

Don't forget about  
AP Exam Registration

deadline • Friday  
March 15  
at 2:30 PM

Monday 12.1

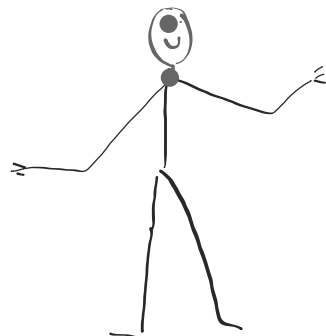
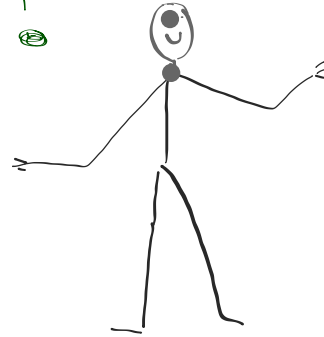
Tues Review 12.1  
strive for 5

Wed Half-Test Ch. 12  
AP Exam Review

Thur ≡ AP Exam Overview  
≡ Start Review Process

Today:

The last inference procedure  
of AP Stats!



Let's perform  
a significance  
test

Woo-hoo !!



Why do we perform a significance test for a slope?

When data from a random sample or a randomized experiment suggests that a linear association exists between two variables, there are two possible explanations for why the slope differs from 0.

there is really no association and we got a non-zero slope due to sampling variability (or chance variation due to random assignment)

OR

there really is an association

[ we do a significance to see which explanation is more plausible ]

Lesson 12.1 Day 3

How does



relate to The **ACT** score?

A counselor is wondering if there is a relationship between GPA and ACT score among 101 students that were applying to schools outside the state. She took a random sample of 9 out of the 101 students and recorded their GPA and ACT score. The data are below.

Student #	83	69	96	89	57	13	24	37	91
GPA	3.7	2.3	4.0	3.8	3.0	1.8	2.0	2.3	3.9
ACT	23	20	35	33	22	13	17	20	29

1. Before even looking at any data, what relationship would you expect GPA and ACT score to have? Explain.

One would think...

Positive, Linear, relationship.

As GPA goes up we would expect  
ACT scores to rise.

Here is the minitab output as well as graphs of the data.

Predictor	Coef	SE Coef	T	P
Constant	1.201	0.0874	13.72	0
GPA	7.507	1.29	5.82	0.0006511
S = 3.252686	R-Sq = 82.8%		R-Sq(adj) = 76.5%	

**2. Find the LSRL for the data.**

Here is the minitab output as well as graphs of the data.

Predictor	Coef	SE Coef	T	P
Constant	1.201	0.0874	13.72	0
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*Handwritten notes:* "y-int" next to Constant, "slope" next to GPA, "SE b<sub>1</sub>" next to SE Coef for GPA.

2. Find the LSRL for the data.

$$\hat{ACT} = 1.201 + 7.507(GPA)$$

↑  
predicted ACT score

3. Do the data provide significant evidence that there is a positive linear relationship between GPA and ACT?

STATE:

Parameter:

Statistic:

H<sub>0</sub>:  $\beta_1 = 0$

H<sub>a</sub>:  $\beta_1 > 0$

Sign. Level:

