

Turn in the Check For Understanding
Questions in the basket at this time.

and

and pick up the Warm Up

(a) Imagine flipping a fair coin three times. Give a probability model for this chance process and be sure to justify why it is a valid model. [Hint: start by listing the sample space]

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TTT TTH THT TTT
 THT HTH
 HTT HHT

| | | | | |
|-------------|---------------|---------------|---------------|---------------|
| # Heads | 0 | 1 | 2 | 3 |
| Probability | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

It's valid because all of the probabilities add up to 1.

(b) Define event A as getting 2 or more heads, event B as getting no heads, and event C as getting at least one head. Find the probability of each of these events.

(c) Are any of these probabilities related?

(b) Define event A as getting 2 or more heads, event B as getting no heads, and event C as getting at least one head. Find the probability of each of these events.

$$P(A) = P(2 \text{ or more heads}) = \frac{3}{8} + \frac{1}{8} = \frac{3+1}{8} = \frac{4}{8}$$

$$P(B) = P(\text{no heads}) = \frac{1}{8}$$

$$P(C) = P(\text{at least 1 head}) = \frac{3+3+1}{8} = \frac{7}{8}$$

(c) Are any of these probabilities related?

— The events no heads and at least 1 head are mutually exclusive (can't happen at the same time) so... $P(B \text{ and } C) = 0$

— They are also complementary events so $P(B) = 1 - P(C)$

- Use a two-way table or Venn diagram to model a chance process and calculate probabilities involving two events.
- Apply the general addition rule to calculate probabilities.

$$P(A \text{ or } B) = P(A) + P(B)$$

that's not it ↗

—

Stand up
if

- Stand if you are female
- Stand if you are wearing blue jeans
- Stand if you are female **or** wearing blue jeans
- Stand if you are female **and** wearing blue jeans

There are two different uses of the word or in everyday life.

When you are asked if you want "soup or salad," the waiter wants you to choose one or the other, but not both.

However, when you order coffee and are asked if you want "cream or sugar," it's OK to ask for one or the other or both.

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However, when you order coffee and are asked if you want "cream or sugar," it's OK to ask for one or the other or both.

In mathematics and probability, "A or B" means one or the other or both.

Two-Way

TABES

pick up the classwork 😊

How do we find probabilities from a two-way table?

- Who owns a home? What is the relationship between educational achievement and home ownership? A random sample of 500 people who participated in the 2010 census was chosen. Each member of the sample was identified as a high school graduate (or not) and as a home owner (or not). The two-way table displays the data.

| | High school graduate | Not a high school graduate | Total |
|-----------------|----------------------|----------------------------|-------|
| Homeowner | 221 | 119 | 340 |
| Not a homeowner | 89 | 71 | 160 |
| Total | 310 | 190 | 500 |

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Define event A as being a high school graduate. Define event B as being a homeowner. Suppose we choose a member of the sample at random. Find the probability that the member:

(a) is a high school graduate.

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$$P(A) = P(\text{high school grad}) = \frac{310}{500}$$

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(b) is a high school graduate and owns a home.

$$\frac{221}{500}$$

(c) is a high school graduate or owns a home.

(b) is a high school graduate and owns a home.

$$P(A \text{ and } B) = P(\text{HS grad and homeowner}) = \frac{221}{500} = .442$$

There's about a 44.2% chance that a randomly selected person is both a high school grad and is a homeowner.

(c) is a high school graduate or owns a home.

$$P(A \text{ or } B) = P(\text{HS grad or homeowner})$$

$$= \frac{221 + 89 + 119}{500} = \frac{429}{500}$$

$$\frac{221}{500} + \frac{89}{500} + \frac{119}{500} //$$

(d) Explain why $P(A \text{ or } B) \neq P(A) + P(B)$

$$P(A \text{ and } B) = \frac{221}{500}$$

$$P(A) + P(B) = \frac{310}{500} + \frac{340}{500}$$

↑
Outcomes are
double
counted

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(d) Explain why $P(A \text{ or } B) \neq P(A) + P(B)$

Because the outcomes
of $P(A) + P(B)$ are
double counted.

