

HW Questions

(no WARM UP yet)



Curving / Scaling of Ch. 7 TEST

Raw score \rightarrow $\boxed{\frac{63}{83}}$



$\boxed{\frac{75}{95}}$

0

100

-20

$$\frac{63}{83}$$

$$\frac{75}{95}$$

$$75.9$$

$$79$$

HW
Questions
?

24

$$y = 3^{(x)}$$

↓ 4

7
→

18

$$\sqrt{(x-4)^2 + (y-3)^2} = \sqrt{25}$$

$$(x-4) + (y-3) = 5 \quad ???$$

No can't take
sq. root of separate
terms.

$$2 + 3$$

$$c=3$$

$$x = \frac{-(2) \pm \sqrt{(2)^2 - 4(1)(3)}}{2(1)} = \frac{-2 \pm \sqrt{24}}{2} = \frac{-2 \pm 2\sqrt{6}}{2}$$

$$x = \frac{2(-1 \pm \sqrt{6})}{2}$$

$x = -1 \pm \sqrt{6}$ are the two ^x intercepts

- 8-17
- a. $y = 3x^2 + 2x^2 + x$ Polynomial
- b. $y = (x-1)^2(x-2)^2$ Polynomial (If multiplied out, every term would be ^{whole number} $\cdot x$)
- c. $y = x^2 + 2^x$ Not because of 2nd term
- d. $y = 3x - 1$ Polynomial
- e. $y = (x-2)^2 - 1$ Polynomial
- f. $y^2 = (x-2)^2 - 1$ Not if you isolated y we would get $y = \pm \sqrt{(x-2)^2 - 1}$

g. $y = \frac{1}{x^2} + \frac{1}{x} + \frac{1}{2}$ Not - the first term would be x^{-2}

h. $y = \frac{1}{2}x + \frac{1}{3}$ Polynomial

i. $y = x$ Polynomial

j. $y = -7$ Polynomial

8-19

$$\begin{aligned}
 \text{a. } & x^2 - 6x + 8 = 0 \\
 & (x-2)(x-4) = 0 \\
 & x-2=0 \quad x-4=0 \\
 & x=2 \quad x=4
 \end{aligned}$$

so roots of equation
are
2 and 4

$$\begin{aligned}
 \text{b. } & x^2 - 6x + 9 = 0 \\
 & (x-3)(x-3) = 0 \\
 & \quad \downarrow \quad \downarrow \\
 & x-3=0 \quad \text{same}
 \end{aligned}$$

3 is the
root of
the equation

$$y = x^2 - 6x + 9$$

$$x^3 - 4x = 0$$

$$\begin{aligned}
 \text{c) } & y = x^3 - 4x \\
 & y = x(x^2 - 4) \\
 & \quad \text{diff. of squares} \\
 & y = x(x+2)(x-2) \\
 & 0 = x(x+2)(x-2) \\
 & \quad \downarrow \quad \downarrow \quad \downarrow \\
 & x=0 \quad x+2=0 \quad x-2=0
 \end{aligned}$$

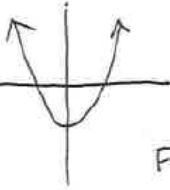
$$x^3 - 4x = 0$$

$$\begin{aligned}
 & x(x^2 - 4) = 0 \\
 & x(x+2)(x-2) = 0 \\
 & \quad \downarrow \quad \downarrow \\
 & \quad x-2=0 \\
 & \quad x=2
 \end{aligned}$$

$$\begin{aligned}
 & x(x^2 - 4) = 0 \\
 & \quad \downarrow \quad \downarrow \\
 & x=0 \quad x^2 - 4 = 0 \\
 & \quad \quad \downarrow \\
 & \quad \quad x^2 = 4 \\
 & \quad \quad \sqrt{\quad} \quad \sqrt{\quad} \\
 & \quad \quad x = \pm 2
 \end{aligned}$$

8-10

$$y = x^2 - 7$$



Find the roots of the equation

Since the graph shows 2 x-intercepts, there must be 2 roots (at least), but since $y = x^2 - 7$ is degree 2, there is at most 2 roots.

