

In your Notes: Write down

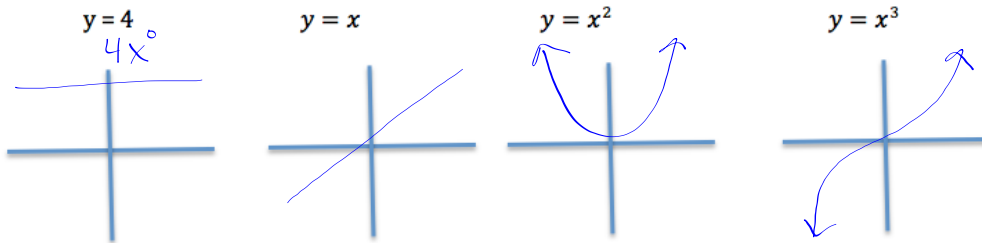
① **Ch 8 - Polynomials**

② **Check your HW with the solutions**

record your score on the  
old Recording Sheet •  
(pink)

③ Then pick up the  
**Warm Up**

2. Sketch the following parent functions (hopefully by recognition, not by using your GDC)



**These are all polynomials with different degrees**

## Notation for Polynomials

The **general equation** of a **second-degree** (quadratic) polynomial is often written in the form  $f(x) = ax^2 + bx + c$ , and the general equation of a **third-degree (cubic) polynomial** is often written in the form  $f(x) = ax^3 + bx^2 + cx + d$ .

For a polynomial with an undetermined degree  $n$ , it is unknown how many letters will be needed for the coefficients. Instead of using  $a, b, c, d, e$ , etc., mathematicians use only the letter  **$a$** , and they use **subscripts**, as shown below.

$$f(x) = (a_n)x^n + (a_{n-1})x^{(n-1)} + \dots + (a_1)x^1 + a_0$$

This general polynomial has degree  $n$  and coefficients  $a_n, a_{n-1}, \dots, a_1, a_0$ .

For example, for  $7x^4 - 5x^3 + 3x^2 + 7x + 8$ , the degree is 4. In this specific case,  $a_n$  is  $a_4$  and  $a_4 = 7$ ,  $a_{n-1}$  is  $a_3 = -5$ ,  $a_{n-2}$  is  $a_2 = 3$ ,  $a_1 = 7$ , and  $a_0 = 8$ .

For each of the following polynomial expressions, find the degree, list all coefficients, and then label them  $a_0$  through  $a_n$ .

$$f(x) = 2x^4 + 5x^2 - 3x + 9 \quad \text{degree } 4$$

*(Handwritten:  $a_n$  above  $2x^4$ ,  $a_0$  above  $9$ , and an arrow pointing from  $0x^3$  to the missing term)*

$$a_4 = 2$$

$$a_3 = 0 \quad a_2 = 5 \quad a_1 = -3 \quad a_0 = 9$$

$$f(x) = x^3 + 10x^2 \quad \text{degree } 3$$

$$a_3 = 1 \quad a_2 = 10 \quad a_1 = 0 \quad a_0 = 0$$

Multi-variable  
term

$$6x^3y^4$$

$$6x^3x^4$$

Polynomial

Not a Polynomial

$$x^1$$

$$8x^0$$

Hw  
checking

2. For each function below, state if it is a polynomial. IF the answer is "yes", fill out the remaining columns *The first is done for you.*

	<u>Polynomial?</u>	<u>Standard. Form</u>	<u>Leading Coefficient</u>	<u>Degree</u>	<u>Name based on degree</u>	<u>Name based on # terms</u>
$P(x) = x^3 - 5x^4 + 7$						

$$Q(x) = -4x^2 + 6x^5$$

$$R(x) = x - 4x^3 + 4 + 3x^2$$

$$T(x) = (2x + 1)(x - 5)$$

$$F(x) = 40x$$

3. The left side of the following equation is a polynomial. Polynomial equation  
The polynomial happens to be in factored form rather than standard form  
and find all of the solutions:

$$x(2x + 1)(3x - 5) = 0$$

4. Factor the following quadratic polynomial ... (into two factors)  ~~$n^2 - 20n + 3$~~

$$18n^2 - 15n + 2$$

	$6n$	$-1$
$3n$	$18n^2$	$-3n$
$-2$	$-12n$	$2$

~~$$\begin{array}{r}
 36n^2 \\
 -3n \quad -12n \\
 -15n
 \end{array}$$~~

$$(6n - 1)(3n - 2)$$

5. **Simplify** the following polynomials. (simplify normally means eliminate all parentheses and put into "standard" form.)

$$(2x + 1)(10x^3 - x^2 + 3x - 7) \text{ some people like to use a box to keep things organized}$$

Handwritten multiplication of  $(2x + 1)(10x^3 - x^2 + 3x - 7)$ . Blue arrows show the distribution of  $2x$  to each term in the second polynomial, and red arrows show the distribution of  $1$  to each term. The result is written as  $20x^4 - 2x^3 + 6x^2 - 14x + 10x^3 - x^2 + 3x - 7$ .

$$20x^4 - 2x^3 + 6x^2 - 14x + 10x^3 - x^2 + 3x - 7$$

$$\downarrow$$

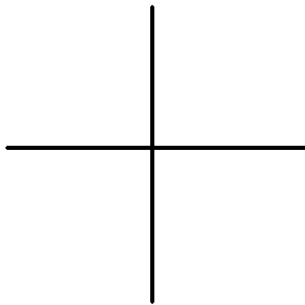
$$20x^4 + 8x^3 + 5x^2 - 11x - 7$$

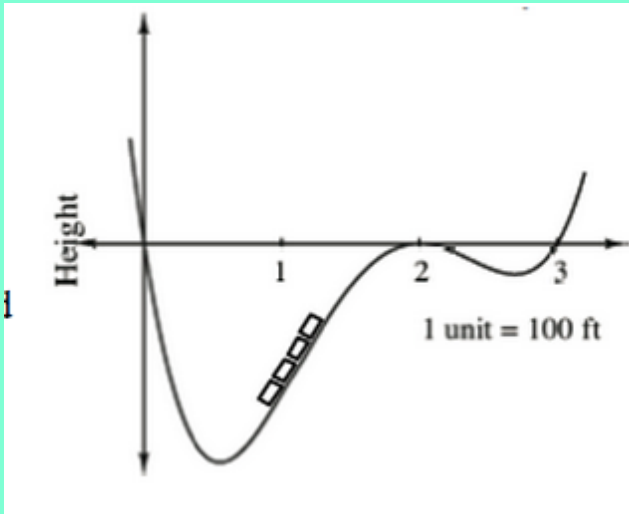
6. **Now it is GDC time.** Graph the polynomial,  $P_1(x) = (x - 2)(x - 5)^2$ . Without simplifying it, can you tell what family it belongs to? \_\_\_\_\_

a) Sketch it

b) Label all x-intercepts on your sketch

c) How are the x-intercepts related to the given function?



 $y =$ 

Quickly check  
your HW



Aim

# Notes

"big and small"

details

of polynomial functions



**Polynomial**  
bare bones

$$\boxed{\begin{array}{l} \text{Any} \\ \text{Number} \end{array} \cdot \overset{\text{Whole}}{\text{Number}} x}$$

