

# Pick Up the Warm Up

- Turn in LCQ 10.2  
=

A telephone survey with regard to support of a bond issue resulted in:

Age:	21-30	31-40	41-50	51-60	61-70	71-80	Total
For:	45	32	28	25	15	8	153
Against:	30	43	47	50	60	67	297

Which of the following sampling strategies was most likely used?

- (A) Cluster sampling      (D) Stratified sampling  
 (B) Proportional sampling      (E) Systematic sampling  
 (C) Simple random sampling

*Answer:* (D) Given the exact same number of people surveyed in each age group, stratified sampling was probably the strategy used. In stratified sampling, the population is divided into homogeneous groups called strata (for example, by age), and random samples of persons from all strata are chosen. We could further do proportional sampling where the sizes of the random samples from each stratum depend on the proportion of the total population represented by the stratum (not done in this case because equal size samples were picked from each age group). In cluster sampling, the population is divided into heterogeneous groups called clusters, and we then take a random sample of clusters from among all the clusters.

To conduct a survey on holiday shopping patterns, a researcher opens a telephone book to a random page, closes his eyes, puts his finger down on the page, and then reads off the next 100 names. Which of the following is *not* a true statement?

- (A) The survey incorporates chance.
- (B) The procedure results in a systematic sample.
- (C) The procedure could easily result in selection bias.
- (D) The procedure is not a simple random sample.
- (E) The use of a phone book will result in undercoverage bias.

*Answer: (B)* A systematic sample involves picking every  $n$ th name on the list not  $n$  in a row. There is a very real chance of *selection bias*. For example, a number of relatives with the same name and similar holiday shopping patterns might be selected. All possible groups of size 100 do not have the same chance of being picked, and so the result is not a simple random sample. Undercoverage bias is present because those with unlisted land phones or with cell phones are not in the phone book, and so are not part of the sampling frame.

## Clarification on Starting Confidence Intervals and Significance Tests

starting a TEST

$H_0$

$H_a$

define variables

Starting a CI

95% Confidence interval

$P_1 =$

$P_2 =$

or

$P_1 - P_2 =$

**STATE** 99% C.I. for  $p_1 - p_2$

where  $p_1$  = true prop. of patients who would report reduced lower back pain taking naxproren & Valium  
 $p_2$  = true proper. of patients who would report reduced lower back pain after taking naxproren and a placebo.

TEST

**STATE**

(a) Is there convincing evidence that there is a all women in this city who intended to vote

✓  $H_0: p_m - p_f = 0$

$H_a: p_m - p_f \neq 0$

✓  $p_m$  = true proportion of all male regist. voters who intended to vote Trump.

$p_f$  = true proport. of all female voters who intended to vote Trump

✓  $\alpha = 0.05$

↓  
 or....  
 $p_1 - p_2$  = true difference in proportions (male - female) who .....

LEC 10.1  
part 2b

the order of context needs to be clear

95% Confid. Interval (for  $P_M - P_F$ )

$P_M$  = true proportion of all male registered voters who intended to vote for Trump.

$P_F$  = true proportion of all female voters who intended to vote for Trump.

OR  $P_M - P_F \rightarrow$  true difference in the proportion of men and women (men-women) who intended to ...

When designing an experiment to compare two means, a completely randomized design may not be the best option.

A matched pairs design might be a better choice.....

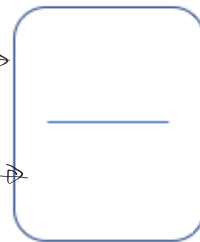
# Activity page 684

## "Get your Heart Beating"

Standardizing the Way We Measure  
(will reduce variability in the results)

Standing Pulse rates  
get recorded on top

Sitting



handout

Do a 2-sample t test (if conditions are met) to determine if there is convincing evidence that standing pulse rates are higher on average.

Can do informally

- just do the State step for now.
- in the open space.

Do a 2-sample t test (if conditions are met) to determine if there is convincing evidence that standing pulse rates are higher on average.

