Pick Up the
Warm Up

transformed
parabola



$$
y=x^{2}
$$

$$
y=a(x-h)^{2}+k
$$

Consider the parabolic paths of two soccer penalty kicks, represented in the graph at right. One kick covers a horizontal distance of 20 yards and reaches a maximum height of 9 yards. The other kick covers a horizontal distance of 24 yards, but only reaches a maximum height of 6 yards.

Find an equation that describes the path of each kick.

$y=x^{2}$

$$
\begin{aligned}
& y=a(x-h)^{2}+k \\
& y=a(x-10)^{2}+9
\end{aligned}
$$

$$
\begin{aligned}
& y=a(x-10)^{2}+9 \\
& 0=a(20-10)^{2}+9 \\
& 0=100 a+9 \\
& \text { \& } \\
& a=-\frac{9}{100} \\
& =-.09 \\
& \text { Substitute in a } \\
& \begin{array}{c}
(20,0) \\
\pi
\end{array} \\
& y=\frac{-9}{100}(x-10)^{2}+9
\end{aligned}
$$

$$
\begin{aligned}
y=a(x-10)^{2}+9 & \begin{array}{l}
\text { Substitute in a } \\
\text { point on the curve } \\
\text { (not the vertex) }
\end{array} \\
=a(20-10)^{2}+9 & (20,0) \\
0 & =100 a+9
\end{aligned}
$$

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$$
y=\frac{-1}{24}(x-12)^{2}+6
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$$
y=\frac{-1}{24}(x-12)^{2}+6
$$

$$
\begin{aligned}
& 4 m^{5} \cdot 3 m^{-7}=12 m^{-2}=\frac{12}{m^{2}} \\
& \frac{x^{2} x \cdot m^{1} \cdot m^{-7}}{w^{-7} \cdot x^{3} w^{2}} x=\frac{x^{4} w^{2} w}{1}=x^{4} w^{9} \\
& \left(\frac{m^{5} \cdot h^{-3}}{y}\right)^{-2} \frac{m^{-2}}{y^{-2}}=\frac{n^{5} y^{-2}}{m^{10}}
\end{aligned}
$$

If your HW recording sheet is out and you have a pen then check your solutions
let me know if there are questions afterwards

4-30. Consider the graphs of $f(x)=\frac{1}{2}(x-2)^{3}+1$ and $g(x)=$ $2 x^{2}-6 x-3$ at right. Homework Help
a. Write an equation that you could solve using points $A$ and $B$. What are the solutions to your equation?
Substitute them into your equation to show that they work. $\frac{1}{2}(x-2)^{3}+1=2 x^{2}-6 x-3$
b. Are there any solutions to the equation in part (a) that do not appear on the graph? Explain.
c. Write an equation that you could solve using point $C$. What does the solution to your equation appear to be? Again, substitute your solution into the equation. How close was your estimate?

d. What are the domains and ranges of $f(x)$ and $g(x)$ ?

$\square$
(7) $(x-2)^{2}-3=1$

AlMs
Validate solutions because sometimes "good" solutions are "bad"

- Approximate solutions when an algebraic solution is not possible.

Use algebraic strategies to Solve

$$
\begin{gathered}
(\sqrt{2 x+3})^{2}=(x)^{2} \\
2 x+3=x^{2} \\
0=x^{2}-2 x-3 \\
\vdots \\
x=-1 x=3
\end{gathered}
$$

$$
\begin{aligned}
& x=3 \\
& x=-1
\end{aligned}
$$

We should have got two apparent solutions

$$
\begin{aligned}
& x=-1 \\
& x=3
\end{aligned}
$$

now do an algebraic check in the original equation

$$
\sqrt{2 x+3}=x
$$

check $x=-1$
check $x=3$

$$
\sqrt{2(-1)+3}=(-1)
$$

$$
\begin{gather*}
\sqrt{2(3)+3}=13  \tag{3}\\
\sqrt{6+3} \\
\sqrt{9} \\
3
\end{gather*}
$$

$\sqrt{2 x+3}=x$
check $x=-1$

$$
\sqrt{2(-1)+3}=(-1) \quad \sqrt{2(3)+3}=(3)
$$



$x=-1$ is
extraneous
check $x=3$

$$
3=3
$$

$$
x=3 \frac{i s}{\text { a }} \frac{\text { solvior }}{}
$$

$$
\sqrt{1}=(-1) \quad \sqrt{9}=3
$$

$$
\begin{aligned}
x & =3 \\
x & =-1(\text { extraneous })
\end{aligned}
$$

Validate Graphically

$$
{\underset{y}{y_{1}}}_{\sqrt{2 x+3}}^{y_{2}}
$$



Why did the extraneous solutions appear?

If the sideways parabola is completed, it would intersect at $X=-1$

The graph of $y=\sqrt{2 x+3}$ did not intersect because
 $\sqrt{2 x+3}$ has no negative values

Equations with radicals
called radical equations, commonly have solutions that have extraneous solutions

$$
5=\sqrt{x-2}
$$

Every group needs
Leader
Runner
Player (1 or 2)


Runners
Be prepared to show proof on part a
Leaders
Get a consensus answer on part $b$ and be prepared to share it with the class.

$$
20 x+1=3^{x}
$$

(a)
what were the solutions?
How did you prove they were solutions?

$$
\begin{gathered}
x=0 \\
20(0)+1=3 \\
\\
\left\{\begin{array}{l}
0 \\
\xi
\end{array}\right.
\end{gathered}
$$

$$
\begin{aligned}
& x=4 \\
& 20(4)+1=3^{4} \\
& 80+1
\end{aligned} \sum_{81} \sum_{81} 88
$$

(b) Are the solutions a single number?
or
or be the coordinates of a point?


$$
\begin{aligned}
20 x & +1=3^{x} \\
x & =0 x+(48)
\end{aligned}
$$

The original equation $20 x+1=3^{x}$ only has one variable so the solutions are the $x$-coordinates of the points of intersection.

$$
x=0 \quad x=4
$$

move on to

$$
20 x+1=3^{x}
$$ C

(c)

$$
\begin{aligned}
& 20 x=3^{x}-1 \\
& x=0 \quad x=4
\end{aligned}
$$

$$
B . B .
$$



Your 2 worst were



# 1 question <br>  

You will be given one equation to solve graphically with your calculator. (it will be unsolvable algebraically)
4.... 22 -25, 27-28

26 a an optional problem, not for extra credit.... just for the challenge (fun) of it.
-

$$
0.572
$$

$$
3
$$



