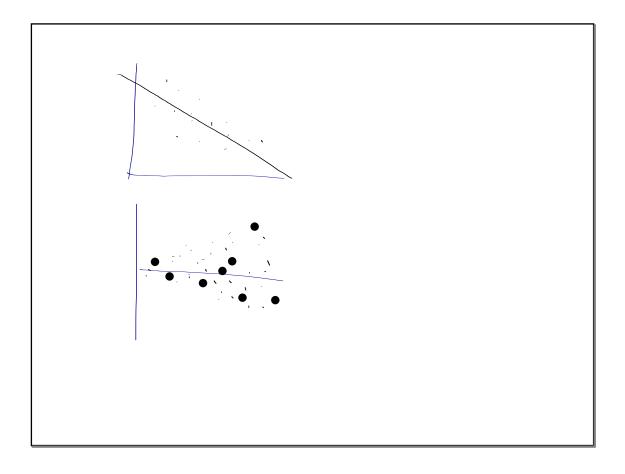
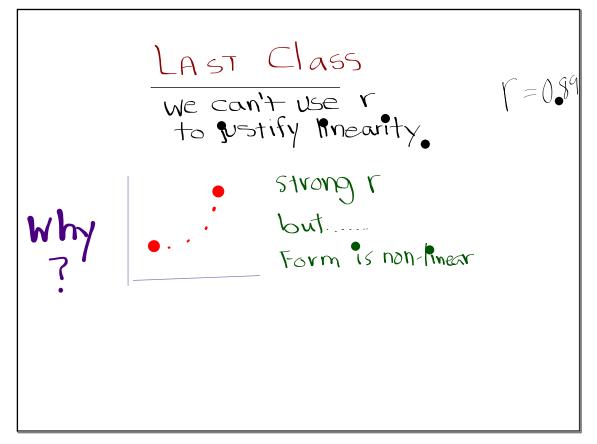
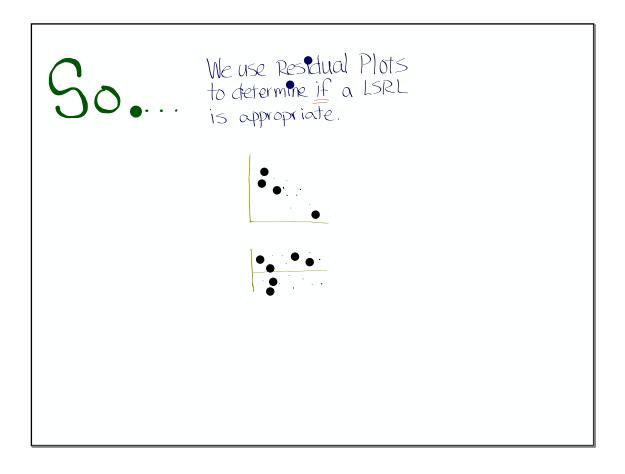
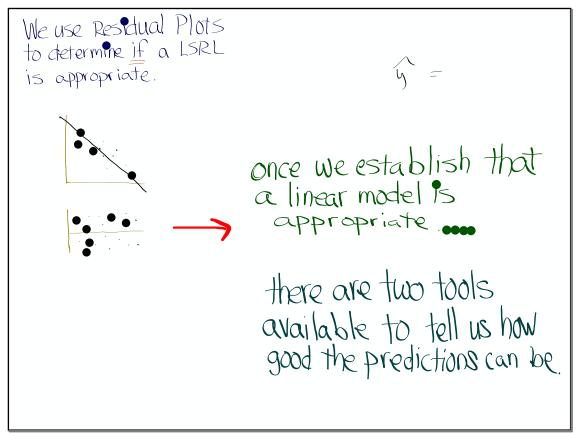
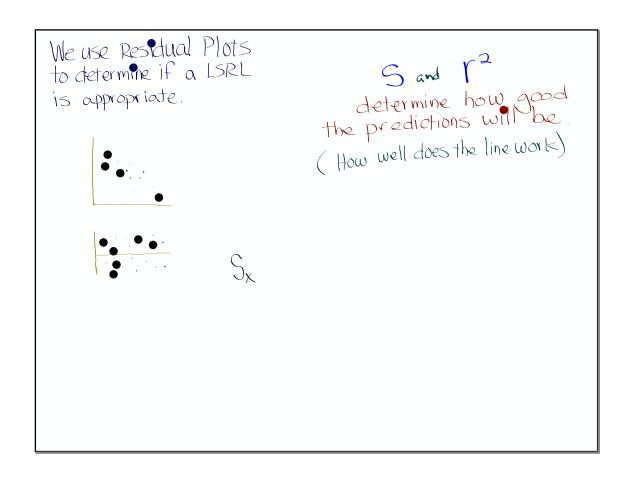
The Role of sand r2 in
Regression
(pages 188-192)

