WARM UP
Write down the formula for standard deviation (way back from chapter 1)

- Look it up if you need to

$$
\begin{aligned}
& S_{x}= \\
& \text { variance }=S_{x}^{2}=
\end{aligned}
$$

WARM UP
Write down the formula for standard deviation (way back from Chapter 1)

- Look it up if you need to

$$
\begin{aligned}
& S_{x}=\sqrt{\frac{\left(x_{1}-\bar{x}\right)^{2}+\left(x_{2}-\bar{x}\right)^{2}+\infty}{n-1}}=\sqrt{\frac{\sum\left(x_{i}-\bar{x}\right)^{2}}{n-1}} \\
& \text { Variance }=S_{x}^{2}=\frac{\sum\left(x_{i}-\bar{x}\right)^{2}}{n-1}
\end{aligned}
$$



Weill use $\sigma_{x}$ for distributions of random variables because well know the entire probability distribution.

Learing Targets
(1) CALCULATE and INTERPRET the standard deviation of a discrete random variable.

USE the probability distribution of a continuous random variable (uniform or Normal) to CALCULATE the probability of an event.

Suppose you got a new job and each day your boss, Mr. Cedarlund, draws a slip of paper from a bag to determine your wage for the day. Let the random variable $X=$ daily wage ( $\$$ per hour).

| $x$ | $2^{1}$ | $3^{5}$ | 7 | 10 | 15 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Lesson 6.1: Day 2: How much do you get paid?

Suppose you got a new job and each day your boss draws a slip of paper from a bag to determine your wage for the day. Let the random variable $\boldsymbol{X}=$ daily wage (\$ per hour).

1. What is your wage for the day? $\qquad$ Add your data to the table on the board and complete the table below.

| $x$ | 1 | 5 | 7 | 10 | 15 | 25 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | $2 / 17$ | $3 / 17$ | $7 / 17$ | $3 / 17$ | 17 | $2 / 17$ |

2. Calculate and interpret the expected value of $X$, perhaps with the help of technology.

$$
\begin{aligned}
& E(X)=\|\left(\frac{2}{1}\right)+5\left(\frac{3}{1}\right)+\ldots 00.8 .99 \\
& \text { If we daw many wages the } \\
& \text { expected wage wo r val be about }
\end{aligned}
$$


4. Interpret the standard deviation.

5. Mrs. Gallas decides she would rather assign wages so that employees could get any amount from $\$ 10$ to $\$ 20$ and all are equally likely. Draw a graph to represent this probability distribution.

## Continuous Random Variables <br> (pages 371-374)

A continuous random variable can take any value in an interval on the number line.

We describe the probability distribution of a continuous random variable with a density curve, such as a Normal curve



## How to Find Probabilities for a Continuous Random Variable

The probability of any event involving a continuous random variable is the area under the density curve and directly above the values on the horizontal axis that make up the event.

FIGURE 6.2 The probability distribution of the continuous random variable $Y=$ randomly generated number between 0 and 9 . The shaded area represents $P(3 \leq Y \leq 7)$.

5. Mrs. Gallas decides she would rather assign wages so that employees could get any amount from $\$ 10$ to $\$ 20$ and all are equally likely. Draw a graph to represent this probability distribution.


 density curve

0000.
5. Mrs. Gallas decides she would rather assign wages so that employees could get any amount from $\$ 10$ to $\$ 20$ and all are equally likely. Draw a graph to represent this probability distribution.

6. What is the probability that an employee makes between $\$ 12$ and $\$ 12.50$ ?


Width
$12.50-12=0.5$ Height
$1 / 10$

$$
\begin{aligned}
& \text { Prob. } \\
& =(0.5)\left(\frac{1}{10}\right)
\end{aligned}
$$

$$
=.05
$$

Probability and Continuous Random Variables
${ }^{\text {mporatan I Jess }}$ Deviation
of a Discrete Rand. Variable
$\sigma=\sqrt{\sum\left(x_{i}-\mu\right)^{2} \cdot p_{i}}$
$\sigma^{2}=$ Variance
$O=\sqrt{\frac{\text { Variance }}{\text { q }}}$

AP EXAM TIP
AP FORMULA $Z$ Formula for variance of Sheet $\longrightarrow$ of a discrete random variable is included. (but not standard deviation)

So just remember that the standard deviation is just the square root of the Variance

$$
\sigma_{x}=\sqrt{\sigma_{x}^{2}}
$$

$\square$
It is possible, but slightly unlikely that the AP exam will require you to calculate the standard deviation "by hand", but you could be

Probability and Continuous Random Variables


Continuous Random Variables

The possible values for a continuous random variable have no gaps. These variables can take values that are "all the decimals and all the decimals that are in between all the decimals".

Check Your Understanding

Check Your Understanding -- The heights of young women can be modeled by a Normal distribution with mean $\mu=64$ inches and standard deviation $\sigma=2.7$ inches. Suppose we choose a young woman at random and let $\mathrm{Y}=$ her height (in inches).

1. What type of variable is Y , discrete or continuous? Explain.
continuous, all heights are possible
2. Interpret the standard deviation.

The heights typically vary by 2.7 inches from the mean of 64 in .
3. Find $P(Y \leq 63)$. Interpret this value.
4. Find $P(68 \leq Y \leq 70)$. Interpret this value.
(i) $z=\frac{68-64}{2.7}=1.48$
$z=\frac{70-64}{2.7}=2.22$
Using Table A:
$0.9868-0.9306$
$=0.0562$


Using technology:
normalcdf(lower:1.48, upper:2.22, mean: 0, SD:1) $=0.0562$
(ii) normalcafflower:68, upper:70, mean:64, SD:2.7) $=0.0561$
3. Find $P(Y \leq 63)$. Interpret this value.