⌘

State  $H_0: \mu_{\text{stand}} - \mu_{\text{sit}} = 0$

$H_a: \mu_{\text{stand}} - \mu_{\text{sit}} > 0$

Plan Two-sample t test for  $\mu_1 - \mu_2$

Random •

10% •

Normal •

DO

$$\bar{X}_{\text{stand}} = 73$$

$$S_{\text{stand}} = 13.6$$

$$\bar{X}_{\text{sit}} = 71$$

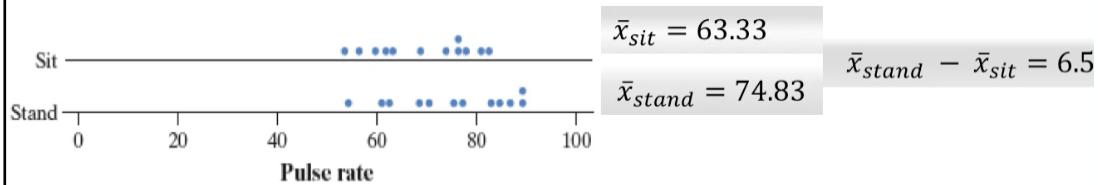
$$S_{\text{sit}} = 15.4$$

2 Samp T Test gives  $t = 0.20$   
and P-value = .42 using  $df = 6.12$

Conclude

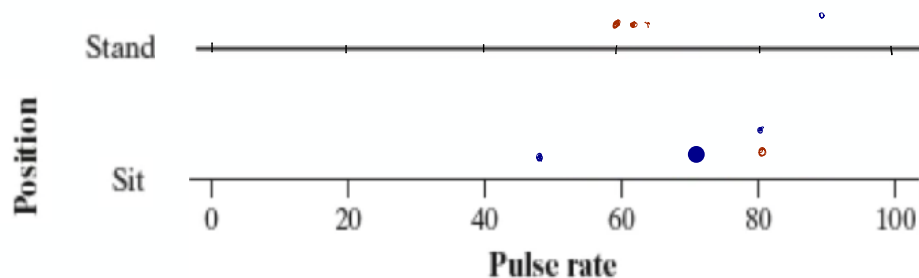
## Experiment #2 Matched Pairs Design

# example from another class



A two-sample t test of  $H_0: \mu_{stand} - \mu_{sit} = 0$  versus  $H_a: \mu_{stand} - \mu_{sit} > 0$  yields  $t = 1.42$  and a P-value of 0.09. These data do not provide convincing evidence that standing pulse rates are higher, on average, than sitting pulse rates for people like the students in this class

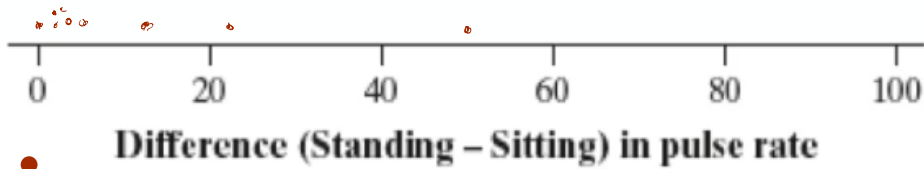
Write your rate on the side board and  
put a dot on the plot below



→ Is there some evidence that the standing pulse rates are higher, on average?



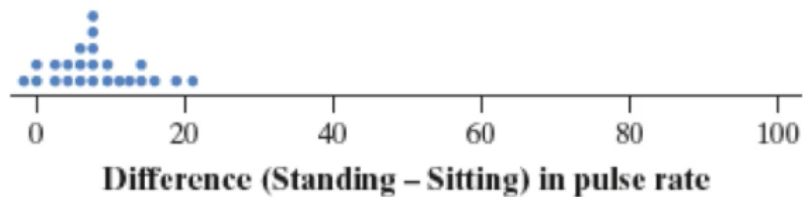
randomized design P-Value = .42  
 Matched pairs - P value = .03