Polynomial

Not a Polynomial

$$-3x^7$$

100

$$5x^3$$

$$\frac{3}{2}x^2$$

$$\sqrt{13}x^8$$

$$\sqrt[3]{x}$$

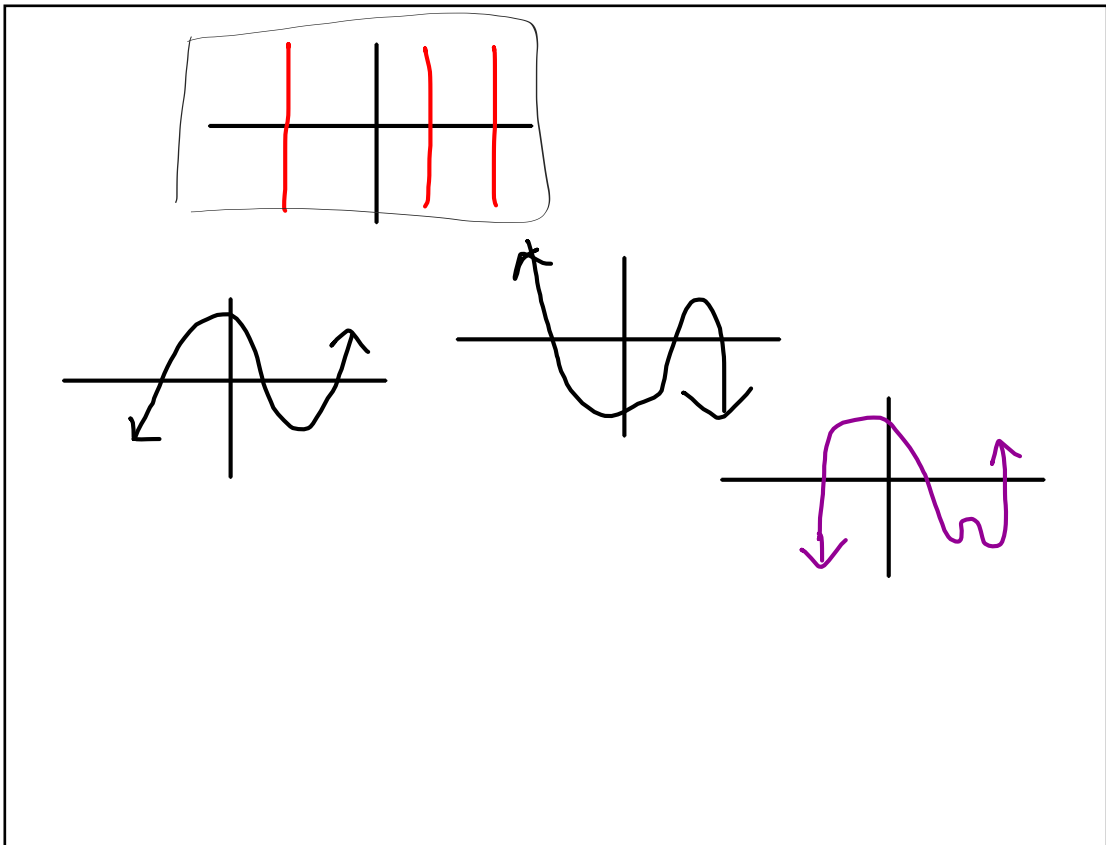
$$\frac{4}{x^2} = 4x^{-2}$$

Polynomials are made up of one or more monomials.

monomials:  $\text{number} \cdot \overset{\text{exponent}}{\text{variable}}$

polynomial:  $3x^{40} + 7x^{12}$

Polynomial Graphs  
can be complex



Therefore.....

it helps to know  
the Big Picture before  
you graph

Predict the degree

$$Q(x) = \frac{(x^2 - 6x + 5)(x + 10)}{(x - 1)(x - 5)(x + 10)} \quad \begin{array}{cc} \text{parent} & \text{degree} \\ \hline x^3 & 3 \end{array}$$

$$G(x) = \frac{x(x+3)^2(x+1)}{x \cdot x^2 \cdot x} \quad \begin{array}{cc} x^4 & 4 \end{array}$$

$$P(x) = (x+2)(x+3)(x+4)^5 \quad 1x^7 \quad 7$$

$$P(x) = (x+2)(x+3)(x+4)^5 \quad -4x^7 \quad 7$$

-4

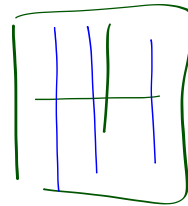
from  
last night's  
Hw

$$P_1(x) = (x - 2)(x + 5)^2$$

What is the  
parent ?

