


Check your  
solutions to  
yesterday's  
HW.

then

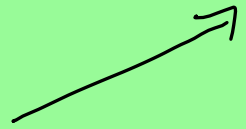


HW  
Help



# HW Questions

check  
# 36



8-36

where does  $y = (x+3)^2 - 5$  cross  $x$ -axis?  $\rightarrow$  set  $y=0$ 

$$(x+3)^2 - 5 = 0$$

$$(x+3)^2 = 5$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x+3 = \pm\sqrt{5}$$

$$x = -3 \pm \sqrt{5}$$

 $(-3+\sqrt{5}, 0)$  and  $(-3-\sqrt{5}, 0)$

8-37

Use  
Zero Prod  
Prop

$$f(x) = (x - 74)^2(x + 29)$$

would inter

$$(x - 74)^2(x + 29) = 0$$

$$\downarrow$$

$$x - 74 = 0$$

$$\downarrow$$

$$x + 29 = 0$$

$$x = 74$$

$$x = -29$$

↗  
bounced

At  
at

8-38

(a)  $(-3, 0) (2, 0) \Rightarrow y = (x+3)(x-2)$

$$y = x^2 - 2x + 3x - 6$$

$y = x^2 + x - 6$  ← 1 possible answer

$$(b) \quad (-3, 0) \quad \left(\frac{1}{2}, 0\right) \Rightarrow y = (x+3)\left(x-\frac{1}{2}\right)$$
$$y = x^2 - \frac{1}{2}x + 3x - \frac{3}{2}$$
$$y = x^2 + \frac{5}{2}x - \frac{3}{2}$$

could also introduce  
stretch factor of  
2 to get

$$y = 2x^2 + 5x - 3$$

8-39

a)  $P(x) = 208x^2 + 15x$  degree 2

b)  $y = 8x^2 - \frac{1}{7}x^5 + 9$  degree 5

c)  $f(x) = 5(x+3)(x-2)(x+7)$  degree 3

d)  $y = (x-3)^2(x+1)(x^3+1)$  degree 6

5x3

8-40

- a) Parabolas are written as  $y = ax^2$  (Polynomial)
- b) Exponentials,  $y = 2^x$ , for example (NOT)
- c) cubics  $y = 2x^3$  (Polynomial - can be written in form  $y = ax^n$ )
- d) Lines  $y = 3x + 2$  (Polynomial) →
- e) circles (NOT)

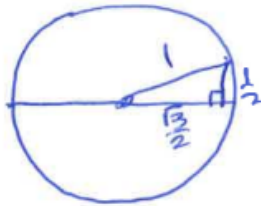


8-44c

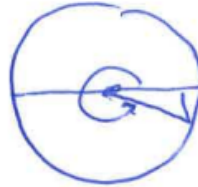
Find all solutions in interval  $0^\circ \leq \theta \leq 360^\circ$ 

