

Section 3.2 Learning Targets

Day 1 of 4

- Make predictions using regression lines, keeping in mind the dangers of extrapolation.
- Calculate and interpret a residual.
- Interpret the slope and y intercept of a least-squares regression line.

Start by working
on 1 to 4
of the Barbie
Bungee jump

Lesson 3.2: Day 1: How good are the predictions for Barbie?

Barbie™



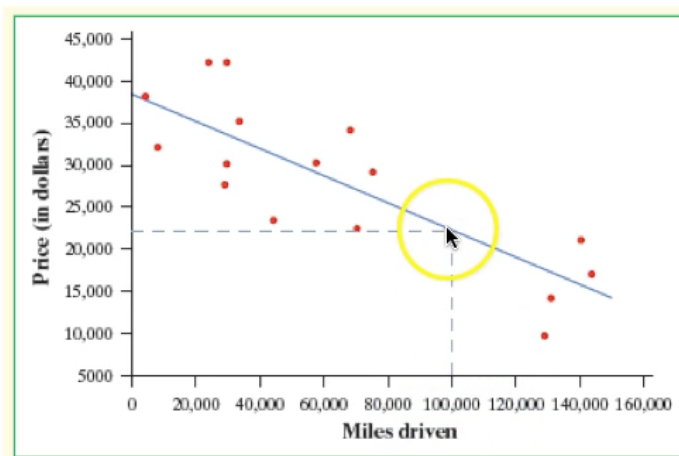
A class performed the “Barbie Bungee” activity. In this activity, students made a chain of rubber bands, connecting them one at a time to Barbie’s feet and then measuring the distance that Barbie travels on her bungee jump. The distance is measured from the edge of the jumping platform to the lowest point that Barbie’s head reaches.

Here is the data from one of the groups. The group forgot to record their measurement for 5 rubber bands.

Number of rubber bands	0	1	2	3	4	5	6	7
Distance traveled (cm)	25	32	41	49	55	?	69	78

1. Go to [stapplet.com](https://www.stapplet.com) to make a scatterplot. Then click “Calculate least-squares regression line”. This is the line that best models the data. Write the equation below.

- We use regression lines to predict the value of a response variable for a particular value of the explanatory variable



1. Go to stapplet.com to make a scatterplot. Then click "Calculate least-squares regression line". This is the line that best models the data. Write the equation below.

Your answer: ? $y = 7.4638x + 25.3333$?

AP answer:

"y-hat" $\rightarrow \hat{y} = 25.333 + 7.464x$

means
predicted
y

Distance = $25.333 + 7.464$ (Rubber bands)

Use context when writing out regression equation

A **regression line** is a line that describes how a response variable y changes as an explanatory variable x changes. Regression lines are expressed in the form $\hat{y} = b_0 + b_1x$ where \hat{y} (pronounced "y-hat") is the predicted value of y for a given value of x .

Why do statisticians prefer ?

$$\hat{y} = b_0 + b_1x$$

y-intercept

Real world

There are often more than one explanatory variables that can help predict the response variable. • $(x_1, x_2, x_3, \text{etc})$

$$y = a + bx_1 + b_2x_2 + b_3x_3$$

↑ the y-intercept is the starting point for making a prediction
process called multiple regression

2. Use the regression line to predict the distance Barbie travels for 5 rubber bands.
Show work.

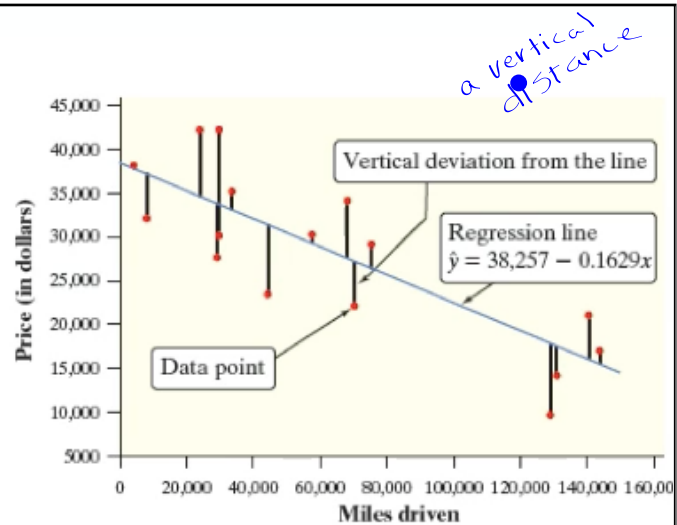
Your work:

AP format:

$$\begin{aligned} \text{distance} &= 25.333 + 7.464(5) \\ &= 62.653 \text{ cm} \end{aligned}$$

A residual is the difference between the actual value of y and the predicted value of y for a particular value of x .