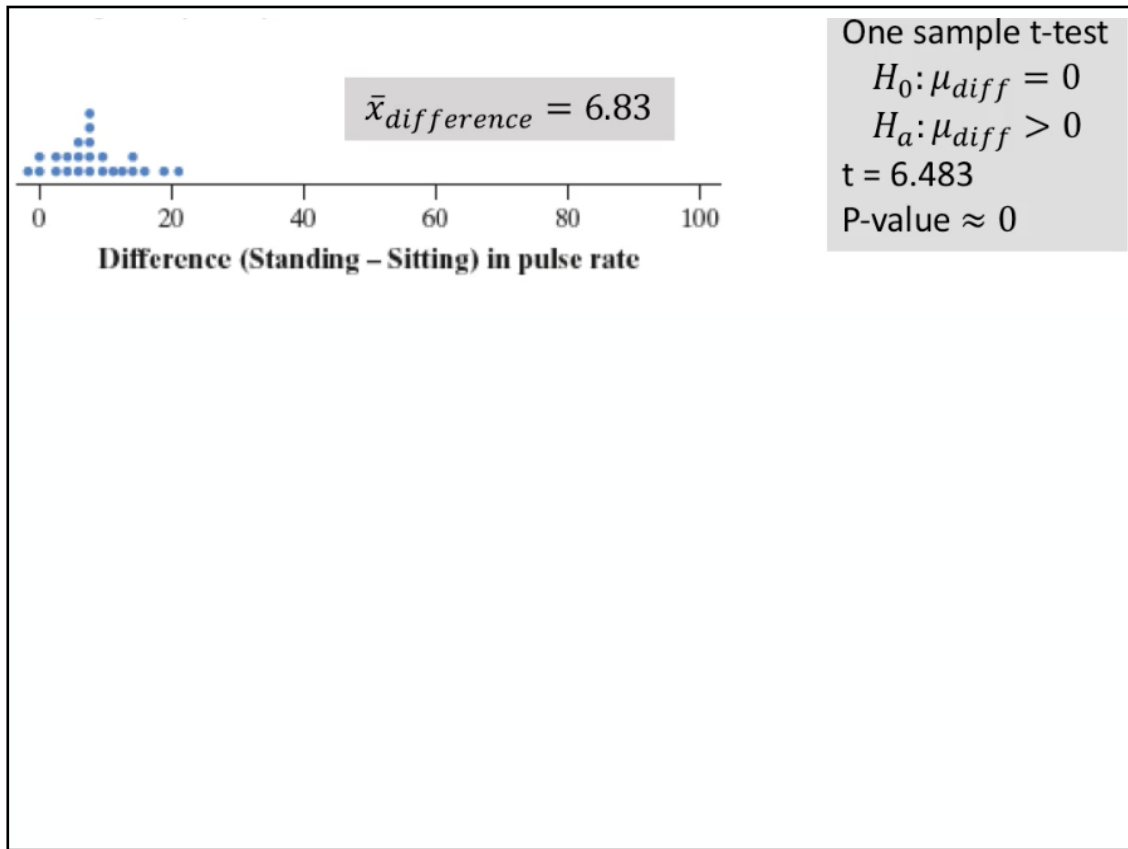


$H_0: \mu_{diff} = 0$

Is there some evidence that standing pulse rates are higher, on average?

Sample class





Conduct a one-sample t Test for  $\mu_{diff}$

$H_0: \mu_{diff} = 0$   
 $H_a: \mu_{diff} > 0$

DO

$\bar{X}_{diff} =$

$S_{diff} =$

T-TEST gives

$t =$  and

$P =$

Which design provides more convincing evidence?

Matched pairs design reduced variability in the response variable

- ... by accounting for a big source of variability - the difference between individuals.

Matched pairs design reduced variability in the response variable

- ... by accounting for a big source of variability - the difference between individuals.

and that makes it easier to detect the fact that standing causes an increase in pulse rate.

↑  
avg.



Using a Paired Design (rather than completely rand. design)

- likely has a smaller P-value
- provides more convincing evidence for  $H_a$

### Using a Paired Design (rather than completely rand. design)

- likely has a smaller P-Value
- provides more convincing evidence for  $H_a$
- results in more POWER.

### Using a Paired Design (rather than completely rand. design)

- likely has a smaller P-Value
- provides more convincing evidence for  $H_a$
- results in more POWER.

↖  
this is because there will likely be more variability in the completely rand. design.