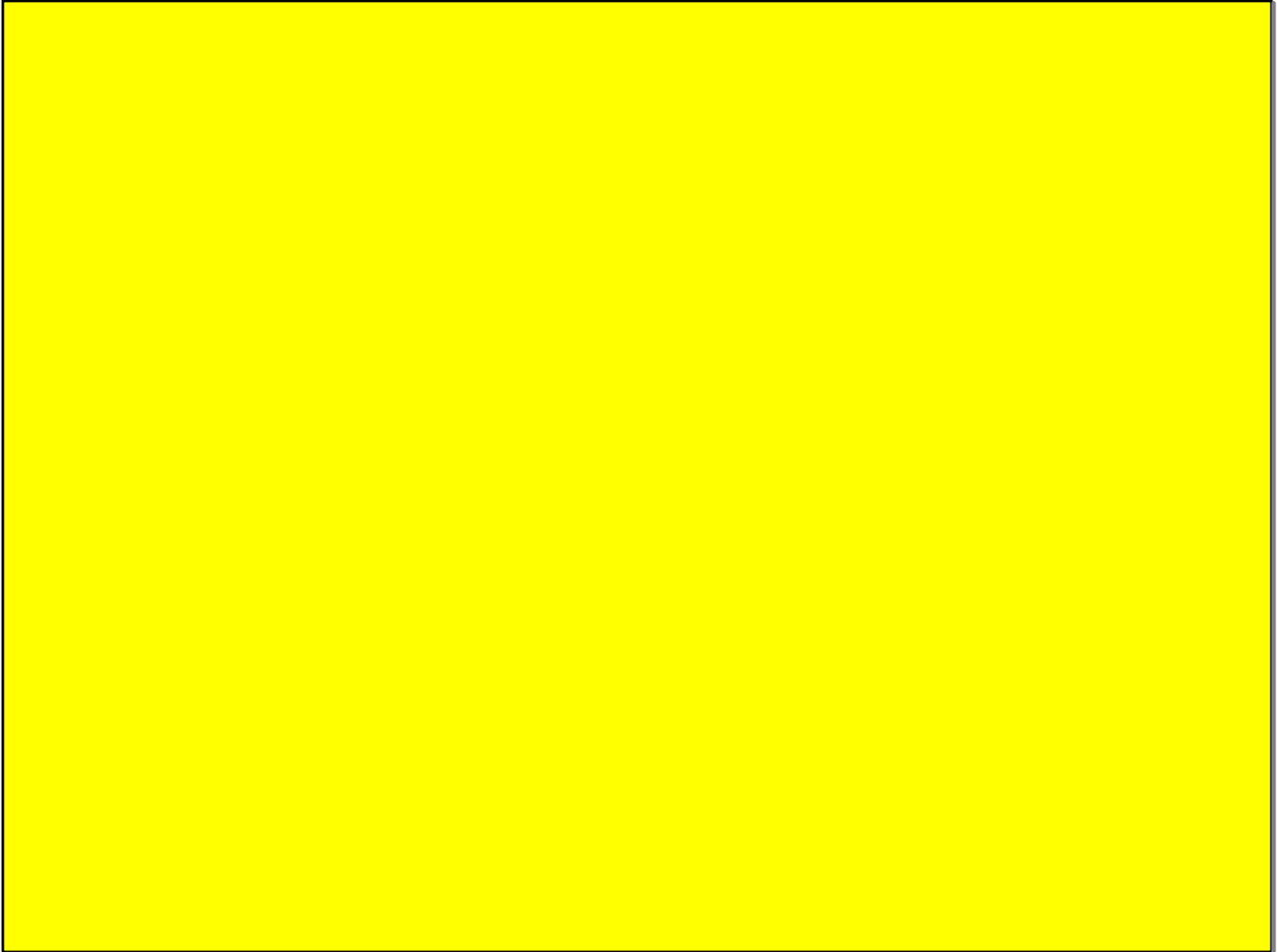
$$\cos \theta = \frac{\sqrt{3}}{2}$$

↙ Positive so to the right



or

So  $30^\circ$  and  $330^\circ$



If

you were asked to write  
an equation of a polynomial  
in standard form and you were  
given two x-intercepts  
(5, 0) (-8, 0)

How would you begin?

$$y = (x - 5)(x + 8)$$

Pick up the  
warm up

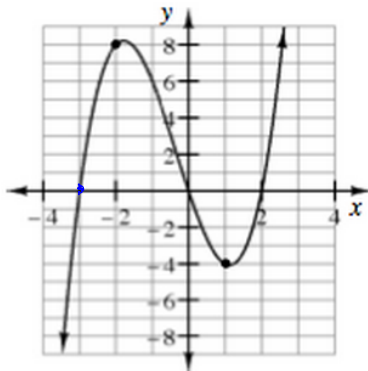
do #1 only

## Warm Up

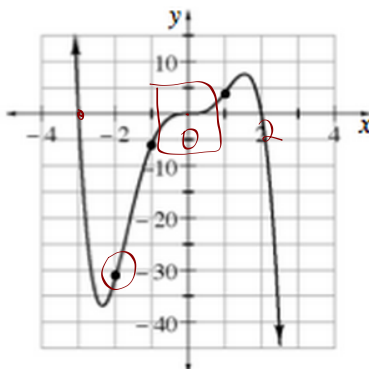


Find reasonable equations for each of the following polynomial functions.

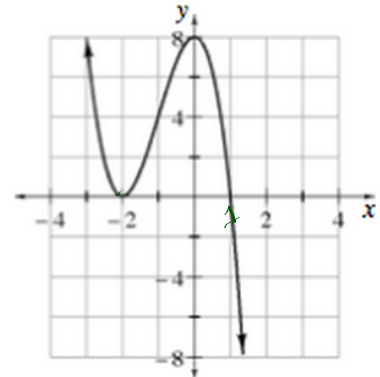
a.



b.



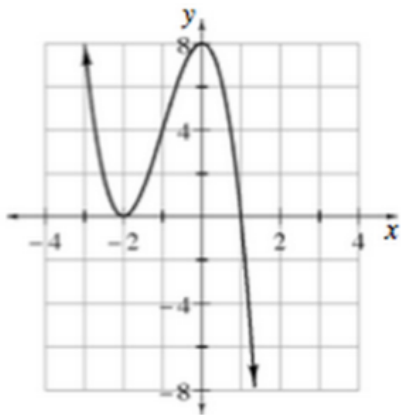
c.



$$y = (x+3)x(x-2) \quad y = a(x+3)x^3(x-2) \quad y = a(x+2)^2(x-1)$$

Without using a graphing calculator, how can you check the accuracy of your equations? Were each of your equations accurate? If not, why do you think your equation(s) were not accurate?

c.



