

WARMUP - Factor

1) $x^2 - 4$

$$(x+2)(x-2)$$

2) $4x^2 - 1$

$$(2x+1)(2x-1)$$

3) $6x^2 - 3x$

$$3x(2x-1)$$

$$A^2 - B^2 = (A+B)(A-B)$$

4) $x^2 - 3x - 4$

$$\begin{array}{r} \cancel{-4} \\ \cancel{(1)} \cancel{(-4)} \\ \cancel{x} \cancel{-3} \end{array}$$

$$\begin{array}{c} x \quad -4 \\ x \left| \begin{array}{|c|c|} \hline x^2 & -4x \\ \hline x & \end{array} \right| \\ \hline 1 \quad x \quad -4 \end{array}$$

$$(x-4)(x+1)$$

5) $2x^2 - 3x - 2$

$$\begin{array}{c} (2x+1) \downarrow (x-2) \\ \cancel{1} \quad \cancel{1} \end{array}$$

$$\begin{array}{r} \cancel{-4} \\ \cancel{-4} \quad 1 \\ \cancel{-3} \end{array}$$

$$\begin{array}{c} 2x \quad 1 \\ x \left| \begin{array}{|c|c|} \hline 2x^2 & 1x \\ \hline -4x & -2 \\ \hline \end{array} \right| \\ \hline -2 \end{array} \quad (2x+1)(x-2)$$

6) $3x^2 + 4x + 1$

$$\begin{array}{r} \cancel{3} \\ \cancel{1} \quad \cancel{3} \\ \cancel{4} \end{array}$$

$$\begin{array}{c} 3x^2 + 1x + 3x + 1 \\ x(3x+1) + 1(3x+1) \\ (3x+1)(x+1) \end{array}$$

Section 6.8 Solving Trig Equations Part 2

Ex: Solve on $0 \leq \theta < 2\pi$

$$2\cos^2 \theta + \cos \theta - 1 = 0$$

$$(2\cos \theta - 1)(\cos \theta + 1) = 0$$

$$2\cos \theta - 1 = 0 \quad \cos \theta + 1 = 0$$

$$\cos \theta = \frac{1}{2}$$

$$\cos \theta = -1$$

$$\theta = \frac{\pi}{3}, \frac{5\pi}{3}, \pi$$

$$\begin{array}{c} 2x^2 + x - 1 \\ \cancel{2} \cancel{-2} \\ \cancel{1} \end{array}$$

$$\begin{array}{c} x \quad 1 \\ 2x \left| \begin{array}{|c|c|} \hline 2x^2 & 2x \\ \hline -1x & -1 \\ \hline \end{array} \right| \\ \hline -1 \end{array}$$

$$(2x-1)(x+1)$$

ex: Solve on $0 \leq \theta < 2\pi$

$$\cos^2 \theta - \sin^2 \theta + \sin \theta = 0$$

$$\underbrace{1 - \sin^2 \theta}_{(-1)} - \sin^2 \theta + \sin \theta = 0 \quad \leftarrow \text{get equation to have same trig function.}$$

$$2\sin^2 \theta - \sin \theta - 1 = 0$$

$$(2\sin \theta + 1)(\sin \theta - 1) = 0$$

$$2\sin \theta + 1 = 0 \quad \sin \theta - 1 = 0$$

$$\sin \theta = -\frac{1}{2} \quad \sin \theta = 1$$

$$\theta = \frac{7\pi}{6}, \frac{11\pi}{6}, \frac{\pi}{2}$$

$$\begin{array}{c} -2 \\ \cancel{(-2 \times 1)} \\ -1 \end{array}$$

$$\begin{array}{cc|c} \sin \theta & -1 & \\ \hline 2\sin \theta & -2\sin \theta & \\ \hline 1 & \sin \theta & -1 \end{array}$$

ex: Solve for $0 \leq \theta < 2\pi$

$$\sin(2\theta) - \sqrt{3}\sin \theta = 0$$

$$2\sin \theta \cos \theta - \sqrt{3}\sin \theta = 0$$

$$\sin \theta (2\cos \theta - \sqrt{3}) = 0$$

$$\sin \theta = 0$$

$$2\cos \theta - \sqrt{3} = 0$$

$$\cos \theta = \frac{\sqrt{3}}{2}$$

$$\theta = 0, \pi, \frac{\pi}{6}, \frac{11\pi}{6}$$

Solve on $0 \leq \theta < 2\pi$

$$1) 2\cos^2\theta + \cos\theta = 0$$

$$2) 2\sin^2\theta + \sin\theta - 1 = 0$$

$$3) \sin^2\theta - \cos^2\theta = 1 + \cos\theta$$

$$4) (\tan\theta - 1)(\sec\theta - 1) = 0$$

$$5) \sin^2\theta = 6(\cos\theta + 1)$$