$$\text{Set } y = 0 \quad x^2 - 7 = 0$$

$$x^2 = 7$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \pm \sqrt{7}$$

So, $\pm \sqrt{7}$ are the two roots

8-22

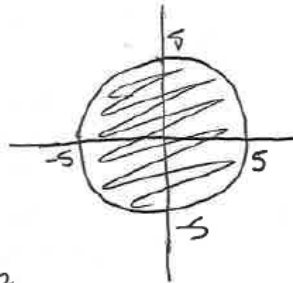
$$\text{Graph } x^2 + y^2 \leq 25$$

TEST (0,0)

$$0^2 + 0^2 \leq 25$$

true

so, shade inside



8-24

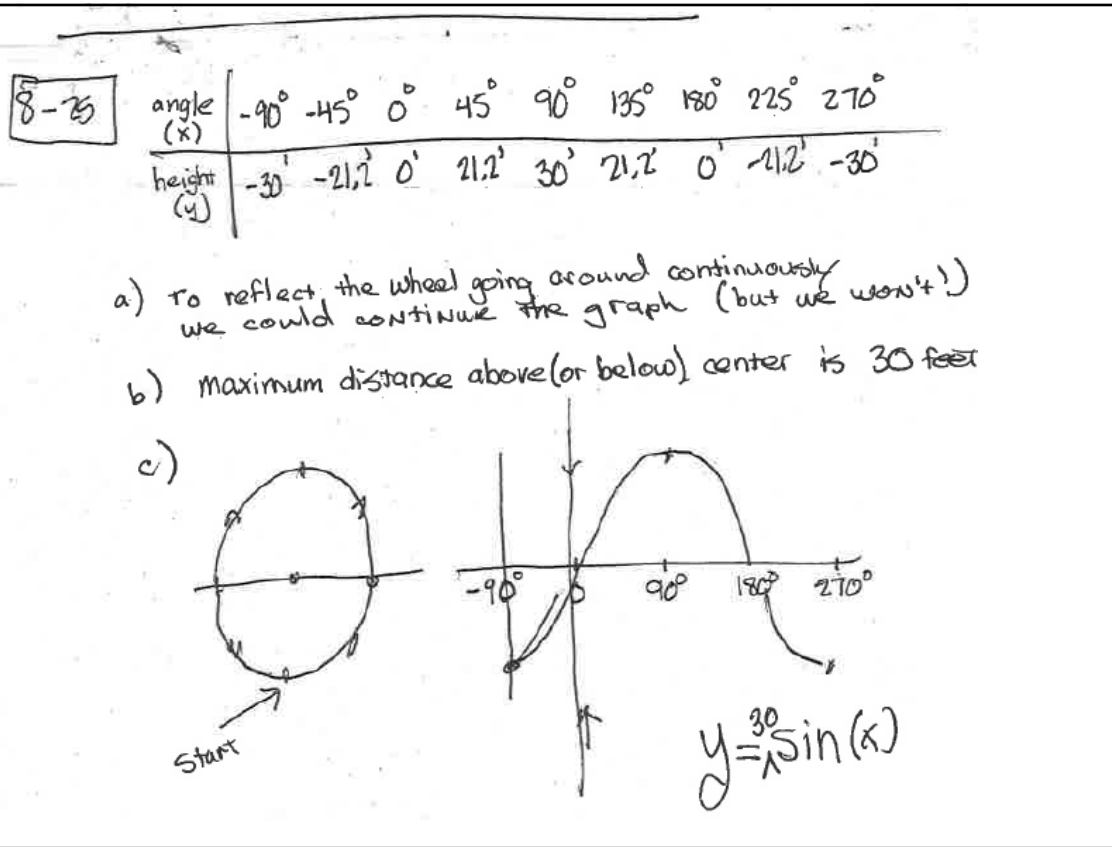
$$y = 3^x$$

a) DOWN 4

$$y = 3^x - 4$$

b) RIGHT 7

$$y = 3^{x-7}$$



Today:

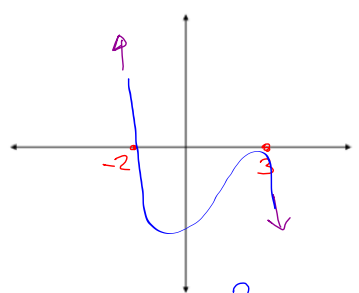
Long Warm Up, short lesson

① **Check your HW**
from yesterday.

② pick up and do the
Warm Up

①

$$f(x) = -(x+2)(x-3)^2$$



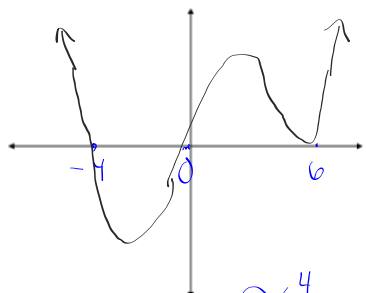
leading term $-x^3$

degree 3 (odd)

orientation (-)

end behavior $\uparrow \downarrow$

$$g(x) = x(x+4)(x-6)^2$$



leading term x^4

degree 4

orientation (+)

end behavior $\uparrow \uparrow$

Previously

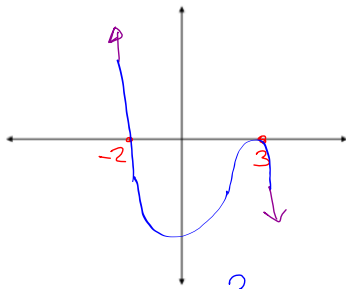
Squared factors
indicate double roots
(creating x-intercepts
that bounce)