# Choosing the Correct Inference Procedure

## Paired Data or Two Samples?

$$\mu_1 - \mu_2$$

**Two-sample t procedures** require data that come from *independent random samples* from the two populations of interest or from *two groups in a randomized experiment*.

10.1  
10.2

$$\mu_{diff}$$

**Paired t procedures** require *paired data* that come from *a random sample* from the population of interest or from *a randomized experiment*.

10.3

handout

handout  
😊

handout

Caution! The proper \_\_\_\_\_ method depends on how the data were \_\_\_\_\_.

handout

Caution! The proper Inference method depends on how the data were Produced.

It can be difficult  
to decide when to use a  
two-sample  $t$  test or a  
paired  $t$  test.

• especially when mixed  
in with all of the  
others.



**1. How many samples do I have?**

One:

Two:

**2. Can any piece of data in the first group be compared to any piece of data in the second?**

If yes:

If no:

**3. Do they represent pairing the data?**

Yes:

No:

**1. How many samples do I have?**

One:  $\mu$  diff

Two:  $\mu_1 - \mu_2$  (Usually watch out for 2 samples that pair individuals)

**2. Can any piece of data in the first group be compared to any piece of data in the second?**

If yes:  $\mu_1 - \mu_2$

If no: if they must stay pairs  $\mu$  diff

**3. Do they reference pairing the data?**

Yes:  $\mu$  diff

No:  $\mu_1 - \mu_2$

**Other things to look for:**Paired

- Can't scramble a list
- Same # of values in each
- "Mean difference"

Unpaired

- Can scramble a list
- Can have different # of values
- "difference of means"

## Luke's Taco Shop

- look at the first situation
- Get a consensus

**Luke's taco shop**

*Two samples or paired data?*

In each of the following settings, decide whether you should use two-sample  $t$  procedures to perform inference about a difference in means OR paired  $t$  procedures to perform inference about a mean difference. Explain your choice.

(a) Luke's taco shop is considering a switch to a new tortilla that supposedly has a larger diameter. To test this claim, Luke takes a random sample of 50 of the old tortillas and 50 of the new tortillas and records the diameter of each.

-How many samples do I have?

-Can any piece of data in the first group be compared to any piece of data in the second group?

-Are pairs referenced?

(a) **Two-sample  $t$  procedures**; the data come from independent random samples of the old and new tortillas.

(b) Luke's taco shop wants to be sure that the new tortillas taste better than the old tortillas. Luke selects a random sample of 20 regular customers. Each customer is asked to try both tortillas and then record a "taste" score for each. The order in which the customers try the two tortillas is randomized.

-How many samples do I have?

-Can any piece of data in the first group be compared to any piece of data in the second group?

-Are pairs referenced?

#### Paired

- Can't scramble a list
- Same # of values in each
- "Mean difference"

#### Unpaired

- Can scramble a list
- Can have different # of values
- "difference of means"

(b) **Paired  $t$  procedures**; the data come from two measurements of the same variable ("taste" score) for each regular customer.

(c) Luke's taco shop is not sure whether to cook the tortillas in the oven or on the grill. The chefs want tortillas to cook as quickly as possible. Luke sets up an experiment taking a batch of 50 tortillas and randomly assigning half of them to be cooked one at a time in the oven and half of them to be cooked one at a time on the grill. The time it takes until ready to serve is recorded for each tortilla.

-How many samples do I have?