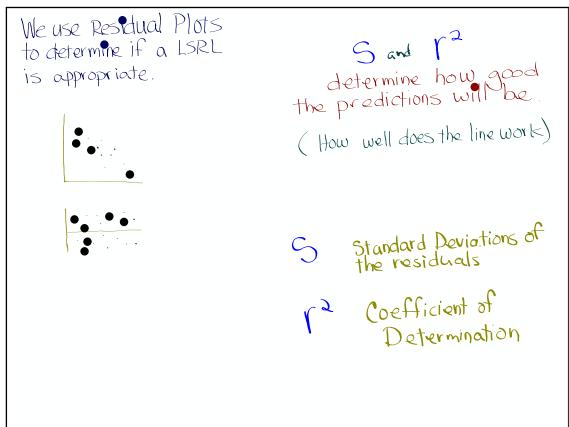


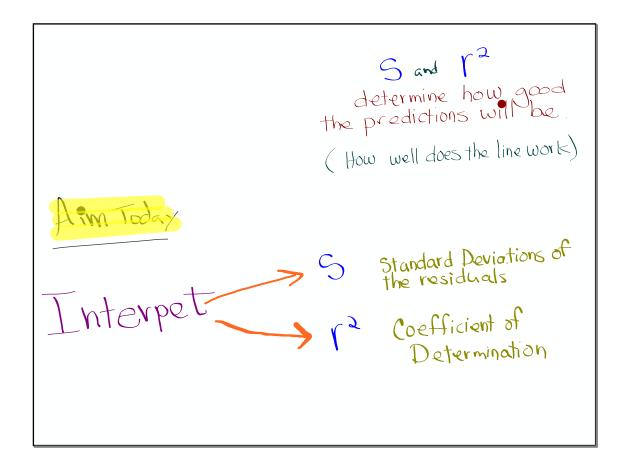








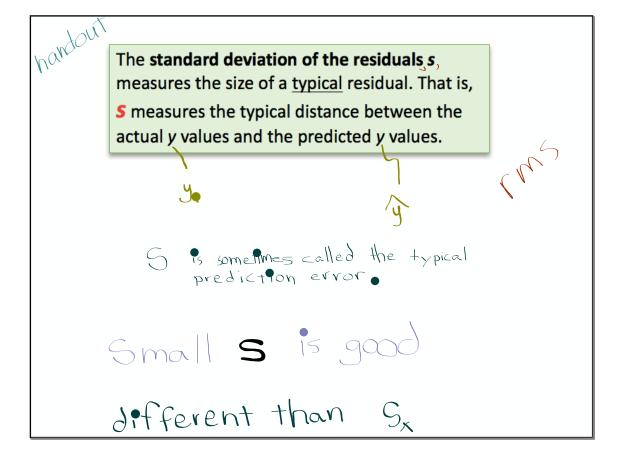


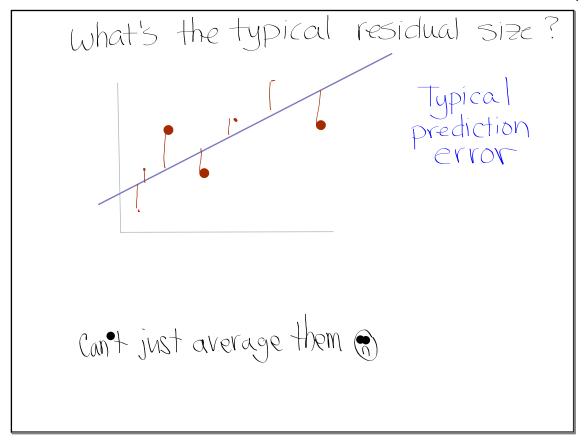


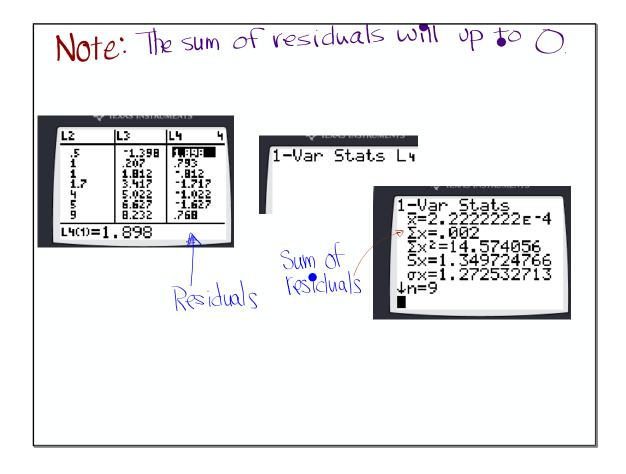
Normally

Experience First - Formalize later

Today - Formalize right away







The **standard deviation of the residuals** *s* measures the size of a <u>typical</u> residual. That is, **s** measures the typical distance between the actual *y* values and the predicted *y* values.

$$s = \sqrt{\frac{\sum residuals^2}{n-2}} = \sqrt{\frac{\sum (y_i - \hat{y})^2}{n-2}}$$

Most likely you will be given this value

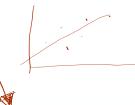
$$S_{x} = \sqrt{\frac{\sum (x_{i} - \bar{x})^{2}}{n - 1}}$$

We divide by n-2 rather than n-1. We used n-1 for s when we estimated the mean (used x for μ). Now we are estimating both slope and the y-intercept, so we use n-2. We subtract one more for each parameter we estimate.

Coefficient of Determination

 r^2 measures the fraction of the variability in the y variable that is accounted for by the LSRL using x.

$$r^2 = 1 - \frac{\sum \text{residuals}^2}{\sum (y_i - \overline{y})^2}$$



The **coefficient of determination** r^2 measures the percent reduction in the sum of squared residuals when using the least-squares regression line to make predictions, rather than the mean value of y.

