

HW Help

Pick Up  
the  
Warm Up

① Convert  $\log_6(60) = t$   
to exponential form

base is 6

The log statement  
produces an exponent,  $t$

So.....

$$6^t = 60$$

or

$$60 = 6^t$$

② Solve  $3.26^{x+1} = 99$   
for  $x$

[show exact answer in terms of log  
base 10 and approx. to  
2 d.p.]

$$\log(3.26^{x+1}) = \log(99)$$

$$(x+1) \cdot \log(3.26) = \log(99)$$

$$x+1 = \frac{\log(99)}{\log(3.26)}$$

$$x = \frac{\log(99)}{\log(3.26)} - 1$$

$$x \approx 2.89$$

③ Watch the pattern develop as your teacher [Mr. C] converts each to base 10.

$$\rightarrow \log_8(3) = \frac{\log(3)}{\log(8)} \quad \text{or} \quad \frac{\log_7(3)}{\log_7(8)}$$

$$\rightarrow \log_5(x) = \frac{\log(x)}{\log(5)}$$

$$\rightarrow \log_n(100) = \frac{\log(100)}{\log(n)}$$

$$\rightarrow \log_{\text{base}}(\text{input}) = \frac{\log(\text{input})}{\log(\text{base})}$$

This leads to the change of base formula  
which is:  $\log_a(b) =$   $=$

This is called the

**change of base formula**

$$\log_a(b) = \frac{\log(b)}{\log(a)}$$

which, in fact, can be converted to any base

This is called the

## change of base formula

$$\log_a b = \frac{\log b}{\log a} = \frac{\log_n b}{\log_n a}$$

which, in fact, can be converted to any base

④ Find this formula on your reference sheet.

⑤ Now add to your own notes.

**Log Properties:** If  $y = b^x$ , then  $x = \log_b y$  also.....  $\log_b x^n = n \log_b x$

$$\log_b(m) + \log_b(n) = \log_b(mn) \quad \log_b(m) - \log_b(n) = \log_b\left(\frac{m}{n}\right)$$

$$\log_b(m) = \frac{\log m}{\log b}$$

*can change to any base*

$$\log_b(m) = \frac{\log(m)}{\log(b)}$$

This is called the

**change of base formula**

$$\log_a b = \frac{\log b}{\log a} = \frac{\log_n b}{\log_n a}$$

which, in fact, can be converted to any base

*Add to  
your  
notes*

Lastly, change the following log expression to one with base 5

$$\log_3 4 = \frac{\log_5 4}{\log_5 3}$$

$1.04^x = 2$   
 not helpful      helpful  
 convert to log form      Take log of both sides

$$\log(1.04)^x = \log 2$$

$$x \cdot \log(1.04) = \log(2)$$

$$x = \frac{\log(2)}{\log(1.04)}$$

Now use change of base formula

$$x = \frac{\log(2)}{\log(1.04)}$$

$$x \approx 17.673$$

exact answer in terms of common log

## HW Questions

Answer 103a

$$x = -3$$

$$y = 5$$

$$z = 10$$

**6-72** Find a quadratic in the form  $y = ax^2 + bx + c$  that passes through the three points.

$$(1, 5) \quad 5 = a(1)^2 + b(1) + c \quad \rightarrow \text{I} \quad 5 = a + b + c$$

$$(3, 19) \quad 19 = a(3)^2 + b(3) + c \quad \rightarrow \text{II} \quad 19 = 9a + 3b + c$$

$$(-2, 29) \quad 29 = a(-2)^2 + b(-2) + c \quad \rightarrow \text{III} \quad 29 = 4a - 2b + c$$

$$\text{II} \quad 19 = 9a + 3b + c$$

$$\text{I} \quad 5 = a + b + c$$

$$\text{Subtract} \quad 14 = 8a + 2b$$

$$\text{III} \quad 29 = 4a - 2b + c$$

$$\text{I} \quad 5 = a + b + c$$

$$\text{Subtract} \quad 24 = 3a - 3b$$

$$\begin{array}{l} \downarrow \quad \swarrow \\ \textcircled{A} \quad 14 = 8a + 2b \quad \xrightarrow{3} \quad 42 = 24a + 6b \\ \textcircled{B} \quad 24 = 3a - 3b \quad \xrightarrow{2} \quad \underline{48 = 6a - 6b} \\ \hline 90 = 3a \\ \text{so } \underline{a = 3} \end{array}$$

$$\begin{array}{l} \swarrow \\ 42 = 24(3) + 6b \\ 42 = 72 + 6b \\ -30 = 6b \\ \text{so } \underline{b = -5} \end{array}$$

$$\begin{array}{l} 5 = a + b + c \\ 5 = 3 + (-5) + c \\ 5 = -2 + c \\ \underline{c = 7} \end{array}$$

$$y = 3x^2 - 5x + 7$$

97

$$\log(x) = 0$$

$$10^0 = x \quad 1$$

$$\log(x) = 1$$

$$10^1 = x \quad 10$$

$$\log(x) = 2$$

$$10^2 = x \quad 100$$

Aim

$$10^n = 1500$$

Use properties of logs to simplify log expressions

Why ?

because log equations can get more complex

$$5 \cdot \log_3(x) - \log_3(2x) = 14$$



Tape or Write into your notes ?

