

## HWCheck

- ① Pick up the solutions for the "Extra Practice with Correlation...."
- ② Part of your HW score should be whether you studied the packet on the Chi-Square test of Independence. Be honest 😊

## Extra Practice with Correlation and LSRL "by hand"

This data is a comparing Gross Domestic Product, GDP (per capita, inflation adjusted), with Infant Mortality rate, IMR (number of 0-5 year olds dying per 100).

Countries	GDP	IMR
Nigeria	1956	154
Finland	31684	3.3
Bolivia	37313	61
Congo, Dem. Rep	338	199
Mexico	11772	19
China	5450	24
Hungary	17726	7.1
Bangladesh	1326	62
South Korea	22373	5.4

a) make a scatter plot on your GDC and make a sketch of it below

b) comment on the correlation you see.

c) Calculate the correlation coefficient by hand showing both the formula and critical values. (then check against your GDC)

d) Calculate the LSRL by hand in Point - Slope form, showing all details as done in class. If you want you can convert to slope intercept form and check against your GDC.

**Today** ---The full Chi-Square Test of Indep. Process

**Tuesday**- Special Situations + finish eval. Teenage Pregnancy Project

**Wednesday**- Get a list of Unit Test items

Packet P3 (Info on selecting a project and Ideas for project)

**Thursday**- Evaluate another project (using the scoring guide) +

Use Computer spreadsheet to calculate  $r$  and LSRL

**Friday** - Review Questions

**Monday** - Test on Statistical Applications ← Oct. 8<sup>th</sup>

Chi Square Statistic is :

$$\chi^2 = \sum \frac{(f_e - f_o)^2}{f_e}$$

← Formula Packet


Calculated the Chi-Square Statistic  
3 different ways

AIM:

Carry out the entire  
**Test of Independence**

We'll step back and just observe  
example of the whole process

(ppt: Chi Square ppt)

 Chi-Square Test of Independence.pptx

## Full example of a Chi-Square Problem

Do the data provide convincing evidence of an association between age group and whether or not someone uses Facebook for all U.S. adults?

**1. Do you use Facebook?** Mark Z. is interested in finding out if there is an association between age group and Facebook use among U.S. adults. He takes a random sample of 250 U.S. adults aged 18 or older and records their age and whether or not they use Facebook. The two-way table summarizes the results.

		Age (years)				Total
		18-29	30-49	50-64	65+	
Facebook user?	Yes	60	64	46	21	191
	No	8	20	22	9	59
Total		68	84	68	30	250

$(2-1)(4-1) =$

Do the data provide convincing evidence of an association between age group and whether or not someone uses Facebook for all U.S. adults? **(Use the  $\chi^2$  statistic, Method A)**

**Step 1**

$H_0$ : Age and Facebook use are independent.

$H_1$ : Age and Facebook use are associated  
(are not independent)

## Step 2 Calculated Expected Values

		18-29	30-49	50-64	65+
Facebook Use	Yes	51.952	64.176	51.952	22.92
	No	16.048	19.824	<del>16</del> 16.048	7.08

$$\frac{(59)(68)}{250}$$

FROM matrix B ↗

$$\chi^2 = \sum \frac{(o - fe)^2}{fe}$$

## Step 3

All expected are greater than 5  
so test result will be valid

Step 4 :  $\alpha = .05$   
↳ 5%

$\alpha = .1$   
 $\alpha = .01$

Step 5 degrees of freedom  $df = (4-1)(3-1) = 3$

$$\chi^2_{\text{critical}} = 7.815$$

## Step 6

Reject  $H_0$  if  $\chi^2 > 7.815$

TABLE ↗

Step 7  $\chi^2 = 8.86$   
 $\uparrow$   
 GDC

Step 8 • Since  $8.86 > 7.815$ , then we reject  $H_0$ .

There is evidence to support the claim that Age and Facebook Usage are associated.