**STATE:**

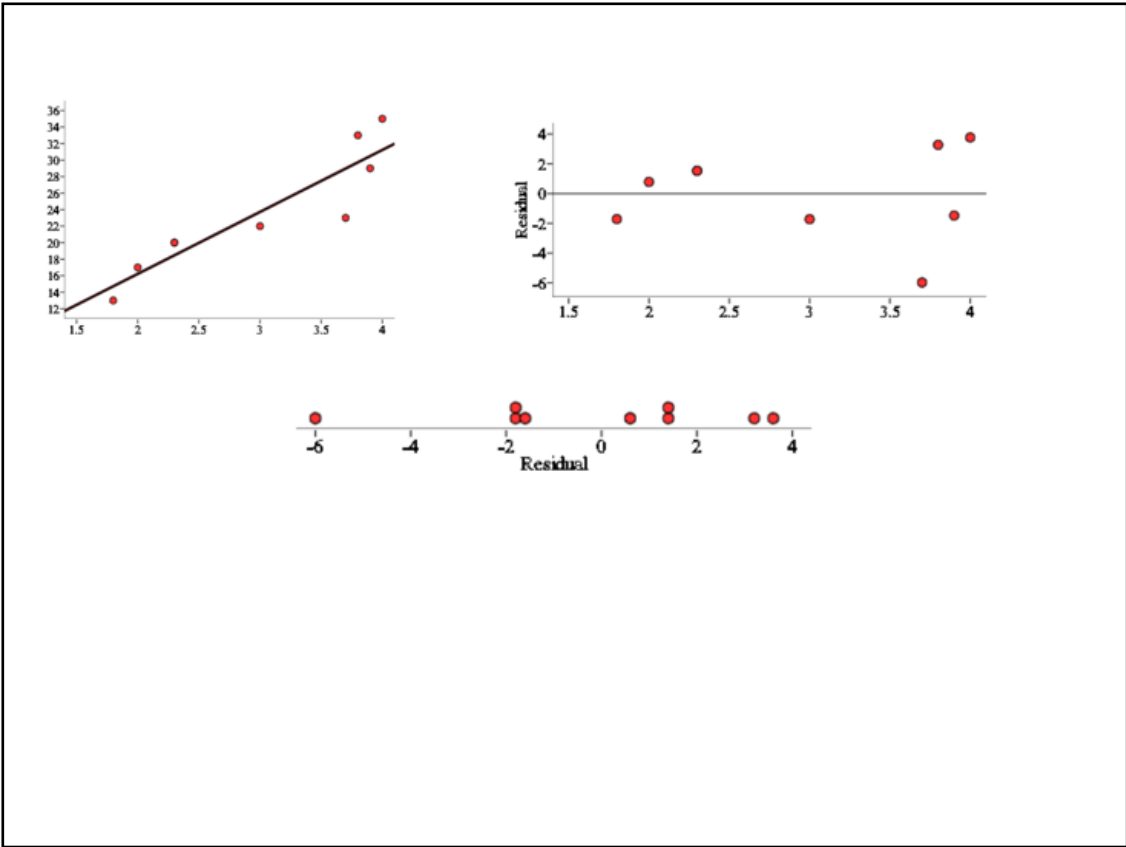
Parameter:  $\beta_1 = 0$  where  $\beta_1$  is the slope of the population regression line relating  $y = \text{ACT score}$  to  $X = \text{GPA}$

Statistic:  $b_1 = 7.507$

*one-sided test*  $H_0: \beta_1 = 0$

$H_a: \beta_1 > 0$   $\uparrow$  We expected a positive relationship

Sign. Level:  $\alpha = 0.05$



**PLAN:** Name of procedure:

Check conditions:

(1) Linear:

(2) Independent:

(3) Normal:

(4) Equal SD:

(5) Random:

**PLAN:** Name of procedure:

One Sample t test for  $\beta_1$   
slope

Check conditions:

✓ (1) Linear: Scatter plot shows a linear relationship and there are no leftover patterns in the residual plot.

✓ (3) Normal: Dot plot shows no strong skewness or clear outliers

✓ (5) Random: "Rand. sample of 9"



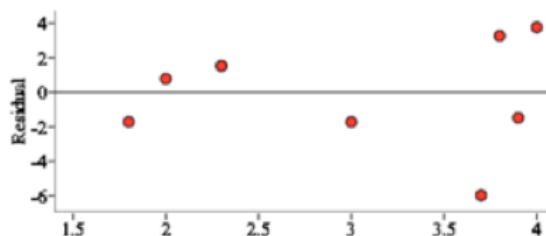
(2) Independent: ✓

$$9 < \frac{1}{10}(101) = 10.1$$

(4) Equal SD: ✓

Residual plot shows a fairly equal amount of scatter around horiz. line  $x=0$  for all  $x$ -values.

If residuals are small for certain values of the explanatory variable and large for others, then the SD of the response variable is not the same for all values of the explanatory variable, thereby violating the “equal SD condition.