Now calculate  
the  $y$ -intercept

$$y = -1(x+2)^2(x-1)$$

$\uparrow$   
0
 $\uparrow$   
0

$$y = -(2)^2(-1)$$

$$y = -4(-1)$$

$$y = 4$$

today

Create polynomial equations that  
represent all points on the graphs  
(not just the  $x$ -intercepts)

back side  
of warm  
up

**To be used later in class**

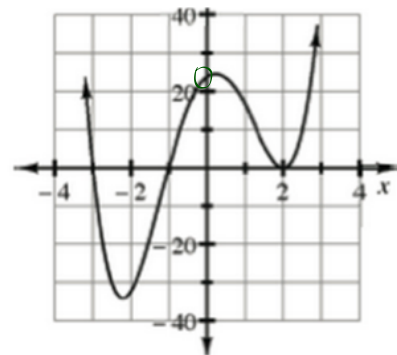
Suppose the person next to you wrote the equation

$$y = \frac{(x+3)(x+1)(x-2)^2}{\quad}$$

to represent the graph at right.

1. Explain how you can decide how well the equation represents the graph. What can you do to the equation to make it a *better fit* for the graph? What equation would fit better?

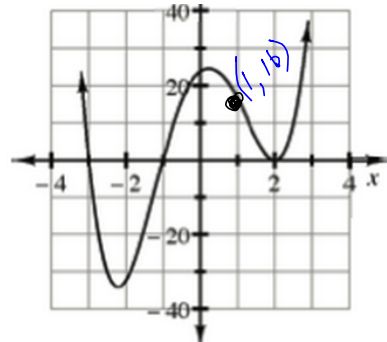
ARE THE INTERCEPTS ENOUGH?



GDC

pick a point on the graph  $(x,y)$   
and plug it in.





2. Before you figured it out, you could have written the polynomial

for this graph as  $P(x) = a(x+3)(x+1)(x-2)^2$ . What if you did not have a graphing calculator, but you were told that the graph goes through the point  $(1, 16)$ ? How could you use that information to determine the exact equation? Once you have decided on a method with your team, try it. How can you test the accuracy of your equation?

$$y = a(x+3)(x+1)(x-2)^2$$

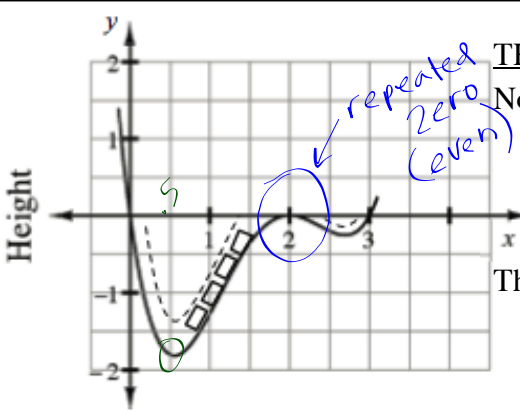
$$16 = a(1+3)(1+1)(1-2)^2$$

$$16 = a(4)(2)(1)$$

$$16 = 8a$$

$$\boxed{a = 2}$$

$$f = a(x+3)(x+1)(x-2)^2 \quad (1, 16)$$



**THE COUNTY FAIR COASTER RIDE**

Now that you have more expertise with polynomial equations and their graphs, the Mathamericaland Carnival Company has hired your team to find the *exact* equation to represent its roller-coaster track.

The numbers along the x-axis are in hundreds of feet. At 250 feet, the track will be 20 feet below the surface. This gives the point (2.5, -0.2).

1. What degree polynomial represents the portion of the roller coaster represented by the graph at right? 4
2. What are the roots?  $x = 2, 3, 0$
3. Find an exact equation for the polynomial that will generate the curve of the track.