Single roots
(create x-intercepts
that cross)

()

①

$$f(x) = -(x+2)(x-3)^2$$



leading term $-x^3$

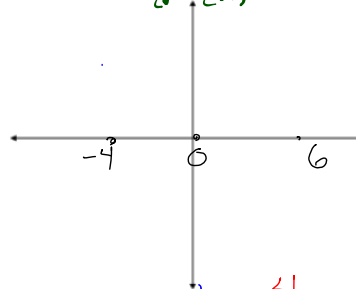
degree 3 (odd)

orientation (-) ↓

end behavior ↑ ↓

$$g(x) = x(x+4)(x-6)^2$$

(cross) bounce



leading term x^4

degree 4

orientation (+) ↓

end behavior ↑ ↑

① $f(x) = -(x+2)(x-3)^2$

leading term $-x^3$

degree 3 (odd)

orientation (-) ↘

end behavior ↗ ↘

$g(x) = x(x+4)(x-6)^2$
(+)(+)(+)

leading term x^4

degree 4

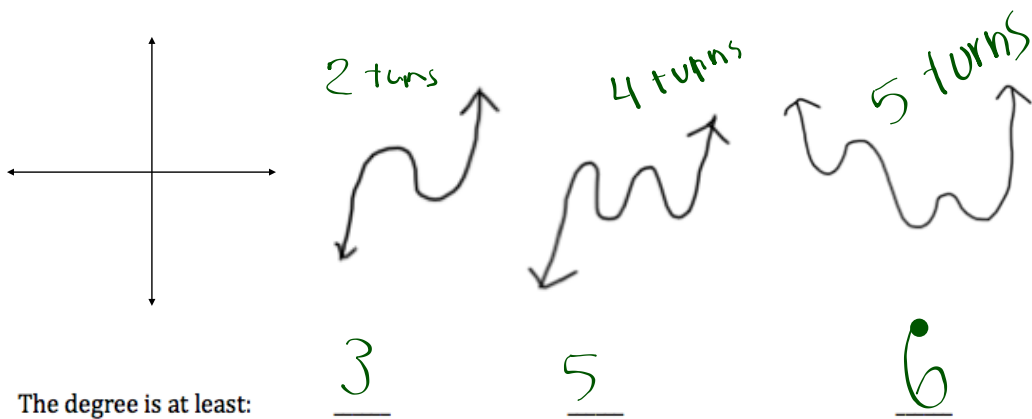
orientation (+) ↘

end behavior ↗ ↗

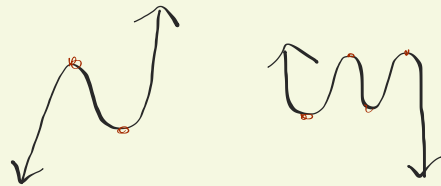
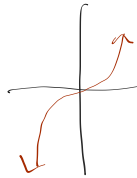
$x^2 - 7x + 18$