Example 2

Preferences

2. Do males and females have a different preference for math or English classes? The two-way table summarizes data about gender and subject preference for a class of 25 AP students.

| | | Gender | | |
|-------------------|---------|--------|--------|-------|
| | | Male | Female | Total |
| Preferred subject | Math | 8 | 12 | 20 |
| | English | 2 | 3 | 5 |
| | Total | 10 | 15 | 25 |

Suppose we choose a student from the class at random. Define event **D** as getting a male student and event **E** as getting a student who prefers math classes.

- a) Find $P(D)$

$$10/25$$

$$P(\text{male student}) =$$

- b) Find $P(D \text{ and } E)$

$$P(\text{male} + \text{Prefers Math}) = 8/25 = .32$$

- c) Find $P(D \text{ or } E)$

$$P(\text{male student or prefers math}) =$$

$$\frac{8}{25} + \frac{12}{25} + \frac{2}{25} = \frac{22}{25}$$

| | | Gender | | |
|-------------------|---------|--------|--------|-------|
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Suppose we choose a student from the class at random. Define event D as getting a male student and event E as getting a student who prefers math classes.

a) Find $P(D) = P(\text{male}) = \frac{10}{25} = 0.4$

b) Find $P(D \text{ and } E)$

$$= P(\text{male and prefer math}) = \frac{8}{25} = 0.32$$

c) Find $P(D \text{ or } E)$

$$= P(\text{male OR math}) = \frac{2+8+12}{25} = \frac{22}{25} = .88$$

also equal to

$$P(\text{male}) + P(\text{math}) - P(\text{male and math})$$

$$= \frac{10}{25} + \frac{20}{25} - \frac{8}{25} = \frac{22}{25}$$

| Preferred subject | Gender | | Total |
|-------------------|--------|--------|-------|
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| Math | 8 | 12 | 20 |
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c) Find $P(D \text{ or } E)$

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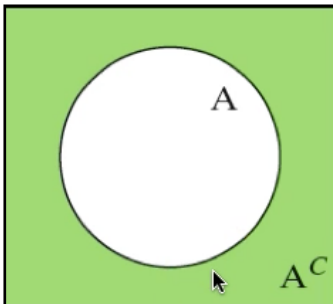
$$P(\text{male}) + P(\text{math}) - P(\text{male and math})$$

$$= \frac{10}{25} + \frac{20}{25} - \frac{8}{25} = \frac{22}{25} = 0.88$$

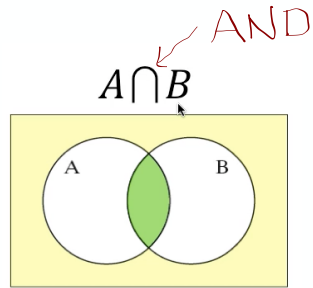
General
Addition
Rule

Venn Diagrams and Probability

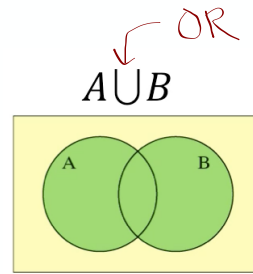
(pages 322-325)



You can see why
 $P(A)$ and $P(A^c)$ add up to 1



Intersection
∩
(football)



Union
∪

HINT: To keep the symbols straight, remember

U for **U**nion and

∩ for **i**ntersection.

$P(A \cup B)$

and on to
example 3
and 4

3. Where are the best tacos?

A survey of all students at a large high school revealed that, in the last month, 38% of them had dined at Taco Bell, 16% had dined at Chipotle, and 9% had dined at both. Suppose we select a student at random. What's the probability that the student has dined at Taco Bell or Chipotle in the last month?

Now create a **Venn Diagram** to display the sample space in a different way.