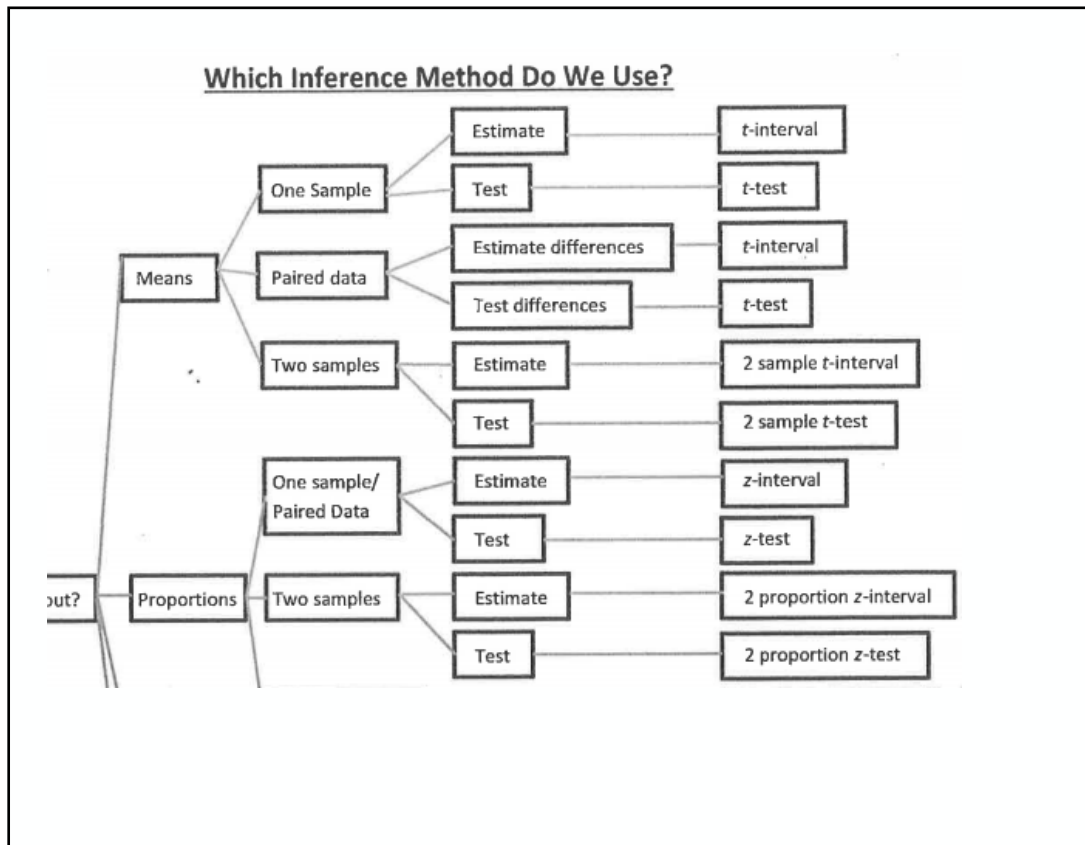
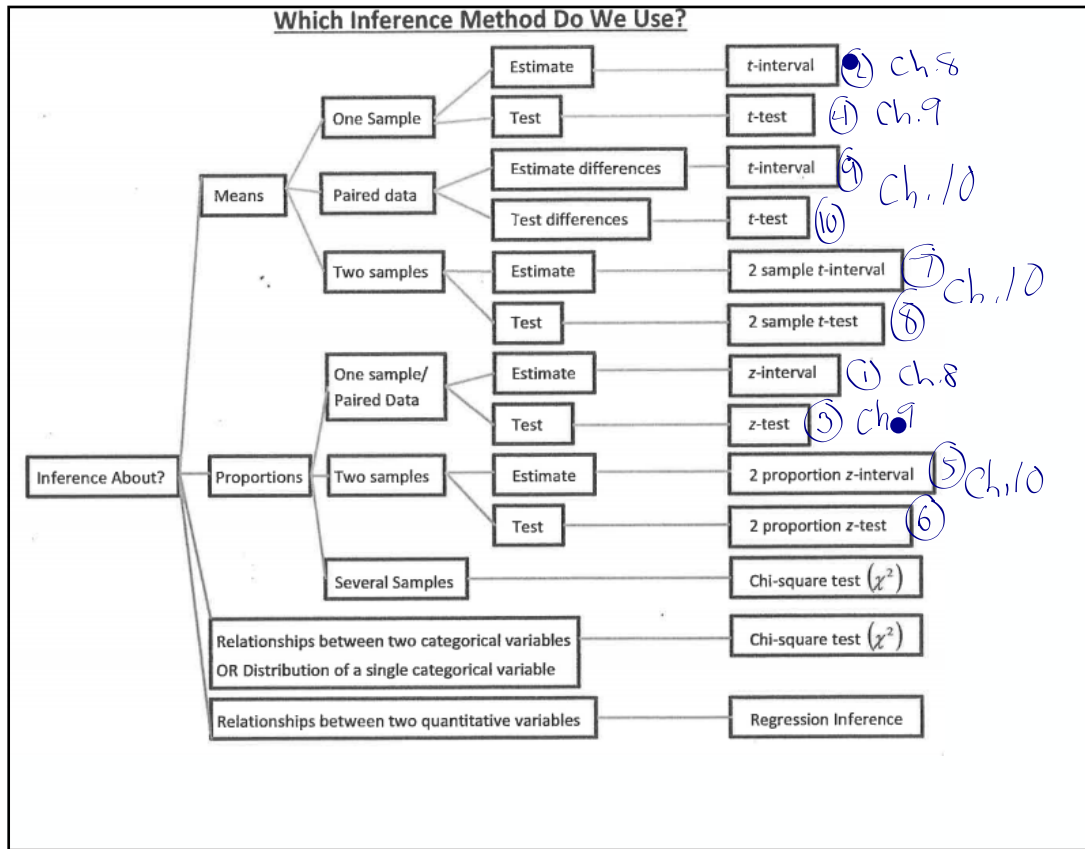
-Can any piece of data in the first group be compared to any piece of data in the second group?

