

57b

$$x = -\sqrt{5} \quad x = \sqrt{5}$$

determine a polynomial

$$y = (x - \quad)(x - \quad)$$



$$55 \quad b \quad -5x^3 + 10x^2 + 8 \quad x+8$$

$$a_3 = -5 \quad a_2 = 10 \quad a_1 = 0 \quad a_0 = 8$$

$$f \quad y = 10$$

$$a_0 =$$

$$(10) \quad 2^x = 17$$

$$a \quad x \log(2) = \log(17)$$

$$x = \frac{\log(17)}{\log(2)}$$

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$$x^2 + y^2 + 10y = -9$$

is a circle because  
of the  $x^2$  and  $y^2$  term

$$x^2 + y^2 + 10y = -9$$

$\left(\frac{10}{2}\right)^2 = 25$        $25$

Gather like terms

$$x^2 + y^2 + 10y + 25 = 16$$

$$x^2 + (y + 5)^2 = 16$$

center  $(0, -5)$   
radius  $= \sqrt{16} = 4$

$$\sqrt{5-2x} + 7 = 4$$

$$(\sqrt{5-2x})^2 = (-3)^2$$

$$5-2x = 9$$

$$-5 \quad -5$$

$$-2x = 4$$

$$x = -2$$

$60d$   $4^{\log_4(x)} = 7$  Abstract!

Convert to log form  $\rightarrow$  exponent =  $\log_4(7)$

$$\log_4(x) = \log_4(7)$$
$$x = 7$$

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$$f(x) = a_n x^n + (a_{n-1}) x^{n-1} + \dots + (a_1) x^1 + a_0$$

55a

$$6x^4 - 3x^3 + 5x^2 + x + 8$$

coefficients  $a_4$   
 $a_3$   
 $a_2$   
 $a_1$   
 $a_0$

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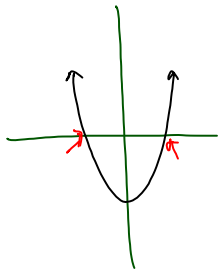
$$x^2 = 2$$

you get  
two solutions

2 x-intercepts  
if graphed

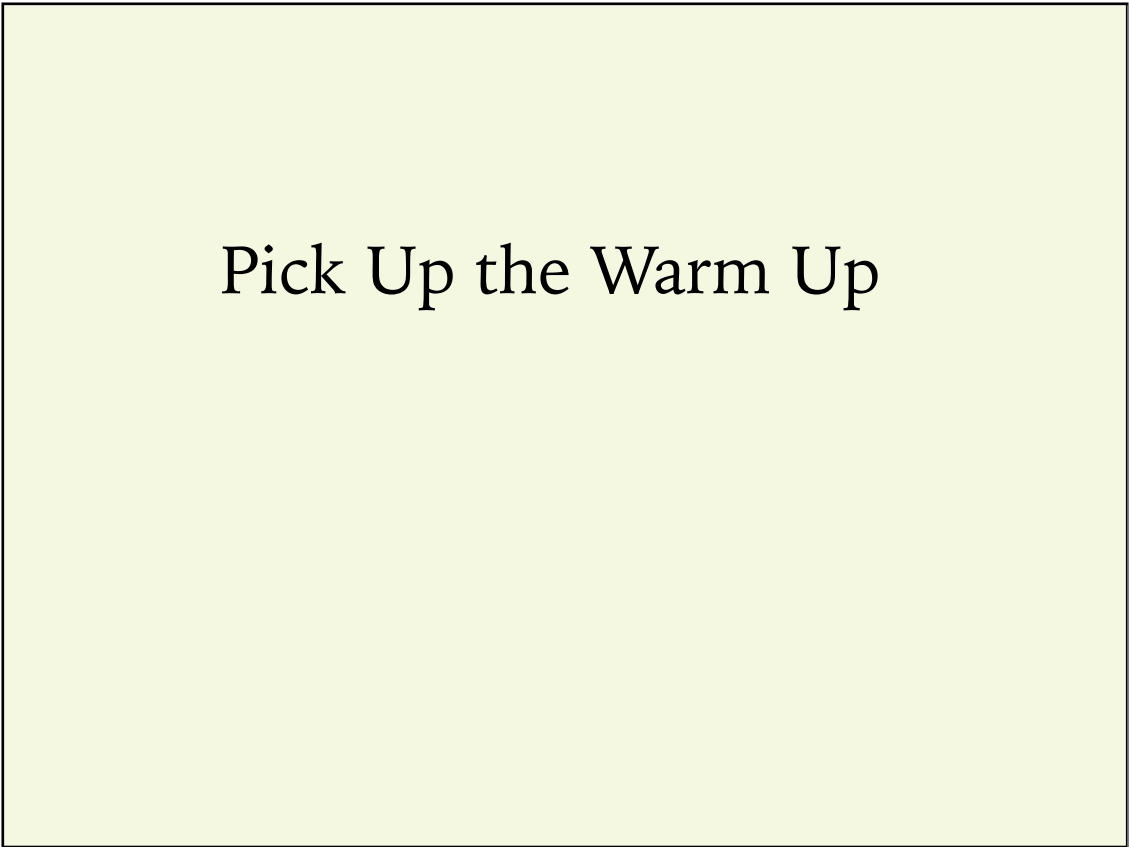
$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \pm\sqrt{2}$$