x^4

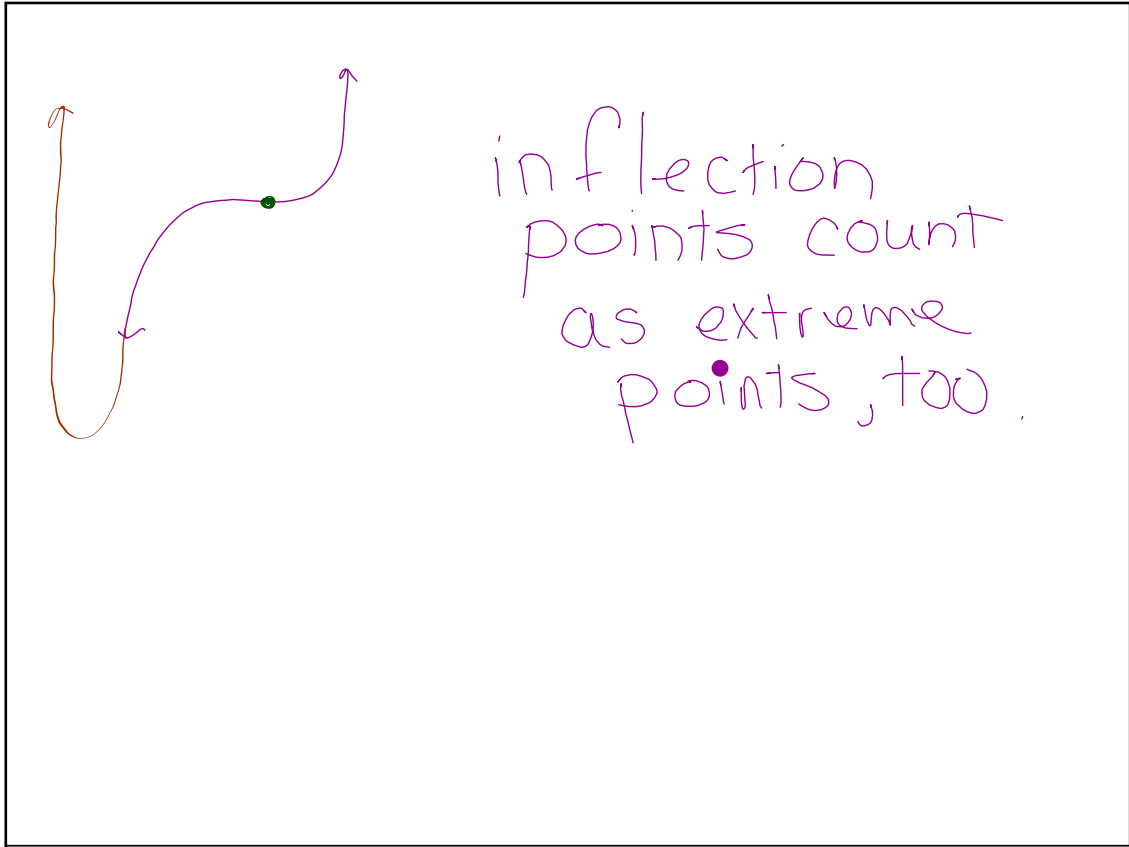
2. Given the graph of 4 functions below, what would be the minimum degree of each function ?



$$y = x^3$$



The minimum degree of a polynomial is equal to the number of turns plus 1



3. Find the exact roots of $f(x) = x^2 + 6x - 8$

$$0 = x^2 + 6x - 8$$

$$a = 1$$

$$b = 6$$

$$c = -8$$

$$x = \frac{-(6) \pm \sqrt{(6)^2 - 4(1)(-8)}}{2(1)}$$

$$x = \frac{-6 \pm \sqrt{68}}{2}$$

$$= \frac{-6 \pm 2\sqrt{17}}{2}$$

$$= \frac{-6}{2} \pm \frac{2\sqrt{17}}{2}$$

$$= -3 \pm \sqrt{17}$$

4
9
16
25
36
49
64

$$x = \frac{-6 \pm \sqrt{68}}{2}$$

but $\sqrt{68} = \sqrt{4\sqrt{17}}$
 $= 2\sqrt{17}$

$$x = \frac{-6 \pm 2\sqrt{17}}{2}$$

$$= -\frac{6}{2} \pm \frac{2\sqrt{17}}{2}$$

$$x = -3 \pm \sqrt{17}$$

The roots are $-3 \pm \sqrt{17}$

4. Predict the roots of $k(x) = x(x+10)(2x-1)$

$$0$$

$$-10$$

$$\frac{1}{2}$$


$$2x - 1 = 0$$

$$2x = 1$$

$$x = \frac{1}{2}$$

5 Could a polynomial with degree 2 not have any real **zeros**? Why?

Yes, because the graph may not cross the x -axis



6. Could a polynomial with degree 5 not have any **real zeros**? Why?

No odd degree graphs must have opposite end behavior so the graphs must cross the x -axis

7. Complete each statement in regards to polynomial, $Q(x)$, that crosses the x -axis at $x = -7$

-7 is a Zero of $Q(x)$

-7 is a root of the equation: $Q(x) = 0$

-7 is an x -intercept of the graph of $Q(x)$.