-Are pairs referenced?

(c) **Two-sample  $t$  procedures**; the data come from two groups in a randomized experiment, with each group

back of the  
Warm Up

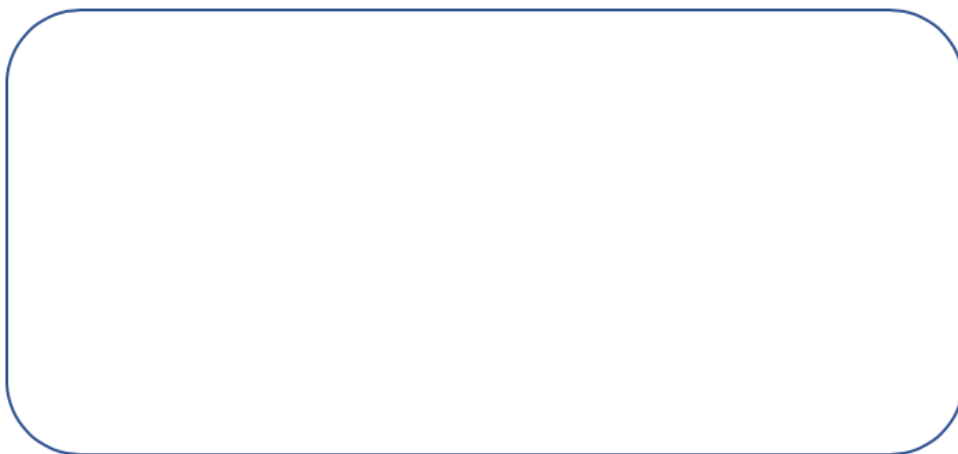
let's check off  
what you know about • in the order  
(as far as inference) we learned them



# Choosing the correct inference procedure

handout

## **Choosing the Correct Inference Procedures**



## Choosing the Correct Inference Procedures



## Choosing the Correct Inference Procedures

Estimate or a Test ?  
CI                      signif. Test

## Choosing the Correct Inference Procedures

Estimate or a Test ?

CI

signif. Test

Proportions or means ?

z

t

## Choosing the Correct Inference Procedures

Estimate or a Test ?

CI

signif. Test

Proportions or means ?

z

t

one sample or two ?

↳ Unpaired ?  
↳ Paired ?



A food scientist wants to estimate the difference between the weights of eggs classified as jumbo and large. They plan on taking a sample of eggs of each type and comparing the average weight between the samples.

Which of these inference procedures is most appropriate?

Choose 1 answer:

- (A) A  $t$ -interval for slope
- 
- (B) A two-sample  $t$ -interval for the difference of means
- 
- (C) A two-sample  $z$ -interval for the difference of proportions
- 
- (D) A paired  $t$ -interval for a mean difference
- 
- (E) A  $z$ -interval for a proportion
- 

Estimate or a Test ?  
CI                      signif. Test

Proportions or means ?  
z                      t

one sample or two ?