In other words, r^2 measures the percent of the variability in the response variable that is accounted for by the least-squares regression line.

 r^2 tells us how much better the LSRL does at predicting values of y than simply guessing the mean y for each value in the dataset.

Backpacking

do #1

We'll do #2 and #3 as a class

Backpacking - Ninth-grade students at the Webb Schools go on a backpacking trip each fall. Students are divided into hiking groups of size 8 by selecting names from a hat. Before leaving, students and their backpacks are weighed. The data here are from one hiking group.

Body weight (lb)	120	187	109	103	131	165	158	116
Backpack weight (lb)	26	30	26	24	29	35	31	28

Analyze the data using stapplet.com.

 Using <u>www.stapplet.com</u> find the LSRL of the data. Write it below (in you know what form!)

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1. Using www.stapplet.com find the LSRL of the data. Write it below (in you know what

$$\hat{q} = 16.265 + 0.091 \times$$

$$\hat{y} = 16.265 + 0.091 \times$$

Backpack = 16.265 + 0.091 (Body Weight)

2. Find and interpret **S**, the standard deviation of the residuals.

3. Find and interpret the value of \mathbf{r}^2 , the coefficient of determination.

2. Find and interpret S, the standard deviation of the residuals.

5=227 The actual backpack weight is typically about 2.27 The away from the weight predicted by the LSRL with x = the body weight.