8. Circle the polynomials:

$$y = 3x^2 + 2x - \sqrt{x}$$

$$f(x) = x^2 - 8x$$

$$g(x) = (x - 2)^3 - 1$$

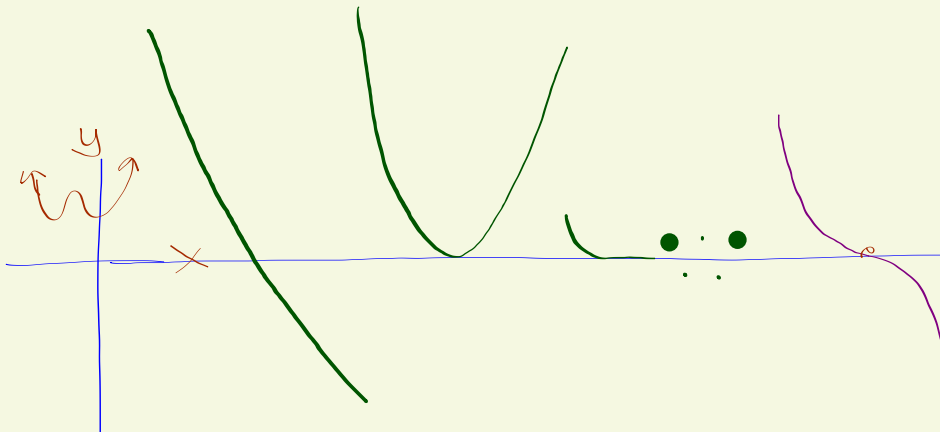
$$y = \frac{1}{x^2} + \frac{3}{x} + 3$$

$$y = 2x + 1$$

$$x^2 + y^2 = 25$$

$$y = -7$$

$$y = (x - 2)^3(x + 10)^2$$



Polynomial Graphs either cross or they "bounce". There is no 3rd option.

Continuation from last class:

Polynomials that have repeated factors

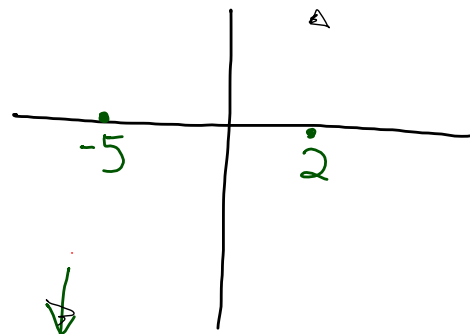
Previously

Squared factors
indicate double roots
(creating x-intercepts
that bounce)

• single roots
(create x-intercepts
that cross)

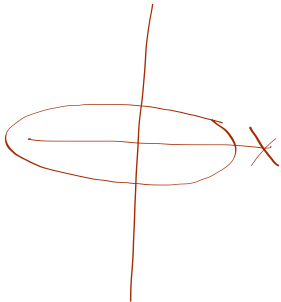
$$P_1(x) = (x-2)(x+5)^2$$

cross at 2 bounce at -5



Triple roots ?

$$y = (x-2)^4(x+5)^3$$



-5

Tobit

factors with odd exponents

$$(x-5)^3, (x+2)^4, (x+8)^5$$

have crossing x-intercepts

factors with even exponents

$$(x-1)^2, (x+2)^4, \text{etc}$$

have x-intercepts that bounce (turn)

~~g23~~

Sketching practice
 (No calculators)
 have your notes handy

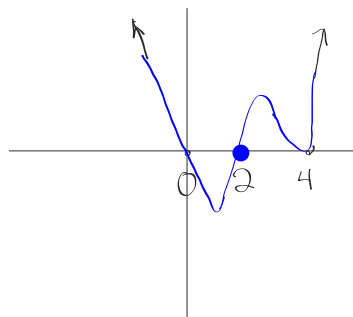
$$y = x^1(x-2)^3(x-4)^2$$

lead term x^6

degree 6

orientation (+)

end behavior $\uparrow \uparrow$

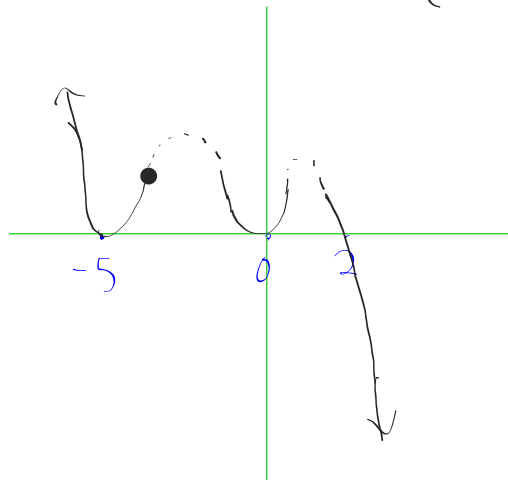


6/

Next

$$f(x) = -x^2(x+5)^4(x-2)^3$$

(3, 4)

 $-x^9$ 

5

5 minutes

- ① Make up a polynomial for your partner to sketch.
- ② Swith papers. Sketch
- ③ Rotate again to check each other's answers

LCQ
on sketching Polynomials
- NOTES OK!
- but No GDC

Assignment

8.....36-40, 44c