Critical values of the  $\chi^2$  distribution

degree of freedom

$\nu$	10%	5%	1%
1	2.706	3.841	5.024
2	4.605	5.991	7.378
3	6.251	7.815	9.348
4	7.779	9.488	11.143
5	9.236	11.070	12.833
6	10.645	12.592	14.449
7	12.017	14.067	16.013
8	13.362	15.507	17.535
9	14.684	16.919	19.023
10	15.987	18.307	20.483
11	17.275	19.675	21.920
12	18.549	21.026	23.337
13	19.812	22.362	24.736
14	21.064	23.685	26.119
15	22.307	24.996	27.488
16	23.542	26.296	28.845

$\alpha = .1$

$\alpha = .05$

significance level

## 2. Are you headed for college?

A curious student wondered if students in her high school would respond differently to a teacher than to a student when asked about their intention to go to college after high school. One hundred students from her high school volunteered to participate in an experiment, and they were randomly assigned to have either a student or a teacher interview them. This two-way table summarizes the data.

		Interviewer		Total
		Student	Teacher	
Going to college?	Yes	14	27	41
	No	36	23	59
Total		50	50	100

Expected Values

$$\frac{(50)(59)}{100}$$

		Student	Teacher
		Yes	20.5
No	29.5	29.5	

Does the data provide convincing evidence that there is an association between how a student responds when asked whether they will attend college and who asks the question? (Use the  $\chi^2$  statistic, Method A)

step 1

$H_0$ : Whether the interview is a Teacher or student is independent of whether the student indicates college intention.

$H_1$ : Interviewer and indicating college intention is associated.

Step 3 The test will be valid because all four expected values are greater than 5

Step 4  $\alpha = 0.05$

Step 5  $df = (2-1)(2-1) = 1$

$$\chi^2_{\text{critical}} = \cancel{6.67} \quad 6.64 \quad 3.841$$

Step 6 Reject  $H_0$  if  $\chi^2 > 3.841$



Step 7  $\chi^2 = 6.986$

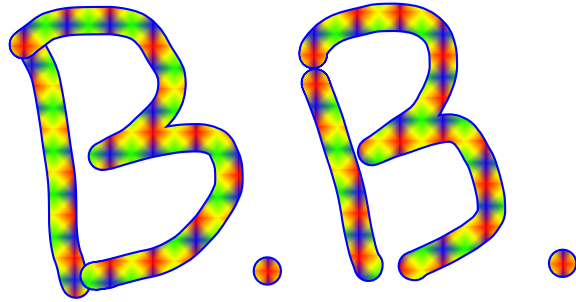
Step 7. We reject  $H_0$  because  $6.986 > 3.841$

There is evidence to support the claim that the interviewer and college intention are assoc.

degree of freedom

significance level

$\nu$	10%	5%	1%
1	2.706	3.841	5.024
2	4.605	5.991	7.378
3	6.251	7.815	9.348
4	7.779	9.488	11.143
5	9.236	11.070	12.833
6	10.645	12.592	14.449
7	12.017	14.067	16.013
8	13.362	15.507	17.535
9	14.684	16.919	19.023
10	15.987	18.307	20.483



Now using  
Method B

## B. The Chi Squared Test of Indep. (using Probability)

You may be asked to perform the test using **probability** instead of the Chi-Square statistic. In that case, you will follow steps 1 through 4. But continue with the following steps instead:

### 5. State the *rejection inequality*

"If the p-value is less than the significance level " (5% or 0.05 for many cases), then I will reject  $H_0$ .

### 6. Calculate the *p-value*.

This step must be done on a calculator. Follow the same calculator steps as if you are calculating the Chi-square statistic.

### 3. Chi-Square by finding the *p-value*, Method B.

Are people who are prone to sudden anger more likely to develop heart disease? An observational study followed a random sample of 8474 people with normal blood pressure for about four years.

Each person took the Spielberger Trait Anger Scale test. Researchers also recorded whether each individual developed coronary heart disease (CHD).

		Anger level			Total
		Low	Moderate	High	
CHD status	Yes	53	110	27	190
	No	3057	4621	606	8284
	Total	3110	4731	633	8474

Do these data provide convincing evidence of an association between the variables in the larger population? (Make the determination by finding the p-value, Method B)

$H_0$ : CHD status and anger level are independent.

$H_1$ : CHD status and anger level are associated.

Step 2: Check if expected values are greater than 5  
and 3  
✓ Test will be valid because .....