$x^3$

predicted  
shape ?



Predict the degree

$$P(x) = 3(x+2)(x+3)^2(x+4)^5$$

Leading term :  $3x^8$

degree : 8

leading  
coefficient 3

Chapter 8 is very graphing calculator intensive.....

Your GDC will help you learn some things.....

so, eventually, you won't need it for those same things later.

So, lets learn about a potential tool on the GDC

graph  $y = x^2 - 3x + 2.2$

ZOOM-IN

ZOOM-BOX

~~ZOOM-FIT~~

$P_2$

No GDC

$P_1$   $P_2$   $P_3$

$$P_2(x) = 2(x-2)(x+2)(x-3) \quad 2x^3$$

How many  
distinct  
factors?

4

How many x-intercepts  
you predict? 3

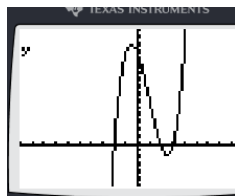
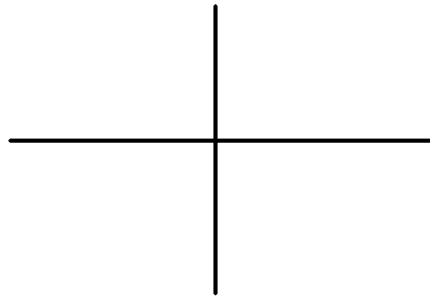
What is the  
degree? 3

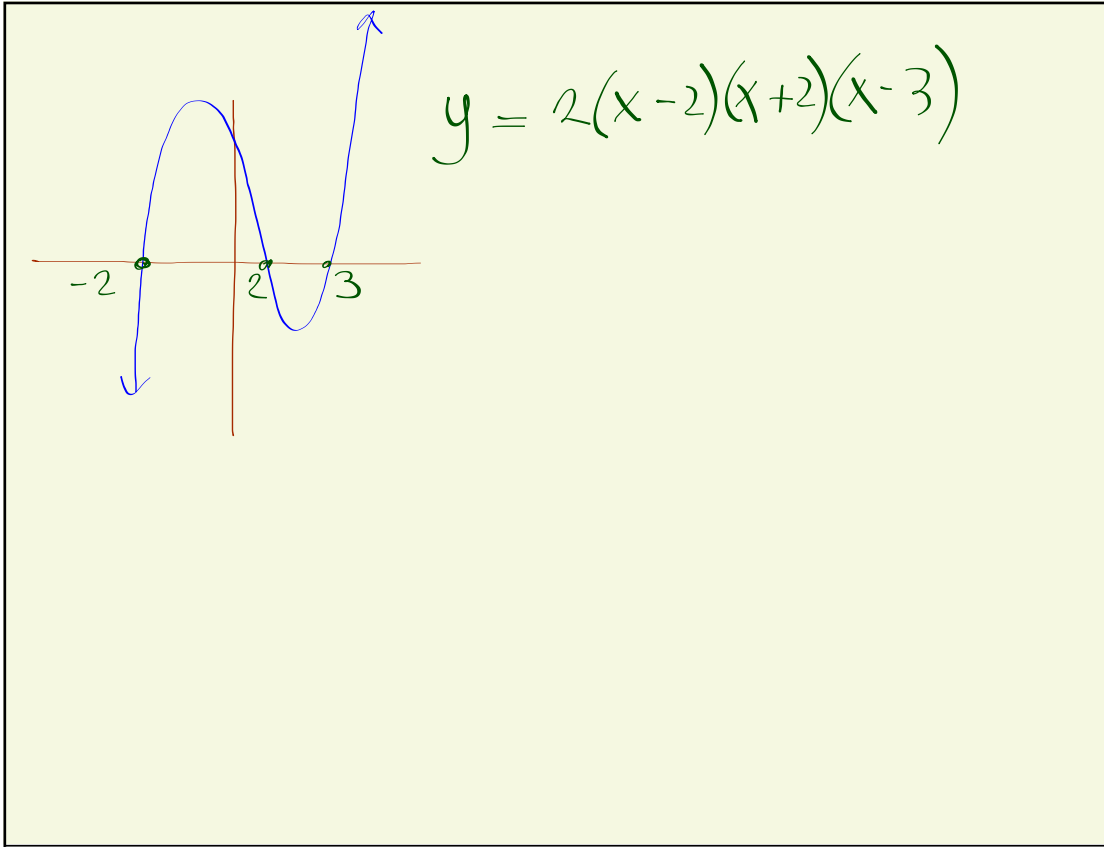
What would the  
leading coefficient  
be? 2