If a residual is positive, the actual value is greater than the predicted value. If it is negative, the actual value is less than the predicted value.



3. One of the group members later found the measurement for 5 rubber bands was 64 cm. Was the prediction from #2 too high or too low? How far off?

Your work:

AP format:

$$\text{Residual} = \text{Actual} - \text{Predicted}$$

$$64 - 62.653 = 1.347$$

The predicted distance was 1.347 cm too low.

AP !!!

4. Predict the distance that Barbie would travel if the group used 20 rubber bands.
Would you trust this prediction more or less than the prediction you made in #2?

Your work:

AP format:

$$\text{distance} = 25.333 + 7.464(20) = 174.613 \text{ cm}$$

We would trust this
prediction less
because it is
an extrapolation

Extrapolation is the use of a regression line for prediction far outside the interval of x values used to obtain the line. Such predictions are often not accurate.



CAUTION:

Don't make predictions using values of x that are much larger or much smaller than those that actually appear in your data.

Now stop and wait !

5. What is the y-intercept of the equation of the regression line? What does it mean?

25.333
cm

6. What is the slope of the equation of the regression line? What does it mean?

7.464

Now stop and wait !

5. What is the y-intercept of the equation of the regression line? What does it mean?

(0, y-int)

When we use 0 rubber bands the predicted distance travelled is 25.333 cm.

6. What is the slope of the equation of the regression line? What does it mean?

$$\text{slope} = \frac{\Delta y}{\Delta x}$$

$$= \frac{\text{change in } y}{\text{change in } x}$$

7.464

The predicted distance goes up by 7.464 cm for each additional rubber band.

Big Ideas:

Check Your Understanding:

1. Some data were collected on the weight of a male white laboratory rat for the first 25 weeks after its birth. A scatterplot of y = weight (in grams) and x = time since birth (in weeks) shows a fairly strong, positive linear relationship. The regression equation $\hat{y} = 100 + 40x$ models the data fairly well.

Big Ideas:

$\hat{y} = b_0 + b_1x$

↑
y-int.

↑
slope

careful of
extrapolation

Residuals

Resid = Actual - Pred

$R = A - P$

y-value y-value

The actual y-context was
resid higher/lower than
predicted for $X =$

y-int. when $X=0$ context
the predicted y-context
is y-int

slope with each additional
X-context the predicted
y-context increases/decreases
by slope

Check Your Understanding:

1. Some data were collected on the weight of a male white laboratory rat for the first 25 weeks after its birth. A scatterplot of y = weight (in grams) and x = time since birth (in weeks) shows a fairly strong, positive linear relationship. The regression equation $\hat{y} = 100 + 40x$ models the data fairly well.

1. Some data were collected on the weight of a male white laboratory rat for the first 25 weeks after its birth. A scatterplot of y = weight (in grams) and x = time since birth (in weeks) shows a fairly strong, positive linear relationship. The regression equation $\hat{y} = 100 + 40x$ models the data fairly well.
 - a. Interpret the slope of the regression line.
 - b. Does the value of the y intercept have meaning in this context? If so, interpret the y intercept. If not, explain why.

1. Some data were collected on the weight of a male white laboratory rat for the first 25 weeks after its birth. A scatterplot of y = weight (in grams) and x = time since birth (in weeks) shows a fairly strong, positive linear relationship. The regression equation $\hat{y} = 100 + 40x$ models the data fairly well.
 - a. Interpret the slope of the regression line.
With each additional week, the predicted weight increases by 40 grams.
 - b. Does the value of the y intercept have meaning in this context? If so, interpret the y intercept. If not, explain why.

Yes. When a rat is 0 weeks old, the predicted weight is 100 grams.

c. Predict the rat's weight at 16 weeks old.

d. Calculate and interpret the residual if the rat weighed 700 grams at 16 weeks old

c. Predict the rat's weight at 16 weeks old.

$$\widehat{\text{Weight}} = 100 + 40(16) \\ = 740 \text{ grams}$$

d. Calculate and interpret the residual if the rat weighed 700 grams at 16 weeks old

$$\text{Residual} = 700 - 740 = -40 \text{ grams}$$

The actual weight is 40 grams lower than predicted at 16 weeks old.

- e. Should you use this line to predict the rat's weight at 2 years old? Use the equation to make the prediction and discuss your confidence in the result. (There are 454 grams in a pound.)

Nope. There are 104 weeks in 2 years. and our data is ^{only} from the first 25 weeks. This is an extrapolation.

LCQ

Assignment

3.2.....37, 39, 41, 43, 45

I encourage you to read/study pp. 176-182