$$y = a(x-2)^2(x-3)(x)$$

$$-.2 = a(2.5-2)^2(2.5-3)(2.5)$$

$$-.2 = a(.5)^2(-.5)(2.5) \Rightarrow -.2 = -.3125a$$

4. What is the deepest point of the roller coaster's tunnel?

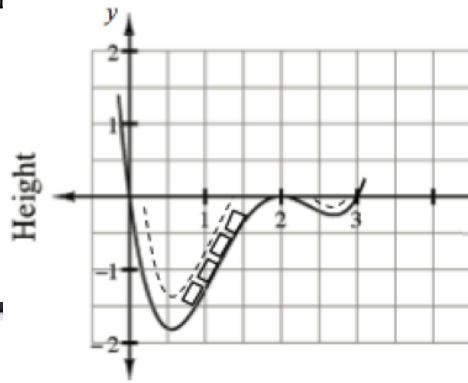
$$a = .64$$

$$y = .64(x-2)^2(x-3)(x)$$

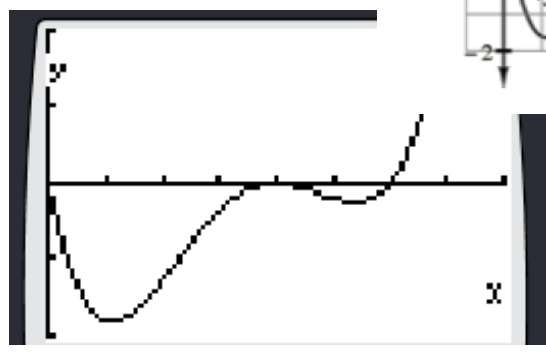
plug in  $x = .5$

4. What is the deepest point of the roller coaster's tunnel?

```
Plot1 Plot2 Plot3
Y1=.64X(X-2)²(X-3)
Y2=
```



```
WINDOW
Xmin=
Xmax=4
Xscl=.5
Ymin=-2
Ymax=2
Yscl=1
Xres=1
```



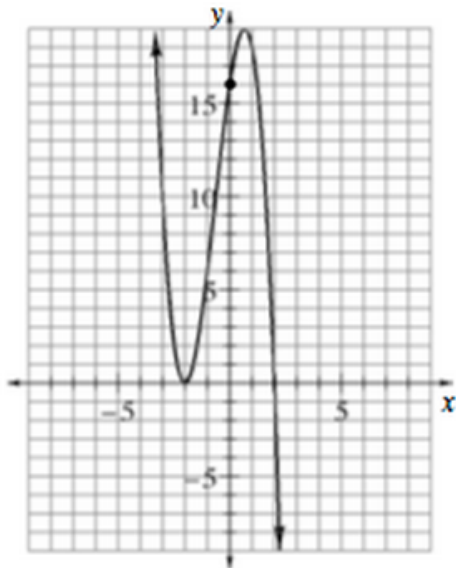
Minimum  
 $X=.55699756$   $Y=-1.81339$

*≈ 181 feet below ground*

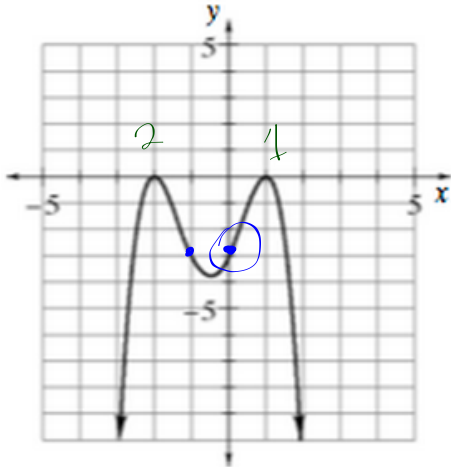
8-49b

be prepared to show your  
process on the doc cam.

a.



b.

 $(0, -3)$ 

$$y = a(x+2)^2(x-1)^2$$

$$-3 = a(0+2)^2(0-1)^2$$

$$a = -\frac{3}{4}$$





do the following questions  
in your notes

50  $\rightsquigarrow$  51  $\rightsquigarrow$  53

$8-50$ bounce at  
 $(-1, 0)$ crosses  
at  $(4, 0)$ through  
 $(-2, -18)$ Likely  
answer  
by many

$$y = 3(x+1)^2(x-4)$$

8-51

Armando  $y = 3(x+1)^4(x-4)$

Does it work ?

Check Additional  
Point

$$(-2, -18)$$

$$-18 = 3(-2+1)^4(-2-4)$$

$$-18 = 3(-1)^4(-6)$$

$$-18 = -18$$

yes

8-52 New additional point (1, -36)

Original

$$y = 3(x+1)^2(x-4)$$

$$-36 = 3(1+1)^2(1-4)$$

$$-36 = 3(2)^2(-3)$$

$$-36 = -36$$

Armando's

$$y = 3(x+1)^4(x-4)$$

$$= 3(1+1)^4(1-4)$$

$$= 3(2)^4(-3)$$

$$-36 \neq$$

•

You have to know how many times a factor is used (is repeated),

OR

↑ by knowing the degree of the polynomial

you need an additional point to check.

**8....54-58, 59b, 60,62**

$$a_1 =$$

$$a_0 =$$

55a

coefficients  $a_4$   
 $a_3$   
 $a_2$   
 $a_1$   
 $a_0$