**DO:** General Formula:  $\text{test stat} = \frac{\text{stat} - \text{Null}}{\text{SD}}$

Specific Formula:  $t = \frac{b_1 - \beta_1}{\text{SE}_{b_1}}$  ← hypothesized slope

Work:

$$t = \frac{7.507 - 0}{1.29} = 5.819$$

Picture:

df = 9 - 2 = 7

Test statistic: 5.819

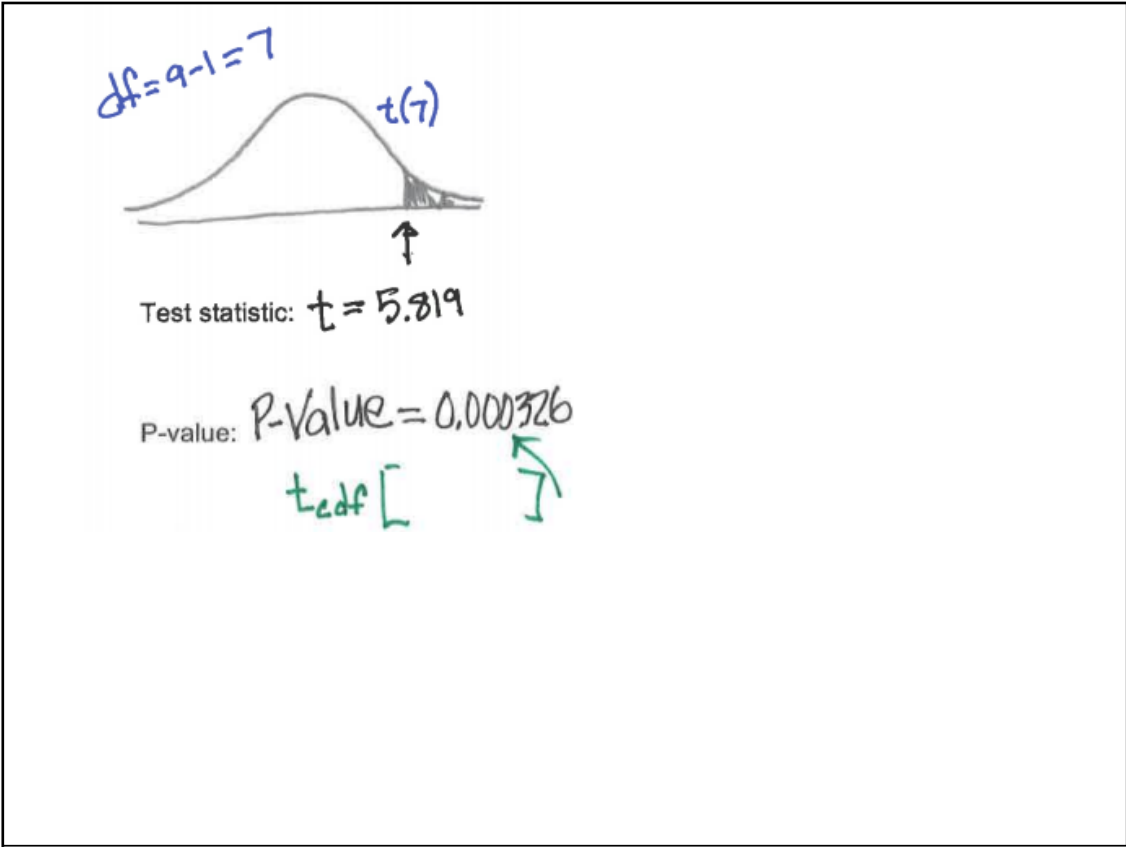
P-value:  $t_{cdf} [ \quad ] = .000326$

**DO:** General Formula:  $\text{Test Stat.} = \frac{\text{stat} - \text{Null}}{\text{SD}}$

Specific Formula:  $t = \frac{b_1 - \beta_1}{\text{SE}_{b_1}}$  ← hypothesized slope

Work:

$$t = \frac{7.507 - 0}{1.29} = 5.819$$



Here is the minitab output as well as graphs of the data.

Predictor	Coef	SE Coef	T	P
Constant	1.201	0.0874	13.72	0
GPA	7.507	1.29	5.82	0.0006511

S = 3.252686      R-Sq = 82.8%      R-Sq(adj) = 76.5%

for a 2-sided test

Because the computer output P-value is for a two-sided test, and there is some evidence for  $H_a$ , we cut it in half

$$0.0006511 / 2 = 0.000326$$

**CONCLUDE:**

**CONCLUDE:**  
Because the P-value of 0.00326  
 $< \alpha = .05$ , we reject  $H_0$ .  
There is convincing evidence of  
a positive linear relationship  
between ACT score and  
GPA.....