Step 4:  $\alpha = .05$

Step 5: Reject  $H_0$  if the p-value is less than 5% (or .05)

Step 6: P-value from GDE = .0313

↑ significance level

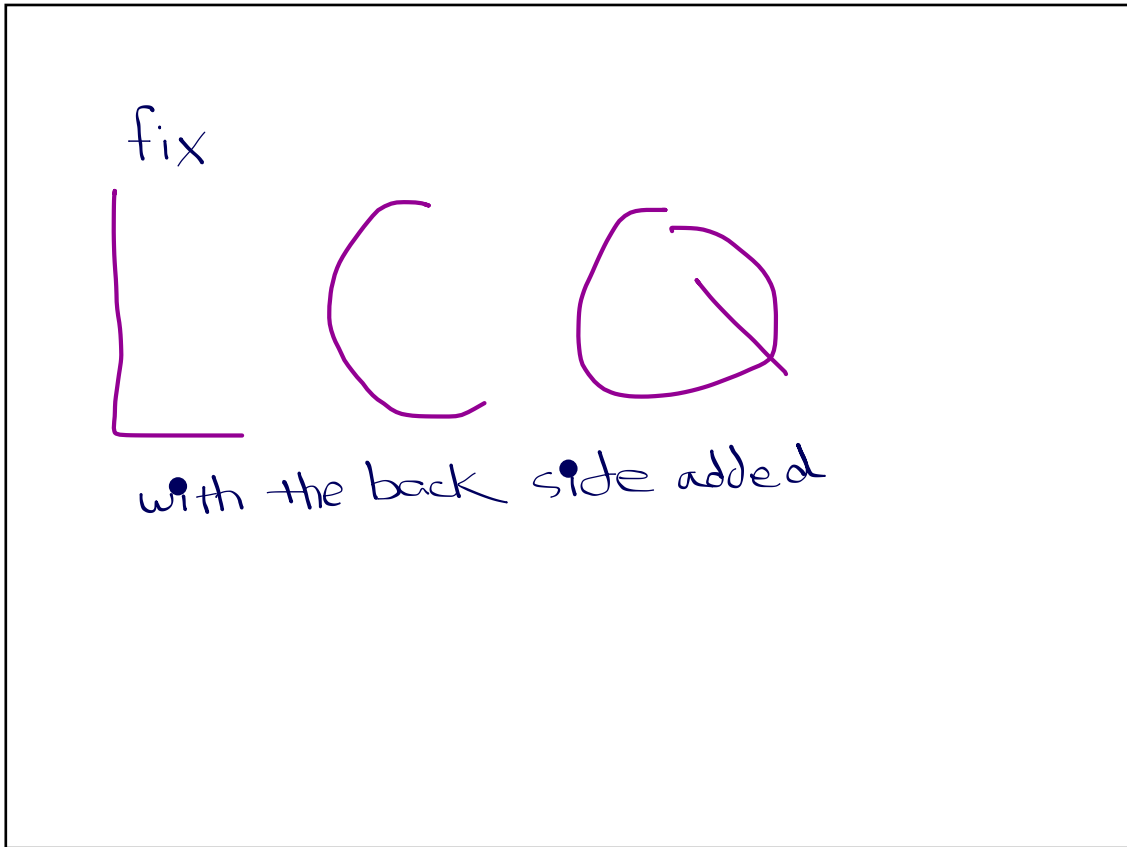
critical from table is needed

✓ Since  $p = .0313$  is less than .05, reject  $H_0$ .

✓ there is evidence to support the claim that CHD and anger level are associated

How do you tell one  
bathroom full of  
statisticians from  
another ?

Check the  
p-value



(b) Using the same data calculate the Pearson's product moment correlation coefficient quickly using your calculator.

(c) Now calculate the Pearson's correlation coefficient again, this time by "hand" using the formula. Show all three critical values and then the final answer

$$r = \frac{\Sigma(x-\bar{x})(y-\bar{y})}{\sqrt{\Sigma(x-\bar{x})^2 \cdot \Sigma(y-\bar{y})^2}} = \frac{\quad}{\sqrt{\quad \cdot \quad}} =$$

(d) Using this correlation coefficient, comment on the correlation.

## Assignment: Ch.11 Packet

- ① p. 337.... 2abc
- ② p. 341.... #1 (use  $X^2$  statistic)
- ③ p. 341....#3 (Use P-value, method B)