

Pick Up the Warm Up
but only do #1 and 2
for now.

Have your χ^2 packet available (pink color)

Warm Up

Practicing Using the Chi-Square Test of Independence

Use your notes as needed. ($5-1$)

	red	green	blue	black	silver
male					
female					

1. A researcher consulted 500 men and women to see if the colour of the car they drove was independent of gender. The colours were red, green, blue, black, and silver. A χ^2 test was conducted at the 5% significance level and the value found was 8.73.

a. Write down the null hypothesis

H_0 : Color and gender are independent

b. Find the number of degrees of freedom. $(2-1)(5-1) = 4$

c. Write down the critical value for this test. 9.488

d. Is car colour independent of gender? Give a clear reason for your answer.

Yes

$$\chi^2 \text{ of } 8.73 < 9.488$$

Since the χ^2 value of 8.73 is not greater than the critical value (9.488), we fail to reject H_0

Therefore, there is not convincing evidence that there is an association between car color preference and gender.

2. Suppose a similar test was conducted on a different population of 300 people. A 5% significance level is used. It was found that the p-value was 0.04. Is colour independent of gender?

$$p = .04$$

Since the p-value < 0.05 , we reject H_0 .

Therefore, we have evidence of an association between car color preference and gender

Two Project Ideas

Aim
for today

The limitations of
the χ^2 Test of Independence

- A. Not enough data
- B. 2×2 adjustment

3.

Consider the contingency table alongside:

- a Construct the expected frequency table.
- b Are any of the expected frequencies less than 5?
- c Combine the data so that none of the cells have an expected frequency less than 5.

	Own a pet?		
	Yes	No	
Age	0 - 19	5	3
	20 - 29	32	22
	30 - 49	42	58
	50+	39	34

Regardless of whether you use Method A or B, what are the first three steps of the χ^2 test of Independence?

1. Contingency Table/State Hypotheses
2. Calculate Expected Values
3. Check to see if ALL expected values are greater than 5

3.

Consider the contingency table alongside:

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- b Are any of the expected frequencies less than 5?
- c Combine the data so that none of the cells have an expected frequency less than 5.

	Own a pet?		
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Go to step 7 - Method A
(bottom of page)

In a **2 by 2** contingency table:

-- Yate's continuity correction must be used when calculating χ^2

If $df = 1$, we use

$$\chi_{calc}^2 = \sum \frac{(|f_o - f_e| - 0.5)^2}{f_e}$$

where $|f_o - f_e|$ is the **absolute value** or **modulus** of $f_o - f_e$

The following table shows the results from a random sample carried out so that the question about the relationship between education and job satisfaction could be analysed.

		Completed University		
		YES	NO	
Satisfied in job	YES	272	618	890
	NO	238	292	530
		510	910	1420

1. Calculate the expected freq
2. Set up a table to organize.

f_o	f_e	$ f_o - f_e $	$\frac{(f_o - f_e - 0.5)^2}{f_e}$
272	319.65		
618	570.35		
238	190.35		
292	339.65		

$$\chi^2_{calc} = \sum \frac{(|f_o - f_e| - 0.5)^2}{f_e} = 29.1$$

B.B.

Coffee Shop problem

- ✓ Data from a coffee shop in London
- ✓ P3 (look at "simple" and "further" math processes)

Suppose an IB Math Studies
student actually collected
this data

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student actually collected
this data

What type of project could
they create?

- what type of interesting ^{things} could be
investigated?

Ideas

Is age associated with amount of time
in a coffee shop.

Pie chart - To look at distrib. of who
is in the coffee shop

Is occupation assoc. with expenditures
in coffee

Are Age and \$ spent correlation

Look at the distribution of ages
(box plot)

Is occupation as and length of stay
associated?

Ideas

Age of Age in Coffee

LCO

open NOTES

Assignment

Ch.11 Packet

p.341.....#2 (use the χ^2 statistic)

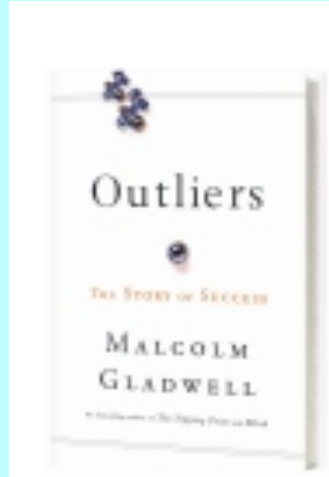
p.344.... #1abcd

p.348.....#4 (use probability)

clearly show all
steps



A small Pennsylvania town.



· Before Test - Questionnaire

Ed.
of
Parent

Pers.
Views
of
math

Income

120 questions
↖