●

**Association still does not imply causation, even if the association is significant.**

Lesson 12.1: Day 3: Significance Test for Slope

● Important ideas:  
Hypotheses

● ●  
Conditions

FORMULAS

Lesson 12.1: Day 3: Significance Test for Slope

Important ideas:

**Hypotheses**  
 $H_0: \beta_1 = 0$   
 $H_a: \beta_1 > 0$   
 $\beta_1 < 0$

**Conditions**  
 L.I.N.E.R.  
 See prev. notes

**FORMULAS**  
 ONE sample t test for  $\beta_1$

DO: test stat. =  $\frac{b_1 - \beta_1}{SE_{b_1}}$   
 $df = n - 2$

P-Value =  $t_{cdf}(\text{Lower}, \text{Upper}, df)$

t and two sided P-Value typically given on computer output

slope

Check your understanding

## **IQ and Crying**



H. Armstrong Roberts/  
 iStockphoto.com/Photo  
 Getty Images

**IQ and Crying:** Infants who cry easily may be more easily stimulated than others. This may be a sign of higher IQ. Child development researchers explored the relationship between the crying of infants 4 to 10 days old and their later IQ test scores. A snap of a rubber band on the sole of the foot caused the infants to cry. The researchers recorded the crying of 38 infants. They measured the crying intensity by the number of peaks in the most active 20 seconds. They later measured the children's IQ at age three years using the Stanford-Binet IQ test.

Here is computer output from a least-squares regression analysis of these data. Do these data provide convincing evidence at the  $\alpha = 0.05$  level of a positive linear relationship between count of crying peaks and IQ in the population of infants? Assume conditions have been met.

**Regression Analysis: IQ versus Crycount**

Predictor	Coef	SE Coef	T	P
Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

S = 17.50    R-Sq = 20.7%    R-Sq (adj) = 18.5%

**Regression Analysis: IQ versus Crycount**

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Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

S = 17.50    R-Sq = 20.7%    R-Sq (adj) = 18.5%

STATE

$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 > 0$$

$$\alpha = 0.05$$

## Regression Analysis: IQ versus Crycount

Predictor	Coef	SE Coef	T	P
Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

S = 17.50 R-Sq = 20.7% R-Sq(adj) = 18.5%

STATE

$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 > 0$$

$$\alpha = 0.05$$

$\beta_1$  = slope of pop. regression line relating  
 $y =$  IQ score to  $x =$  count of  
 crying peaks in pop. of infants.  
 $b_1 = 1.4929$

## Regression Analysis: IQ versus Crycount

Predictor	Coef	SE Coef	T	P
Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

S = 17.50 R-Sq = 20.7% R-Sq(adj) = 18.5%

PLAN

one sample t test for  $\beta_1$

DO

$$t = \frac{b_1 - \beta_0}{SE_{b_1}}$$

$$t = \frac{1.4929 - 0}{.4870}$$

$$= 3.07$$



## Regression Analysis: IQ versus Crycount

Predictor	Coef	SE Coef	T	P
Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

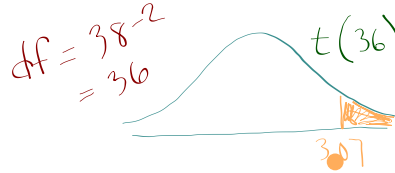
S = 17.50 R-Sq = 20.7% R-Sq(adj) = 18.5%

PLAN

one sample t test for  $\beta_1$ 

Do

$$t = \frac{b_1 - \beta_0}{SE_{b_1}}$$



$$t = \frac{1.4929 - 0}{.4870}$$

$$P = 0.002$$

$$= 3.07$$

for signif. testing  
you can use

## Regression Analysis: IQ versus Crycount

Predictor	Coef	SE Coef	T	P
Constant	91.268	8.934	10.22	0.000
Crycount	1.4929	0.4870	3.07	0.004

S = 17.50 R-Sq = 20.7% R-Sq(adj) = 18.5%

P-Value  
from  
two sided  
test

CONCLUDE Because the P-Value of  $0.002 < \alpha = 0.05$ , we reject  $H_0$ . There is convincing evidence of a positive linear relationship between IQ and crying peaks.

T-Shirts

12.1.... 15, 23-28

study pp. 782-786