

# The Big Picture: Where Chapter 10 Fits

- Chapters 8 and 9 introduced us to confidence intervals and significance tests for a single sample.
- Chapter 10 introduces confidence intervals and significance tests for a difference in proportions and for a difference in means. We use these procedures when we are comparing two independent random samples or two groups in a randomized experiment.

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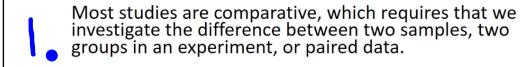
10.2

# The Big Picture: Where Chapter 10 Fits

• Chapters 8 and 9 introduced us to confidence intervals and significance tests for a single sample.

- Chapter 10 introduces confidence intervals and significance tests for a difference in proportions and for a difference in means. We use these procedures when we are comparing two independent random samples or two groups in a randomized experiment.
- Section 10.3 discusses confidence intervals and significance test for a mean difference, which we use when dealing with paired data.

# Chapter 10: The Big Ideas



Inference for the difference in two proportions or the difference in two means is based on the sampling distributions of these differences. Inference for a mean difference uses paired t procedures.

The logic of inference is the same as it was in Chapter 8 (confidence intervals) and Chapter 9 (significance tests), although the details differ somewhat.

When checking Conditions - both groups

The calculations we perform when doing inference for experiments are the same as when doing inference for random samples.

# PACING 9 days

# **Chapter 10: Comparing Two Populations or Groups**

10.1 Comparing Two Proportions
10.2 Comparing Two Means

10.3 Comparing Two Means: Paired Data

Review, FRAPPY, and Test

3 Days 2 Days

2 Days

2 Days

Next Test - Wed. Feb. 6



DETERMINE whether the conditions are met for doing inference about a difference between two proportions.

CONSTRUCT and INTERPRET a confidence interval for a difference between two proportions.

# Lesson 10.1: Day 2: Which gender uses Twitter more?







A recent random sample of 200 U.S. females revealed 110 use Twitter regularly. A separate random sample of 150 males revealed that 60 use Twitter regularly. Construct a 95% confidence interval for the true difference in proportions who use Twitter regularly (females – male).

STATE: State the parameter you want to estimate and the confidence level.

Parameter:

Statistic:

Confidence level:

### Lesson 10.1: Day 2: Which gender uses Twitter more?



A recent random sample of 200 U.S. females revealed 110 use Twitter regularly. A separate random sample of 150 males revealed that 60 use Twitter regularly. Construct a 95% confidence interval for the true difference in proportions who use Twitter regularly (females – male).

STATE: State the parameter you want to estimate and the confidence level.

Parameter:  $P_1 - P_2 \rightarrow \text{true difference in proportions}$ Statistic:  $p_1 - p_2 = .55 - .40$ Confidence level:  $p_1 - p_2 = .55 - .40$ 

Confidence level:

PLAN: Identify the appropriate inference method and check conditions.

Name of procedure:

Check conditions:

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Name of procedure: TWO Sample Z Interval for P1-P2

Check conditions:

10.4

Random

## PLAN: Identify the appropriate inference method and check conditions.

Name of procedure: TWO Sample Z Interval for P1-P2

200 < 1 (all females)

150 < Y10 (of all males

Random Rand Sample of 200 Us females

I Rand. Samp of 150 Us males!

Large Counts

#### PLAN: Identify the appropriate inference method and check conditions.

Name of procedure: TWO Sample Z Interval for P1-P2

Check conditions:

10.4 200 
$$< \frac{1}{10}$$
 (all females)
$$150 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100 < 100$$

Large Counts 
$$200(.55) = 110$$
  
 $200(.45) = 90$   
 $150(.4) = 60$   
 $150(.6) = 90$ 

#### DO: If the conditions are met, perform the calculations.

Point Estimate + margin of error General Formula:

 $(\hat{P}_1 - \hat{P}_2) + 2*\sqrt{}$ 

Work:

Answer:

DO: If the conditions are met, perform the calculations.

General Formula: Point Estimate + margin of error

Specific Formula:  $(\widehat{P}_1 - \widehat{P}_2) \stackrel{+}{=} 2^* \sqrt{\frac{\widehat{P}_1(1-\widehat{P}_1)}{n_1} + \frac{\widehat{P}_2(1-\widehat{P}_2)}{n_2}}$ 

Work:

Answer:

DO: If the conditions are met, perform the calculations.

Point Estimate + margin of error General Formula:

 $(\hat{P}_{1} - \hat{P}_{2}) \pm 2^{*} \sqrt{\frac{\hat{P}_{1}(1-\hat{P}_{1})}{n_{1}} + \frac{\hat{P}_{2}(1-\hat{P}_{2})}{n_{2}}}$ 

Work:

$$0.15 \pm 1.96 \sqrt{\frac{.55 (40)}{200} + \frac{.4 (.6)}{150}}$$

Answer:

I can also be done 2-PropZInt

l	CONCLUDE: Interpret your interval in the context of the problem.							
l	Interpret:							
	We are ••							

Inte	rpret:						
	\//_	OYO	950	confiden	t that	the	
	VVE	W.E	10				

**CONCLUDE:** Interpret your interval in the context of the problem.

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Interpret:

We are 95° confedent that the interval from .046 to .254

#### CONCLUDE: Interpret your interval in the context of the problem.

Interpret:

We are 95' confident that the interval from .046 to .254 captures the true difference in proportions of females to males who use twitter.