3. Find and interpret the value of \mathbf{r}^2 , the coefficient of determination.

2. Find and interpret **S**, the standard deviation of the residuals.

5=227 The actual backpack weight is typically about 2.27 lb away from the weight Predicted by the LSPL

3. Find and interpret the value of $\boldsymbol{r^2}$, the coefficient of determination.

2. Find and interpret S, the standard deviation of the residuals.

5=2.27 The actual backpack weight is typically about 2.27 lb.

away from the weight predicted by the LSPL

with x = the body weight.

3. Find and interpret the value of r^2 , the coefficient of determination.

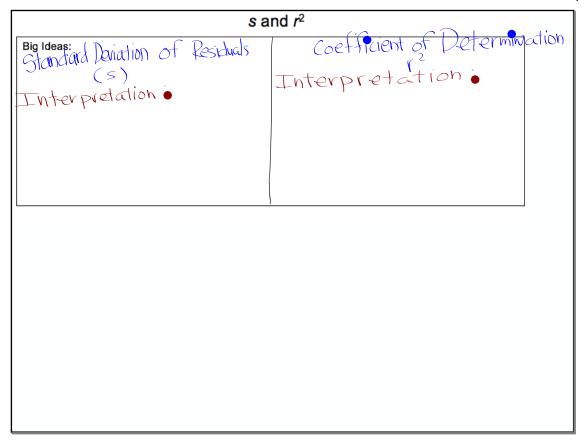
12 = 0.632 About 63.2' of the variability in backpack Weight is accounted for by the LSRL with x= body weight.

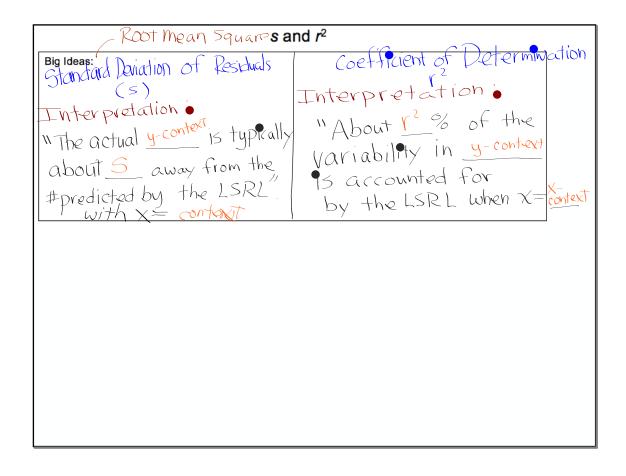
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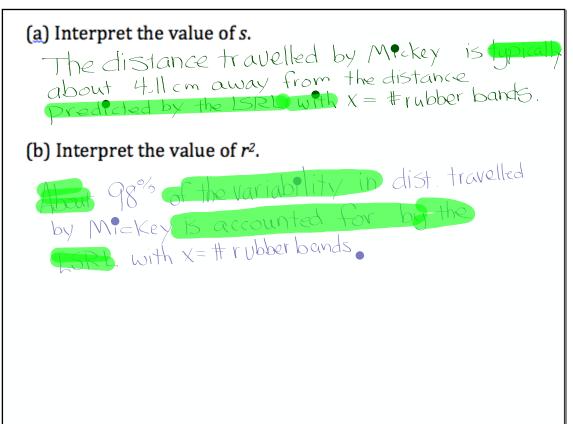
About 63.2 of the variability in backpack weight is accounted for by the LSRR with x= body weight.





Mickey's last bungee jump

- (a) Interpret the value of s.
- (b) Interpret the value of r^2 .



