

homework help



Pick up the

WARM UP!

1. Powell was trying to solve the quadratic equation $x^2 + 2.5x - 1.5 = 0$. “I think I need to use the Quadratic Formula because of the decimals,” she told Walter. Walter replied, “I’m sure there’s another way! Can’t we rewrite this equation so there aren’t any decimals?”

What is Walter talking about? Rewrite the equation so that it has no decimals. You don’t need to solve it!

$$x^2 + 2.5x - 1.5 = 0$$

$$10x^2 + 25x - 15 = 0$$

$$2x^2 + 5x - 3 = 0$$

2. Re-write the following three equations (or system), but do **not** solve them.

a. $\underbrace{100x^2}_{100} + \underbrace{100x}_{100} = \underbrace{2000}_{100}$

$$x^2 + x = 20$$

b. $15x + 10y = -20$
 $7x - 2y = 24$

$$\rightarrow 3x + 2y = -4$$

$$7x - 2y = 24$$

$$c. \frac{1}{3}x^2 + \frac{x}{2} - \frac{1}{3} = 0$$

$$6 \cdot \frac{1}{3}x^2 + 6 \cdot \frac{x}{2} - 6 \cdot \frac{1}{3} = 0 \cdot 6$$

$$2x^2 + 3x - 2 = 0$$

$$6() \quad 6() \quad 6() \quad 6()$$

• Consider each of the following equations and systems. would substitution make them easier to solve? What expression might you temporarily replace with U ?

You do not need to actually solve the equation(s).

$$U = m^2 + 5m - 24$$

a. $(m^2 + 5m - 24)^2 - (m^2 + 5m - 24) = 6$

$$U^2 - U = 6$$

$$U^2 - U - 6 = 0$$

$$U = 3 \quad U = -2$$

$$m^2 + 5m - 24 = 3$$

$$m^2 + 5m - 24 = -2$$

$$(4x^2 + 4x - 3)^2 = (x^2 - 5x - 6)^2$$

?



$$\text{a) } \underset{-5x}{5x} - \underset{-5x}{2y} = 8$$

$$\underset{-2}{-2y} = \underset{-2}{8} - \underset{-2}{5x}$$

$$y = -4 + \frac{5}{2}x$$

$$y = \frac{8 - 5x}{-2}$$

$$\text{b) } \frac{xy}{x} + \frac{3x}{x} = \frac{2}{x}$$

$$y + 3 = \frac{2}{x}$$

$$y = \frac{2}{x} - 3$$

HW

25

JENNA

$$2000x - 4000 = 8000$$

$$\overline{1000} \quad \overline{1000} \quad \overline{1000}$$

$$2x - 4 = 8$$

$$\textcircled{c} \quad \frac{3}{50} - \frac{x}{50} = \frac{7}{50}$$

31

32

a

$$\begin{aligned} & (x^3 y^{-2})^{-4} \\ & (x^3)^{-4} (y^{-2})^{-4} \\ & x^{-12} \cdot y^8 \end{aligned}$$

$$= \frac{y^8}{x^{12}}$$

b

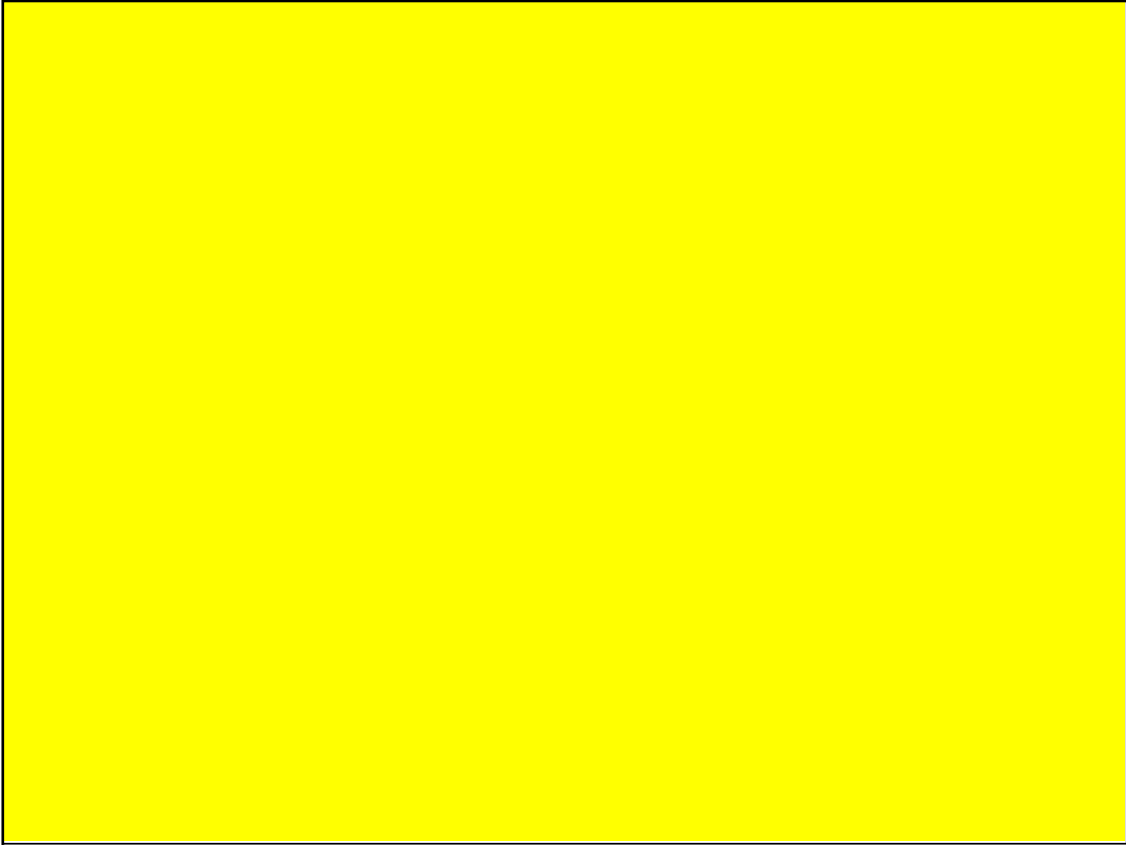
$$\begin{aligned} & -3x^2 (6xy - 2x^3y^2z) \\ & -3x^2 \cdot 6xy + 3x^2 \cdot 2x^3y^2z \\ & -18x^3y + 6x^5y^2z \end{aligned}$$