Pick Up the Warm Up



a. Consider the equation  $x^2 = 2$ . How do you "undo" squaring a number?

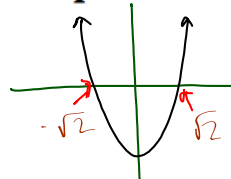
$$x^2 - 2 = 0$$

b. When you solve  $x^2 = 2$ , how many solutions should you get?

You get two solutions

$$x = \pm\sqrt{2}$$

c. How many x-intercepts does the graph of  $y = x^2 - 2$  have?



$$y = x^2 - 2$$

d. Solve the equation  $x^2 = 2$ . Write your solutions both as radicals and as decimal approximations.

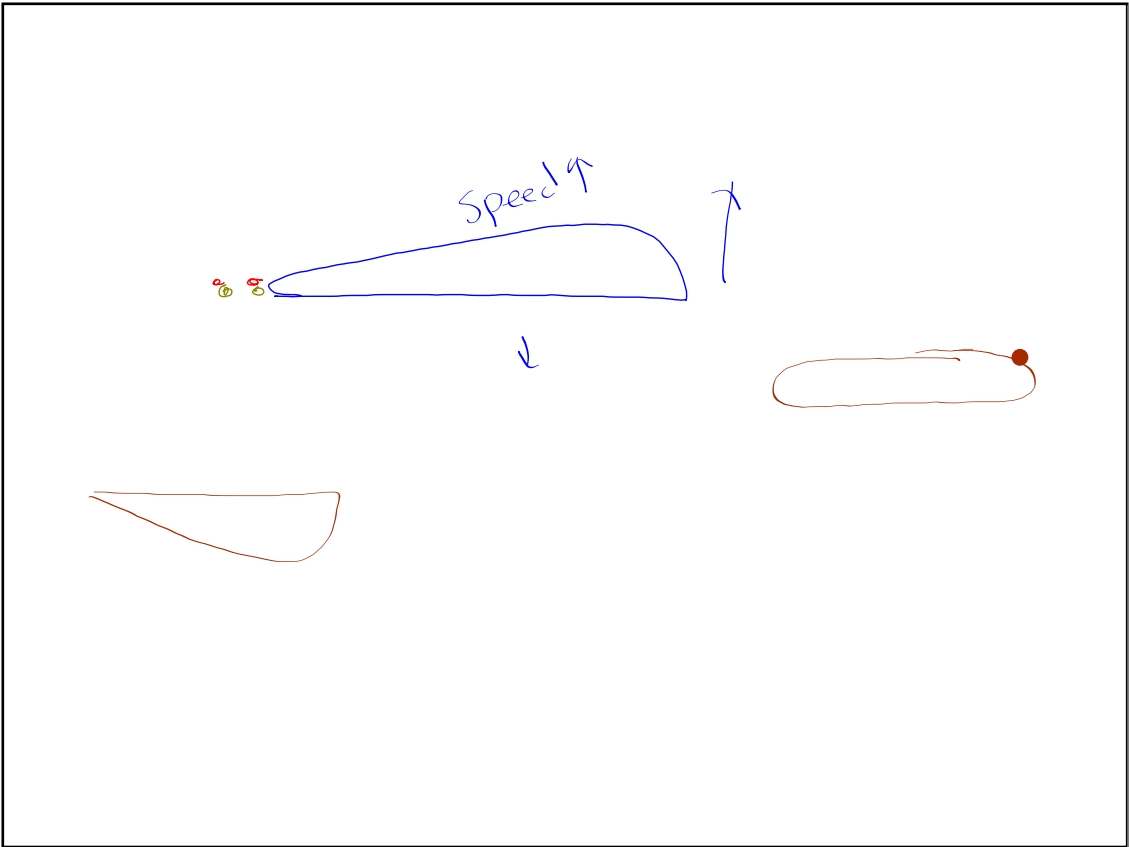
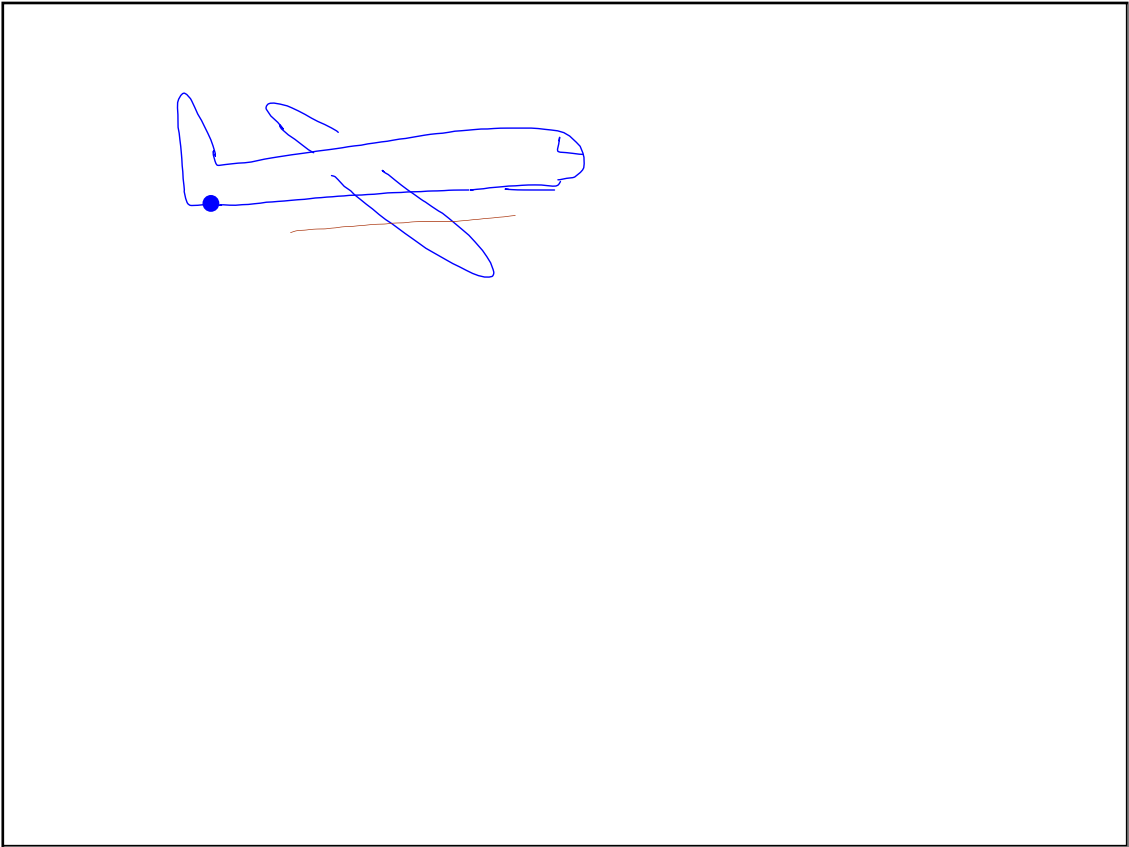
$$x^2 = 2$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \pm\sqrt{2}$$