→ Unpaired ?  
→ Paired ?



CORRECT (SELECTED)

A two-sample  $t$ -interval for the difference of means

They are interested in the *average* weights, so they should use  $t$  procedures for a *mean*. They are comparing the means between two independent samples, so two-sample procedures are appropriate.

Finn blogs about video games. In a particular game, a certain enemy occasionally drops a rare item when they are defeated. Finn wants to estimate the likelihood that this enemy drops the rare item, so he defeats the enemy 1000 times and tallies how many times the rare item is dropped.

Which of these inference procedures is most appropriate?

(A) A paired  $t$ -interval for the mean difference

(B) A  $t$ -test for a mean

(C) A  $t$ -interval for a mean

(D) A  $z$ -interval for a proportion

(E) A  $z$ -test for a proportion

2

Estimate or a Test ?  
CI                      signif. Test

Proportions or means ?  
z                              t

one sample or two ?

↳ Unpaired ?  
↳ Paired ?



CORRECT (SELECTED)

A z-interval for a proportion

Finn wants to *estimate*, so he should use an *interval*. He's tallying a *categorical* variable, so looking at a *proportion* is appropriate.

A test prep course takes a random sample of 50 its customers. Researchers score each customer on a diagnostic test before taking the course and again on a similar test after taking the course. They want to use these results to estimate the average difference between the before and after scores.

Which of these inference procedures is most appropriate?

- (A) A  $t$ -interval for slope
- 
- (B) A paired  $t$ -interval for the mean difference
- 
- (C) A two-sample  $z$ -interval for the difference of proportions
- 
- (D) A  $z$ -interval for a proportion
- 
- (E) A two-sample  $t$ -interval for the difference of means
- 

3

Estimate or a Test ?  
CI                      signif. Test

Proportions or means ?  
z                      t

one sample or two ?

→ Unpaired ?  
→ Paired ?

A test prep course takes a random sample of 50 its customers. Researchers score each customer on a diagnostic test before taking the course and again on a similar test after taking the course. They want to use these results to estimate the average difference between the before and after scores.

Which of these inference procedures is most appropriate?

- CI ~~CI~~ mean
- Paired 3
- A ~~t~~-interval for slope
- 
- A paired  $t$ -interval for the mean difference
- 
- A two-sample ~~z~~-interval for the difference of proportions
- 
- A ~~z~~-interval for a proportion
- 
- A two-sample  $t$ -interval for the difference of means
- 

Lylah created an app, and she recently updated the app. She randomly samples a group of users to estimate what percentage of all users are using the updated version.

Which of these inference procedures is most appropriate?

Choose 1 answer:

- 4
- A  $t$ -test for a mean
- 
- A  $z$ -interval for a proportion
- 
- A paired  $t$ -test for the mean difference
- 
- A  $z$ -test for a proportion
- 
- A  $t$ -interval for a mean
-

Estimate or a Test ?  
 CI                      Signif. Test

Proportions or means ?  
 z                      t

one sample or two ?  
 ↘ Unpaired ?  
 ↘ Paired ?



INCORRECT

A  $t$ -test for a mean

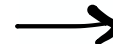
Lylah wants to *estimate*, so she should use an *interval*, not a test. She's tallying a *categorical* variable, so looking at a *proportion* is more appropriate than a mean.



CORRECT (SELECTED)

A  $z$ -interval for a proportion

Lylah wants to *estimate*, so she should use an *interval*. She's tallying a *categorical* variable, so looking at a *proportion* is appropriate.



INCORRECT

A paired  $t$ -test for the mean difference

Lylah collected one data point (whether or not they have the updated version) for each user, so she doesn't have paired data. Also, this data is *categorical*, so looking at a *proportion* is more appropriate than a mean.



INCORRECT

A *z*-test for a proportionLylah wants to *estimate*, so she should use an *interval*, not a test.

INCORRECT

A *t*-interval for a meanLylah is tallying a *categorical* variable, so looking at a *proportion* is more appropriate than a mean.

10.3.....91, 93, 95-97  
and study.... pp.683 - 685

*Test on Wednesday*