Interpreting Computer Regression Output (pages 192-194)

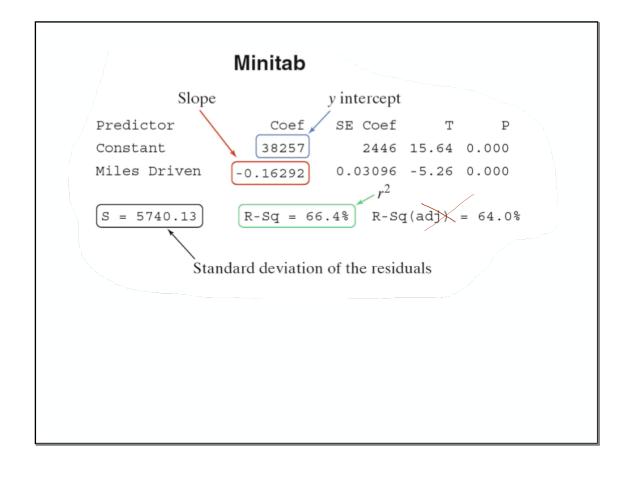
You are not expected to able to use the software but you are expected to interpret the output.

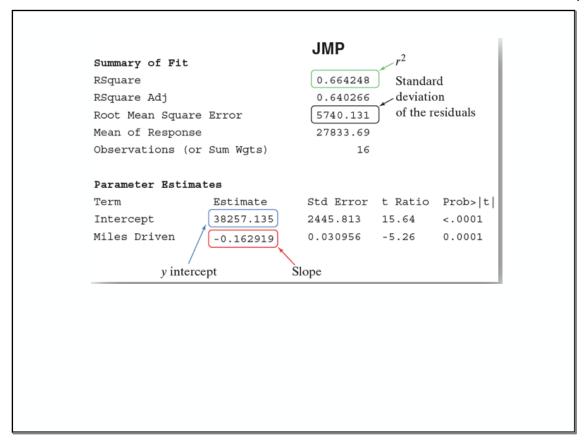
From the output, be sure you can find the:

Slope a
$$\hat{y} = a + bx$$

y-Intercept b

S





Can we predict a school's average SAT math score?

Interpreting regression output

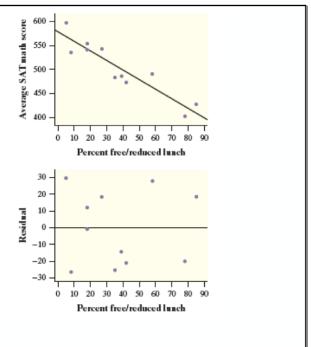
check in w/table mates as you progress

Can we predict a school's average SAT math score? Interpreting regression output

A random sample of 11 high schools was selected from all the high schools in Michigan. The percent of students who are eligible for free/reduced lunch and the average SAT math score of each high school in the sample were recorded.

Students with household income below a certain threshold are eligible for free/reduced lunch.

Here are a scatterplot with the least-squares regression line added, a residual plot, and some computer output:



Predictor	Coef	SE Coef	T	P
Constant	577.9	12.5	46.16	0.000
Foot length	-1.993	0.276	-7.22	0.000
S = 23.3168	R-Sq = 8	5.29% R-Sq	[(adj) =	83.66%
	$r^2 = 85.7$	29		

(a) Is a line an appropriate model to use for these data? Explain how you know the answer.

Because the scatter plot shows a linear association pecause the scure pion shows a leftover pattern, the is and the residual plot shows no leftover pattern, the is applied by Find the correlation. $\Gamma = \pm \sqrt{0.8529} = \pm 0.924$ $\Gamma = \pm \sqrt{0.8529} = \pm 0.924$

(b) Find the correlation.

Find the correlation.
$$\Gamma = \pm \sqrt{0.8529} = \pm 0.924$$
 because the relationship is negative
$$\Gamma = -0.924$$

(a) Is a line an appropriate model to use for these data? Explain how you know the answer.

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Scatter

(b) Find the correlation.

$$\Gamma = \pm \sqrt{0.8529} = \pm 0.924$$

because the relationship is negative $\Gamma = -0.924$

(c) What is the equation of the least-squares regression line that describes the relationship between percent free/reduced lunch and average SAT math score? Define any variables that you

(d) By about how much do the actual average SAT math scores typically vary from the values predicted by the least-squares regression line with x = percent free/reduced lunch?

Jee Your

Assignment:

3.2 55, 57, 59, 67 pp. 188-194