We estimate females use twitter 46' to 25.4' more than males.

We estimate females use twitter
46' to 25.4' more than males

Does this confidence interval provide convincing evidence that there is a difference in Twitter use between the two genders?

 $P_1 - P_2 = O$ 

m Hypotheses testing Day 3

## Confidence Interval for a Difference in Proportions

Important ideas:

2 Sample 2 interval

for P1-P2

P1-P2-> true den en propore

P1-P2-> Statistic

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## Confidence Interval for a Difference in Proportions

Important ideas:

2 Sample 2 interval

for 
$$P_1 - P_2$$
 $P_1 - P_2 \rightarrow \text{true deff in proporo}$ 
 $\widehat{P}_1 - \widehat{P}_2 \rightarrow \text{statistic}$ 
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 $\widehat{P}_1 - \widehat{P}_2 \rightarrow \text{statistic}$ 

### Confidence Interval for a Difference in Proportions

Previous Example
(Twitter)

Previous Larger

Previous Example
(Twitter)

Previous Larger

Previous Larger

Previous Example
(Twitter)

Previous Larger

Previous Larger

Previous Example
(Twitter)

Previous Larger

Previous

**Check Your Understand:** A Pew Research Center poll asked independent random samples of working women and men how much they value job security. Of the 806 women, 709 said job security was very or extremely important, compared with 802 of the 944 men surveyed. Construct and interpret a 95% confidence interval for the difference in the proportion of all working women and men who consider job security very or extremely important.



STATE 
$$P_1 - P_2$$
  $\rightarrow$  time difference in the proportion  $P_1 = \frac{709}{900} = .88$ 
of working woman and man who consider job security very
important.

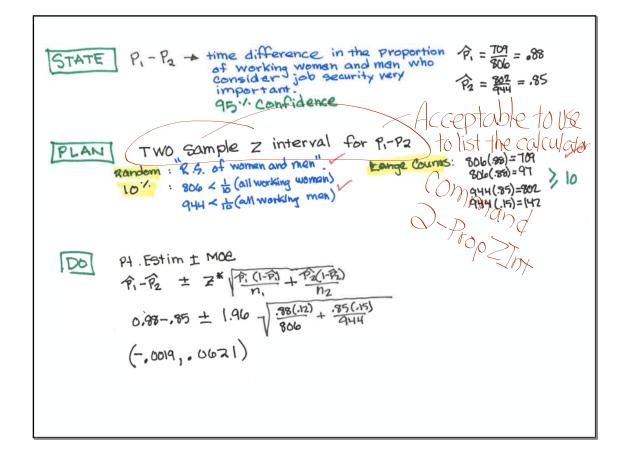
QE' Confidence

PLAN TWO Sample Z interval for  $P_1 - P_2$ 

Random:  $P_1 + P_2 = \frac{30}{910} = .85$ 

Random:  $P_2 + P_3 = \frac{30}{910} = .85$ 

Random:  $P_3 + P_4 = \frac{30}{910} = \frac{30}$ 

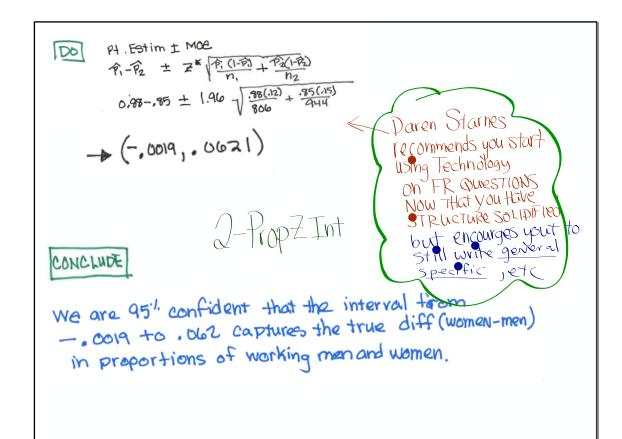


Pt. Estim ± MOR

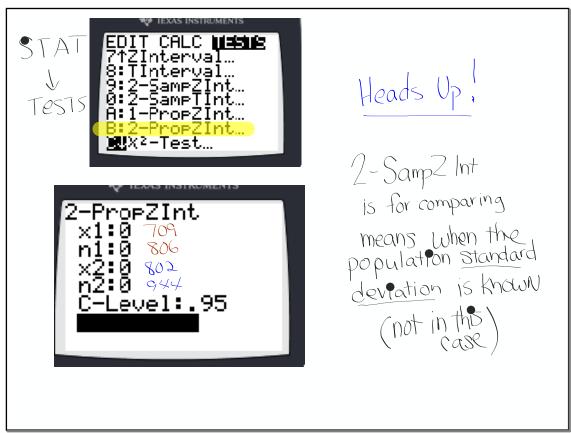
$$\hat{p}_1 - \hat{p}_2 \pm Z^* \sqrt{\hat{p}_1(1-\hat{p}_1)} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}$$
 $0.98-.85 \pm 1.96 - \frac{.98(.12)}{806} + \frac{.85(.15)}{944}$ 
 $- (-.0019, .0621)$ 

