1=2 x-1 \\
& \frac{1}{2} x^{2}=2 x-2 \\
& x^{2}=4 x-4 \\
& x^{2}-4 x+4=0 \\
& x=2 \longrightarrow \begin{array}{l}
x=2 \\
y=3
\end{array}
\end{aligned}
$$

(b)

$$
\begin{gathered}
y=\frac{1}{2} x^{2}+1 \\
y=2 x-1 \\
\frac{1}{2} x^{2}+1=2 x-1 \\
\frac{1}{2} x^{2}=2 x-2 \\
x^{2}=4 x-4 \\
x^{2}-4 x+4=0 \\
x=2 \rightarrow \begin{array}{c}
x=2 \\
y=3
\end{array}
\end{gathered}
$$

What did the Solutiontell US?

The line is tangent to the parabola.

C

$$
\begin{gathered}
y^{2}=x \\
y=x-2
\end{gathered}
$$

Try something
can ask for a hint in a bit
(c)

$$
\begin{aligned}
& \begin{array}{l}
y^{2}=x \\
y=x-2
\end{array} \quad \begin{array}{l}
\sqrt{y^{2}}=\sqrt{x} \\
y= \pm \sqrt{x}(4,2)(1,-1) \\
y=y^{2}-2
\end{array} \\
& 0=y^{2}-y-2 \\
& 0=(y+1)(y-2) \\
& \sum^{y}=\left\{\begin{array}{l}
y=-1
\end{array}\right. \\
& y=2 \quad
\end{aligned}
$$



A line intersects a sideways (sleepy) parabola at two different points
(d)

$$
\begin{aligned}
& 4 x-2 y=10 \\
& y=2 x-5
\end{aligned}
$$

(d)

$$
4 x
$$

$$
4 x-2 y=10
$$

$$
y=\frac{2 x-5}{2}
$$

$$
4 x-2(2 x-5)=10
$$

$$
4 x-4 x+10=10
$$

$$
10=10
$$

true

Assignment
4..... 40-43, 44c

You can replace any question from the above assignment

$$
x^{2}+y^{2}=25
$$ $\begin{aligned} & \text { with a more } \\ & \text { challenging system }\end{aligned} \hat{y}=x^{2}-13$

- 

You can check your answer with we
with that
in mind


$$
4-37
$$

a you

C together


(C) combine to create new
(c)

$$
\begin{aligned}
& x^{2}+y^{2}=25 \quad y=x^{2}-13 \text { the difficult } \\
& x^{2}+\left(x^{2}-13\right)^{2}=25 \\
& x^{2}+\left(x^{2}-13\right)\left(x^{2}-13\right)=25 \\
& \text { Yikes ! }
\end{aligned}
$$

$$
\begin{aligned}
& x^{2}+y^{2}=25 \quad y=x^{2}-13 \quad \text { the ea } \\
& x^{2}=y+13 \\
& ( \pm \sqrt{y+13})^{2}+y^{2}=25 \\
& y+13+y^{2}=25 \\
& y^{2}+y-12=0 \\
& x=y=-4 \quad y=3
\end{aligned}
$$

(d)


$$
q=x^{2}
$$

\& two of the four points are

$$
x= \pm \sqrt{9}
$$

$$
x= \pm 3
$$ $(-3,-4)$ and $(3,-4)$ then plug in $y=3$ to find the other two