35

a circle radius 12
center $(-2, 13)$

$$x^2 + y^2 = r^2$$

b center $(-1, -4)$ radius 1



The strategy used in the warm
up can be described as:

Solving by re-writing

NOTES

Solving equations by re-writing



Example 1

$$\cancel{(x)}\cancel{(x-1)}\left(\frac{x-3}{x}\right) + \frac{\cancel{(x)}2\cancel{(x-1)}}{x-1} = \left(\frac{5-x}{x}\right)\cancel{(x-1)}\cancel{(x)}$$

multiply by x and $x-1$

$$\cancel{(x-1)}\cancel{(x-3)} + 2x = (5-x)\cancel{(x-1)}$$

$$x^2 - \underline{3x} - \underline{x} + 3 + \underline{2x} = \underline{5x} - 5 - x^2 + \underline{x}$$

$$x^2 - 2x + 3 = -x^2 + 6x - 5$$

$$2x^2 - 2x + 3 = 6x - 5$$

$$2x^2 - 8x + 8 = 0$$

$$x^2 - 4x + 4 = 0$$

$$a=1$$

$$b=-4$$

$$c=4$$

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(4)}}{2(1)} = \frac{4 \pm \sqrt{6}}{2}$$

$$= \frac{4}{2}$$

$$x = 2$$

Example 2 - Rewrite to a familiar form

$$x^2 + y^2 + 10x + 8y = 8$$

$$x^2 + 10x + 25 + y^2 + 8y + 16 = 8 + 25 + 16$$

$$(x+5)^2 + (y+4)^2 = 49$$

$$\left(\frac{10}{2}\right)^2$$

25

$$r = 7$$

center $(-5, -4)$

Last
thing
of the day

a) Are the functions equivalent?

$$y = (x-3)(x-5) \quad y = 2(x-3)(x-5)$$

Do they have the same roots?

b) Find roots

$$0 = (x-3)(x-5) \quad 0 = 2(x-3)(x-5)$$

ZPP ZPP

$$(x-3)=0 \quad (x-5)=0 \quad x-3=0 \quad x-5=0$$
$$x=3 \quad x=5 \quad x=3 \quad x=5$$

both have
same roots

ROOTS

- ① A root is a value that, as an input, makes a function turn to 0
- ② A value of a root is the same as its x-intercept(s)
- ③ Functions that have the same roots are not necessarily equivalent.

B.B.

Assignment :

3 45-46 , 49-50, 53-54

Optional
just for
fun
challenge

→ Solve the
system :

$$\frac{\sqrt{x^2 - 15x}}{2y} = 5$$

$$3\sqrt{x^2 - 15x} - 3y = 27$$

bring me your answer
tomorrow and fill
check it.

So, now the
infamous #6

f.
$$\frac{\sqrt{x^2 - 15x}}{2y} = 5$$

$$3\sqrt{x^2 - 15x} - 3y = 27$$

Question # 39 deals with the infamous problem

$$\begin{array}{l}
 2y \cdot \frac{\sqrt{x^2-15x}}{2y} = 2y \cdot 5 \\
 \frac{3\sqrt{x^2-15x}-3y}{3} = \frac{27}{3}
 \end{array}
 \Rightarrow
 \begin{array}{l}
 \sqrt{x^2-15x} = 10y \\
 \sqrt{x^2-15x} - y = 9
 \end{array}
 \Rightarrow
 \begin{array}{l}
 y = \frac{\sqrt{x^2-15x}}{10} \\
 y = \sqrt{x^2-15x} - 9
 \end{array}$$

$$\begin{array}{l}
 2y \cdot \frac{\sqrt{x^2-15x}}{2y} = 2y \cdot 5 \\
 \frac{3\sqrt{x^2-15x}-3y}{3} = \frac{27}{3}
 \end{array}
 \Rightarrow
 \begin{array}{l}
 \sqrt{x^2-15x} = 10y \\
 \sqrt{x^2-15x} - y = 9
 \end{array}
 \Rightarrow
 \begin{array}{l}
 y = \frac{\sqrt{x^2-15x}}{10} \\
 y = \sqrt{x^2-15x} - 9
 \end{array}$$

Graciela and Walter realized they had a big mess to try to solve. “Wait,” Graciela said. “*There’s an easier way. Let’s use substitution to make this system simpler!*”

do parts b → d

$$\sqrt{\frac{x^2 - 15x}{10}} = \sqrt{x^2 - 15x} - 9$$

$$y = \frac{\sqrt{x^2 - 15x}}{10}$$
$$y = \sqrt{x^2 - 15x} - 9$$