leading  
term?  $2x^3$

$$P_2(x) = 2(x-2)(x+2)(x-3)$$

Now graph  
and sketch  
it





$$P_2(x) = 2(x-2)(x+2)(x-3)$$

Did the factor  $2$  have an effect on the x-intercepts ?

have an effect on the y-intercept ?



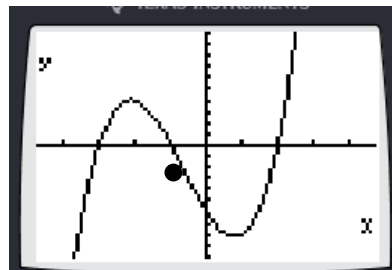
## The leading coefficient of polynomials:

- Affect the y-intercepts
- but do not change the x-intercepts of functions.

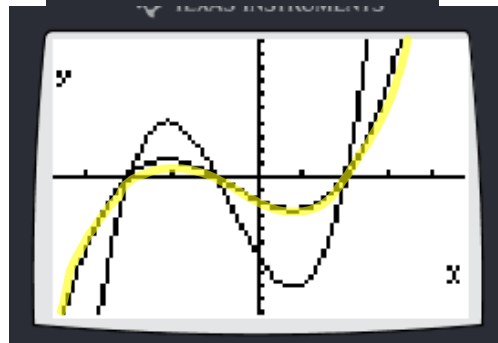
•

example

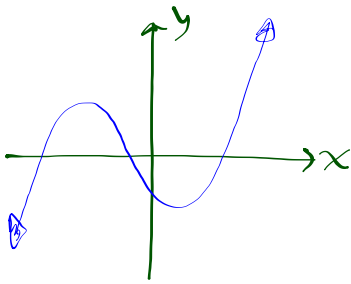
$$y = (x-2)(x+3)(x+1)$$



$$y = \frac{1}{3}(x-2)(x+3)(x+1)$$



## Describing End Behavior



↑  
Sketch

Left As  $x \rightarrow -\infty$ ,  $y \rightarrow -\infty$

Right As  $x \rightarrow \infty$ ,  $y \rightarrow +\infty$

↓ ↑

$$P_3(x)$$

$$P_1(x) = (x - 2)(x + 5)^2$$

$$P_2(x) = 2(x - 2)(x + 2)(x - 3)$$

$$P_3(x) = x^4 - 21x^2 + 20x$$

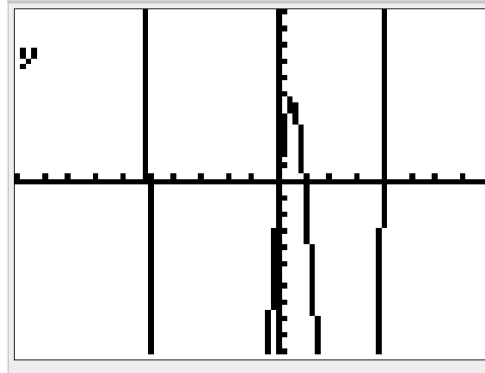
What is different about...