## Logarithm Properties

The following definitions and properties hold true for all positive  $m \neq 1$ .

Definition of logs:

$$\log_m(a) = n \text{ means } m^n = a$$

Product Property:

$$\log_m(a \cdot b) = \log_m(a) + \log_m(b)$$

Quotient Property:

$$\log_m\left(\frac{a}{b}\right) = \log_m(a) - \log_m(b)$$

Power Property:

$$\log_m(a^n) = n \cdot \log_m(a)$$

← Ch. 5

Take notes as we do

109 together

a)  $\log_{11}(4) + \log_{11}(2) - \log_{11}(5)$

Goal: Condense to a single term

$\log_{11}(4 \cdot 2) - \log_{11}(5)$

$\log_{11}\left(\frac{4 \cdot 2}{5}\right) = \log_{11}\left(\frac{8}{5}\right)$

$7 - 2 + 1 - 8$   
 $\uparrow$   
 $7 - 1 - 8$

$5 + 1 - 8$   
 $6 - 8$   
 $-2$

$\log_m(a \cdot b) = \log_m(a) + \log_m(b)$

$\log_m\left(\frac{a}{b}\right) = \log_m(a) - \log_m(b)$

b.  $\log_2(M) + \log_3(N)$

can't  
 (base is not the same)

$$\frac{\log(M)}{\log(2)} + \frac{\log(N)}{\log(3)}$$

$\log_m(a \cdot b) = \log_m(a) + \log_m(b)$

c.  $\log(k) + x\log(m)$

$$\log(k) + \log(m^x)$$

$$\log(k \cdot m^x)$$

d.  $\frac{1}{2}\log_5 x + 2\log_5(x+1)$

$$\log_5 [x^{\frac{1}{2}} \cdot (x+1)^2]$$

$$\log_5 \frac{x^{\frac{1}{2}} \cdot (x+1)^2}{\sqrt{x}}$$

$$\log_m (a \cdot b) = \log_m (a) + \log_m (b)$$

e.  $\log(4) - \log(3) + \log(\pi) + 3\log(r)$

$$\log(4) - \log(3) + \log(\pi) + \log(r^3)$$

$$\log\left(\frac{4}{3}\right) + \log(\pi) + \log(r^3)$$

$$\log\left(\frac{4}{3}\pi\right) + \log(r^3)$$

$$\log\left(\frac{4}{3}\pi r^3\right)$$

$$\log_m(a \cdot b) = \log_m(a) + \log_m(b)$$

$$\log_m\left(\frac{a}{b}\right) = \log_m(a) - \log_m(b)$$

f.  $\log(6) + 23 \log(10)$

Now backwards:

expand  $\log 3m^3p^2$

$$\log(3) + 3\log(m) + 2\log(p)$$

3x

x + x + x

B.B.

Next week - State Testing  
- All Grade 11

MON  
Tues  
Wed

- 3 ways to meet Essential Skills requirement and this is the only free option.
- No new lessons during class MON, Tue, Wed.
- There will be review assignments [to prepare for next test]
- In comp. labs A1, A2

all  
Grade 11  
students

Laptops

→ familiar with  
Calculators

<https://oakportal.org/users/students.shtml>

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Sample Tests Resources

**Welcome Students!**  
Use the sample test to help you ta your best on OSAS Online.

Announcements  
[Equation Editor Tutorial](#)  
Added: January 4, 2017

here

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Grade: Select ▾ Question: Introduction ▾

Next

Hello! The purpose of this tutorial is to explain how to use the Equation  
will be using this tool to enter answers that are numbers, expressions,

Before we get started, there are a couple of important things to remem


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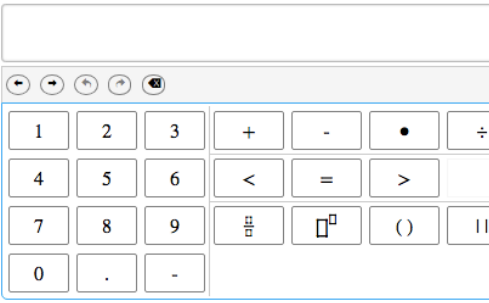
Grade: Select Question: Basic Use

Back Next Refresh

First, we will input a simple equation,  $3 + 5 = 8$ . You can use your keyboard or the on-screen keypad.

- Click on the answer box.
- Press or click on 3.
- Press or click on +.
- Press or click on 5.
- Press or click on =.
- Press or click on 8.

Press here to see how you did 



## Assignment

**6**.....41b, 113, 114a, 115, 122ab

**7**.....163