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General Addition Rule

$$\begin{aligned}
 &= P(\text{Taco Bell OR Chipotle}) \\
 &= P(\text{Taco Bell}) + P(\text{Chipotle}) - P(\text{Taco Bell and Chipotle}) \\
 &= .38 + .16 - .09 = .45
 \end{aligned}$$

Now create a Venn Diagram to display the sample space in a different way.



Left Pacman
Right Pacman
Football

Probability, General Addition Rule, and Venn Diagrams

Big Ideas:

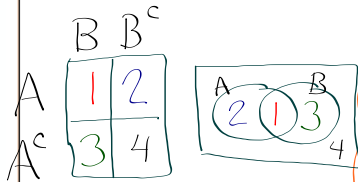
Two way Tables
and Venn Diagrams

General Addition Rule

Probability, General Addition Rule, and Venn Diagrams

Big Ideas:

Two way Tables
and Venn Diagrams

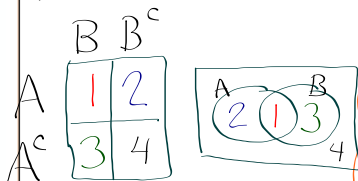


General Addition Rule

Probability, General Addition Rule, and Venn Diagrams

Big Ideas:

Two way Tables
and Venn Diagrams



General Addition Rule

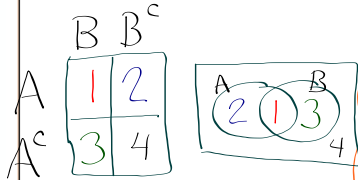
$$P(A \text{ or } B) = P(A) + P(B) - P(\text{A and B})$$

overlap

Probability, General Addition Rule, and Venn Diagrams

Big Ideas:

Two way Tables
and Venn Diagrams



General Addition Rule

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

overlap

If A and B are mutually exclusive

$$P(A \text{ or } B) = P(A) + P(B) = \bigcirc$$

no overlap.

Check Your
Understanding

Check Your Understanding:

What is the relationship between educational achievement and home ownership? A random sample of 500 U.S. adults was selected. Each member of the sample was identified as a high school graduate (or not) and as a homeowner (or not). The two-way table displays the data.

Suppose we choose a member of the sample at random. Define events

G: person is a high school graduate

H: person is a homeowner.

| | High school graduate | Not a high school graduate |
|-----------------|----------------------|----------------------------|
| Homeowner | 221 | 119 |
| Not a homeowner | 89 | 71 |

1. Explain in plain language what $P(G^c)$ means and find the probability.
2. Explain why $P(G \text{ or } H) \neq P(G) + P(H)$. Then find $P(G \text{ or } H)$.
3. Make a Venn diagram to the right to display the sample space of this chance process.

| | High school graduate | Not a high school graduate | |
|-----------------|----------------------|----------------------------|------------|
| Homeowner | 221 | 119 | 340 |
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| | <u>310</u> | <u>190</u> | <u>500</u> |

1. Explain in plain language what $P(G^c)$ means and find the probability.

The probability the person is not a high school grad.

$$P(G^c) = \frac{190}{500} = .38$$

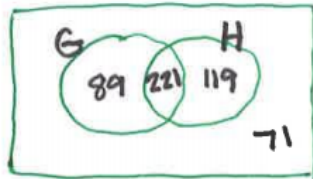
2. Explain why $P(G \text{ or } H) \neq P(G) + P(H)$. Then find $P(G \text{ or } H)$.

There are people who graduated and own a home so they were counted twice.

notice

$$P(G \text{ or } H) = \frac{310 + 340 - 221}{500} = \frac{429}{500} = .858$$

3. Make a Venn diagram to the right to display the sample space of this chance process.



4. Write the event "is not a high school graduate but is a homeowner" in symbolic form and find the probability.

$$P(G^c \cap H) = \frac{119}{500} = .238$$

5.241, 47, 49, 51, 53, 55-58
and study pp.318-325