What  $x$ -intercepts can you determine before graphing?  $x =$

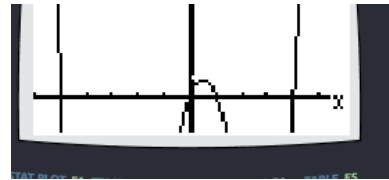
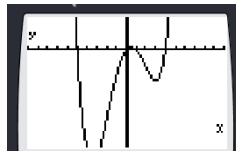
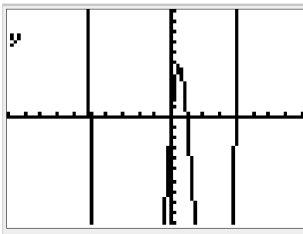
→ sketch function

$$P_3(x) = x^4 - 21x^2 + 20x$$

- a) Leading term
- b) Lead. coeff
- c) Degree
- d) Make a large neat sketch.
- e) Label  $x$ -intercepts
- f) Label  $y$ -intercept
- g) # turns
- h) end behavior

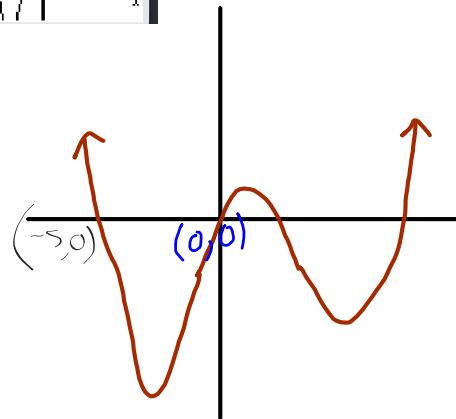


$$P_3(x) = x^4 - 21x^2 + 20x$$



d)

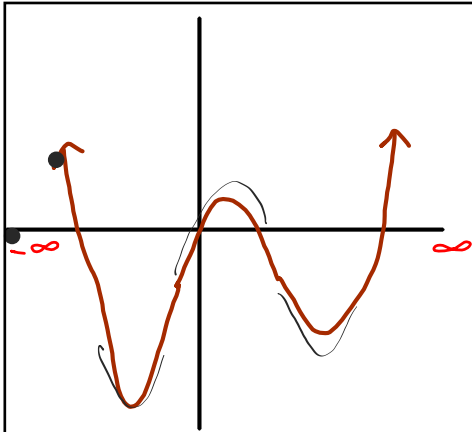
Appropriate  
sketch  
for notes



$$P_3(x) = x^4 - 21x^2 + 20x$$

- a) Leading term  $x^4$   
b) Lead. coeff 1  
c) Degree 4

d)  $x$ -intercepts



Make a large neat sketch.  
Label x-intercepts

f) Label y-intercept

g) # turns 3

h) end behavior

Left: As  $x \rightarrow -\infty$ ,  $y \rightarrow +\infty$

Right: As  $x \rightarrow \infty$ ,  $y \rightarrow \infty$

now  
P  
4

sketch

$P_4$

- a) Leading term
- b) Lead. coeff
- c) Degree
- d) Make a large neat sketch
- e) Label x-intercepts
- f) Label y-intercept
- g) # turns
- h) end behavior

sketch

$P_4$

$$= (x+3)^2(x+1)(x-1)(x-5)$$

- a) Leading term
- b) Lead. coeff
- c) Degree
- d) Make a large neat sketch
- e) Label x-intercepts
- f) Label y-intercept
- g) # turns
- h) end behavior

# Part 1 of: Assignment

on page 372 there are 8  
functions.