4. Find $\mathrm{P}(68 \leq \mathrm{Y} \leq 70)$. Interpret this value.
3. Find $P(Y \leq 63)$. Interpret this value.


$$
\begin{aligned}
& z=\frac{63-64}{2.7} \\
&=-.37 \\
& \text { TABLE } A \rightarrow .3557
\end{aligned}
$$

4. Find $\mathrm{P}(68 \leq \mathrm{Y} \leq 70)$. Interpret this value.
5. Find $P(Y \leq 63)$. Interpret this value.


There is a prob of 0.3557 that a randomly selected female is less than or equal to 63 in e
4. Find $P(68 \leq Y \leq 70)$. Interpret this value.
3. Find $P(Y \leq 63)$. Interpret this value.


$$
\begin{aligned}
& z=\frac{63-64}{27} \\
&=-.37 \\
& \text { TABLE } A \rightarrow .3557
\end{aligned}
$$

4. Find $\mathrm{P}(68 \leq \mathrm{Y} \leq 70)$. Interpret this value.

There is a prob of 0.3557 that a randomly selected female is less than or equal to 63 in .
3. Find $P(Y \leq 63)$. Interpret this value.

4. Find $\mathrm{P}(68 \leq \mathrm{Y} \leq 70)$. Interpret this value.
4.

There is a prob of 0.3557 that a randomly selected female is less than or equal to 63 in

$$
\begin{aligned}
& \text { normalcdf }\binom{\text { Lower Upper } \mu}{-1000,63,64,2.2}
\end{aligned}
$$


4. Find $P(68 \leq Y \leq 70)$. Interpret this value.

$$
\frac{z=\frac{70-64}{27}=2.22}{\frac{N(64,27)}{6470}} \quad z=\frac{68-64}{27}=6.48
$$

normalcdf (lower 648, upper 2.22, 6, A.7.7) $=0.0562$
 randomly selected female is between 68 to 70 in.
$\square$

Practice

1. Buffalo Wild Wings ran a promotion called the Blazin' Bonus, in which every $\$ 25$ gift card purchased also received a "Bonus" gift card for $\$ 5, \$ 15, \$ 25$, or $\$ 100$. According to the company, here are the probabilities for each Bonus gift card. Let $X$ be the amount of money that is won on the Bonus gift card. Recall from the previous example that $\mu_{X}=\$ 6.37$.

| Value $\boldsymbol{x}_{\boldsymbol{i}}$ | $\$ 5$ | $\$ 15$ | $\$ 25$ | $\$ 100$ |
| :--- | :---: | :---: | :---: | :---: |
| Probability $p_{i}$ | 0.890 | 0.098 | 0.010 | 0.002 |

Calculate and interpret the standard deviation of $X$. (Remember you must show numerical values substituted into the appropriate formula. Once you start you can use ellipses (....)

$$
\begin{aligned}
& \sigma_{x}^{2}=(5-6.37)^{2}(.890)+(15 \\
& \sigma_{x}=\sqrt{\sigma_{x}^{2}}=5.47
\end{aligned}
$$

The amount of money that is won on a randomly selected bonus card will typically vary from the mean $(\$ 6.37)$ by about \$ 5.47
2. A certain AP ${ }^{\text {® }}$ Statistics teacher is feeling generous one day and decides that each student deserves some extra credit. The teacher assigns each student a random extra credit value between 0 and 5 (decimals included) by using $5^{*}$ rand on the calculator.

Let $Y=$ amount of extra credit for a randomly selected student. The probability distribution of $Y$ can be modeled by a uniform density curve on the interval from 0 to 5 . Find the probability that a randomly selected student will get more than 3 points of extra credit.

A certain APw Statistics teacher is feeling generous one day and decides that each student
deserves some extra credit. The teacher assigns each student a random extra credit value between 0 and 5 (decimals included) by using $5^{*}$ rand on the calculator.

Let $Y=$ amount of extra credit for a randomly selected student. The probability distribution of $Y$ can be modeled by a uniform density curve on the interval from 0 to 5 . Find the probability that a randomly selected student will get more than 3 points of extra credit.

## SOLUTION:


$\boldsymbol{Y}=$ Amount of extra credit (points)

$$
\text { Area }=\text { base } \times \text { height }=2 \times 1 / 5=2 / 5
$$

$$
P(Y>3)=2 / 5=0.40
$$

3. The weights of 3-year-old females closely follow a Normal distribution with a mean of m 530.7 pounds and a standard deviation of 3.6 pounds. Suppose we randomly choose a 3 -year-old female and call her weight $X$. What is the probability that she weighs at least 30 pounds?

Hint: You must draw a diagram. Then practice by calculating the Z-score. Then Using Table A or appropriate technology that used the Z-score, with correct terminology written.

(i) $z=\frac{30-20.7}{3.6}=-0.19$

Table A: $1-0.4247=0.5753$
Tech: normalcdf(lower: -0.19 , upper: 1000 , mean: 0, SD: 1 ) $=0.5753$
$\{$ (ii) normalcdf(lower: 30, upper: 1000, mean: 30.7, SD: 3.6) $=0.5771$
There is about a $58 \%$ chance that the randomly selected 3-year-old female will weigh at least 30 pounds.


## 6.1 $13,19,21,23,27,29,31-34$

Teach yourself how to make a histogram of a discrete random variable by following the instrutions on page 370.
study pp. 368-374