# CONCLUDE

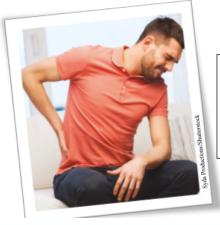
We are 95% confident that the interval from -. 0019 to . 062 captures the true diff (women-men) in proportions of working men and women.



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So far, we have focused on doing inference using data that were produced by random sampling.



The following example shows how to construct and interpret a confidence interval for a difference in proportions from a *randomized comparative* experiment.

# Inference for a

randomized comparative experiment.



# Construct and interpret a confidence interval for a difference in proportions from a randomized comparative experiment.

**BACK PAIN:** Patients with lower back pain are often given nonsteroidal anti-inflammatory drugs (NSAIDs) like naproxen to help ease their pain. Researchers wondered if taking Valium along with the naproxen would affect pain relief. To find out, they recruited 112 patients with severe lower back pain and randomly assigned them to one of two treatments: naproxen and Valium or naproxen and placebo. After 1 week, 39 of the 57 subjects who took naproxen and Valium reported reduced lower back pain, compared with 43 of the 55 subjects in the naproxen and placebo group.

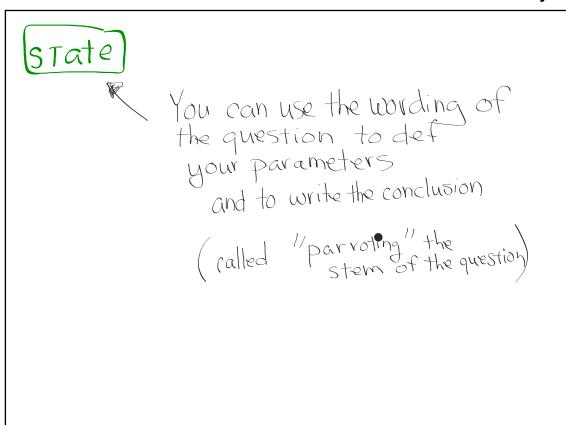
(a) Construct and interpret a 99% confidence interval for the difference in the proportion of patients like these who would report reduced lower back pain after taking naproxen and Valium versus after taking naproxen and placebo for a week.







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where P<sub>1</sub> = true proper of patients who would report reduced lower back point taking maxoroxents

P<sub>2</sub> = true proper of patients

Who would report reduced lower back pain after taking naxoroxen and a placebo.

TWO-sample Z Interval for P<sub>1</sub>-P<sub>2</sub>

Random: Randomly assigned patients to take naproxen add Valium or Naproxen and a placebo.

Large Courts: 31-41-18 45 and 55-43 = 12 all ≥ 10

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And the not needed since researchers

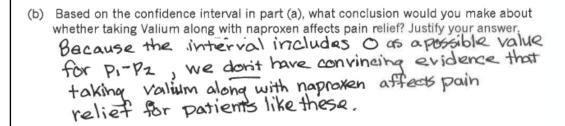
Jid not sample patients without replacement from a larger population

Point Extin 
$$\pm MoE$$
 $9, -p_2 \pm Z^{*} \sqrt{\frac{4.0 + p_2 (14)}{n_1}}$ 
 $(.684 - .782) \pm 2.576 \sqrt{\frac{.684 (.316)}{57} + \frac{.782 (.219)}{55}}$ 
 $-0.098 \pm .214$ 
 $(-.312, 0.116)$ 

CONCLUDE

We are 99% confident that the interval from -312 to .116 captures

PI-P2 = true difference in the true proportions of patients who would report reduce pain after taking naproxen and valium versus after taking naproxen and a placebo.



# Construct and interpret a confidence interval for a difference in proportions from a randomized comparative experiment.

**BACK PAIN:** Patients with lower back pain are often given nonsteroidal anti-inflammatory drugs (NSAIDs) like naproxen to help ease their pain. Researchers wondered if taking Valium along with the naproxen would affect pain relief. To find out, they recruited 112 patients with severe lower back pain and randomly assigned them to one of two treatments: naproxen and Valium or naproxen and placebo. After 1 week, 39 of the 57 subjects who took naproxen and Valium reported reduced lower back pain, compared with 43 of the 55 subjects in the naproxen and placebo group.

(a) Construct and interpret a 99% confidence interval for the difference in the proportion of patients like these who would report reduced lower back pain after taking naproxen and Valium versus after taking naproxen and placebo for a week. (b) Based on the confidence interval in part (a), what conclusion would you make about whether taking Valium along with naproxen affects pain relief? Justify your answer.



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