~~$P_1$~~   ~~$P_2$~~   ~~$P_3$~~   $P_4$

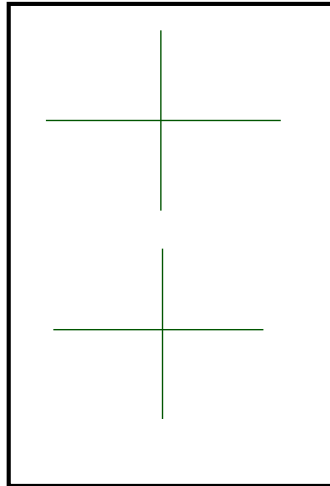
$P_5$   $P_6$   $P_7$   $P_8$



Each person in your group  
will Analyze  $\mathcal{Q}$  of

$P_5$   $P_6$   $P_7$   $P_8$

↑  
At least one has to  
be  $P_6$

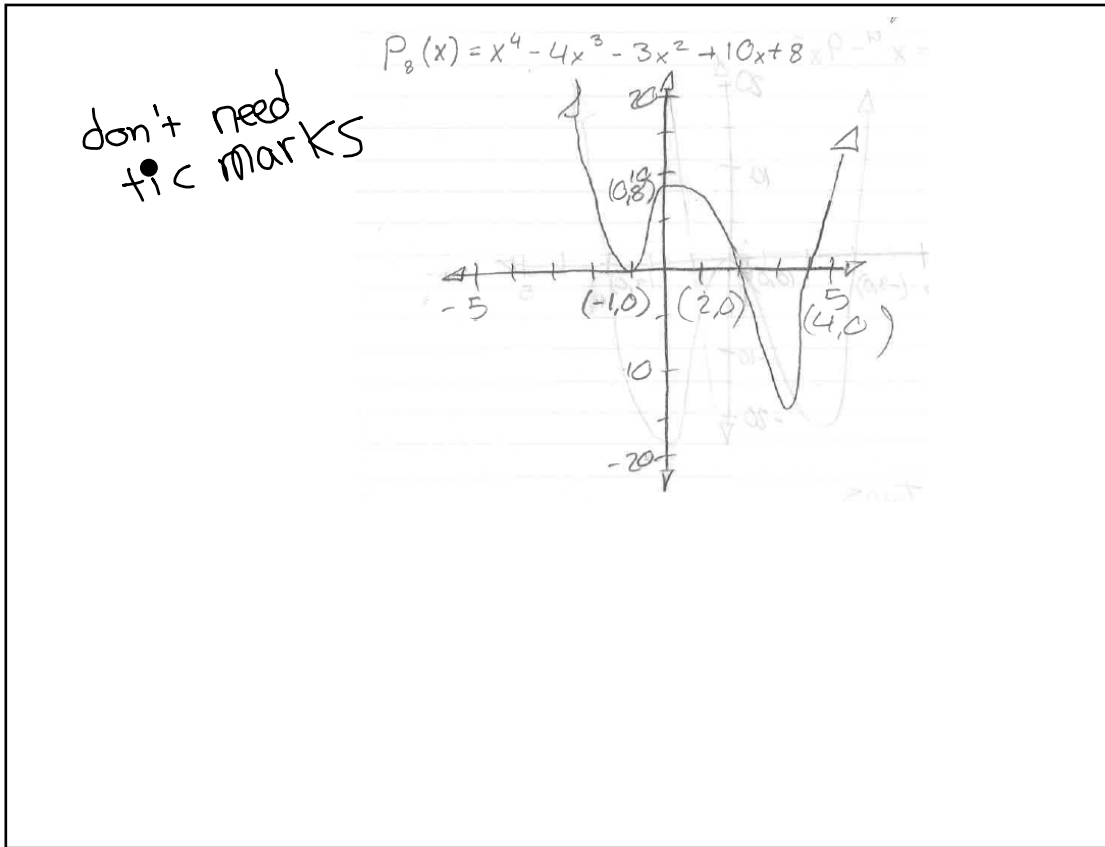


Requirements for EACH Function

- a) Leading term
- b) Lead. coeff
- c) Degree
- d) Make a large neat sketch.
- e) Label  $x$ -intercepts
- f) Label  $y$ -intercept
- g) # turns
- h) end behavior

Take time on each

- ✓ Neat
- ✓ Accurate



## Assignment:

### Worksheet:

### Polynomial Intro Assignment #2

↻  
Added to the  
new recording  
sheet • (purple)

The Pink recording  
(with its assignments  
is due Tuesday)