$$\approx \pm 1.4142$$





NOTES  
on imaginary numbers

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \pm \sqrt{-1} \quad \bullet \text{ impossible}$$

Notes

definition #1

$$\sqrt{-1} = i$$

Solve  $x^2 + 1 = 0$

$$x^2 = -1$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \pm \sqrt{-1}$$

$$x = \pm i$$

$$x = i \text{ or } -i$$

$i$

examples

$$\sqrt{-2}$$

$$\rightarrow i\sqrt{2}$$

$$\sqrt{2} \cdot \sqrt{-1}$$

$$\sqrt{2}i$$

$$\sqrt{-10}$$

$$\rightarrow i\sqrt{10}$$

$$\sqrt{-9}$$

$$\rightarrow i\sqrt{9}$$

$$\rightarrow 3i$$

$$\sqrt{-12}$$

$$\rightarrow i\sqrt{12}$$

$$\rightarrow i\sqrt{4\sqrt{3}}$$

$$\rightarrow 2i\sqrt{3}$$

definition 2

$$i^2 = -1$$

$$i^2 = -1$$

$$i^3 = i^2 \cdot i = -i$$

$$i^4 = i^2 \cdot i^2 = -1 \cdot -1 = 1$$

$$i^5 = i^4 \cdot i^1 = i$$

$$i^6 = i^4 \cdot i^2 = -1$$

$$i^7 = i^4 \cdot i^3 = i^4 \cdot i^2 \cdot i = -i$$

$$i^8 = i^4 \cdot i^4 = 1$$

$$i^{11} = \cancel{i^4 \cdot i^4} \cdot i^3 = i^2 \cdot i = -i$$

$$i^1 =$$

$$i^2 =$$

$$i^3 =$$

$$i^4 =$$

$$i^5 =$$

$$i^{10} =$$

$$i^{16} =$$

$\sqrt{-25}$	$(4i)(4i)$	$(2i)(3i)$	$(2i)(-5i)$
↓		↓	$4i^2 \cdot -5i$
$i\sqrt{25}$	$16i^2$	$6i^2$	$4(-1) \cdot -5i$
↓	↓		$(20i)$
$(5i)$	$(-16)$	$(-6)$	
			$x^2 - 7x + 16 = 0$

$5i(2i-3)$	$\frac{6 \pm \sqrt{-8}}{2}$	$i\sqrt{8}$
$10i^2 - 15i$		$i\sqrt{4}\sqrt{2}$
$-10 - 15i$	$\frac{6 \pm 2i\sqrt{2}}{2}$	$2\sqrt{2}$
$-15i - 10$	$3 \pm i\sqrt{2}$	
<		

## Complex Numbers •••

$$a + bi$$

↑  
 real part

~~~~~  
 • imaginary part

$$7 \pm 3i$$

$$\sqrt{2} \pm 5i$$

$$4 \pm i\sqrt{6}$$

$$\pm 6i$$

## HAPPY FACE

$$(5+i)(5+i)$$

$$(\sqrt{7}+i)(\sqrt{7}-i)$$

$$(5+i)(5+i)$$

$$25 + i^2 + 10i$$

$$24 + 10i$$

$a + bi$

## Conjugates

$$(4 + i)(4 - i)$$

$$16 - i^2$$

$$16 - (-1)$$

$$\boxed{17}$$

$$(-6 + 3i)(-6 - 3i)$$

$$36 - 9i^2$$

$$36 + 9$$

$$\boxed{45}$$

GDC

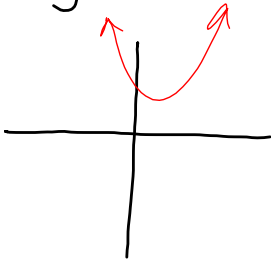
$$2i(\sqrt{7} - 6)$$

Some equations  
have imaginary  
solutions

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page 391

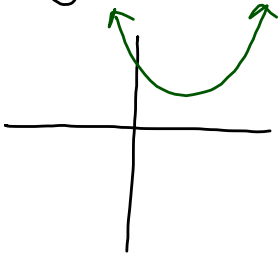


(a)  $y = x^2 - 4x + 5$



$x^2 - 4x + 5 = 0$   
 should not have  
 real solutions

(a)  $y = x^2 - 4x + 5$



$x^2 - 4x + 5 = 0$   
 should not have  
 real solutions

(b) Quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(5)}}{2(1)}$$

$$\begin{aligned} a &= 1 \\ b &= -4 \\ c &= 5 \end{aligned}$$

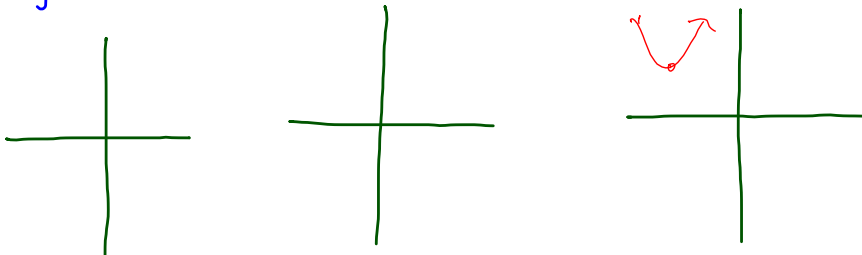
$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(5)}}{2(1)} =$$

BB

$$8-67$$

the vocabulary of the question is important.

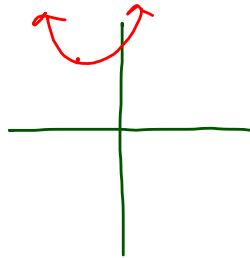
a  $y = (x+3)^2 - 4$     b  $y = (x+3)^2$     c  $y = (x+3)^2 + 4$



#  
roots

roots  
are

$$\textcircled{c} \quad y = (x+3)^2 + 4 \qquad (x+3)^2 + 4 = 0$$



imaginary  
roots

## Assignment

8.....Read the Math Notes on page 392

.....70 to 78

Yes, many of the assignments have been long. The practice is important for your mastery as well as success on the Final Exam.