

## WARMUP

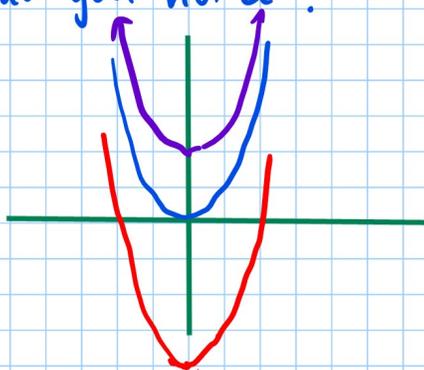
1) Graph on the same axes

$$y = x^2$$

$$y = x^2 - 4 \leftarrow$$

$$y = x^2 + 2 \leftarrow$$

What kind of a shift do you notice? Vertical



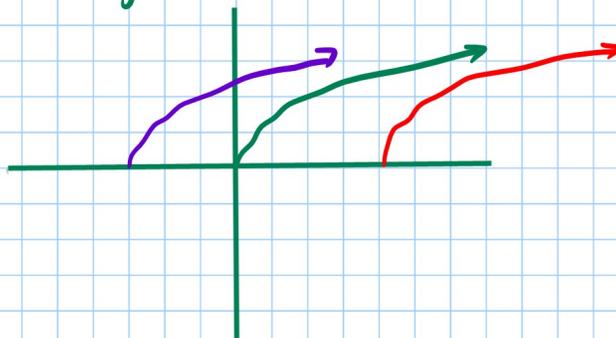
2) Graph on the same axes

$$y = \sqrt{x}$$

$$y = \sqrt{x-4} \leftarrow 4 \text{ right}$$

$$y = \sqrt{x+3} \leftarrow$$

What kind of a shift do you notice?

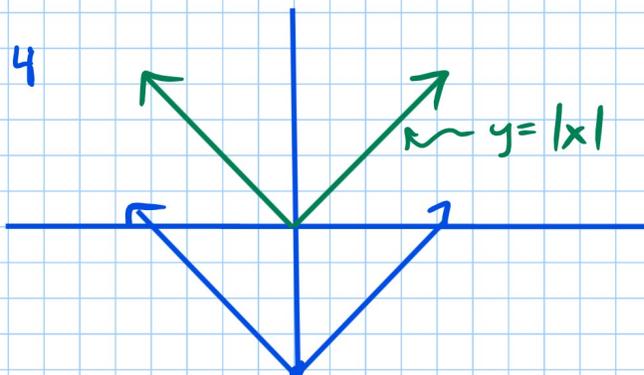


## Section 2.4 Transformations

### Vertical Shifts (c > 0)

- The graph of  $y = f(x) + c$  is the graph of  $y = f(x)$  shifted up  $c$  units
- The graph of  $y = f(x) - c$  is the graph of  $y = f(x)$  shifted down  $c$  units.

ex:  $f(x) = |x| - 4$

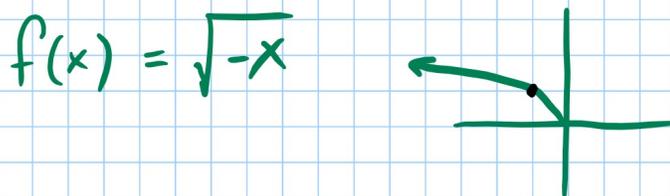
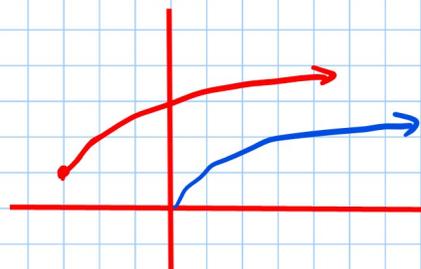


## Horizontal Shifts ( $c > 0$ )

The graph of  $y = f(x - c)$  is the graph of  $f(x)$  shifted  $c$  units to the right.

The graph of  $y = f(x + c)$  is the graph of  $f(x)$  shifted  $c$  units to the left.

ex: Graph  $y = \sqrt{x + 3} + 1$   
left 3      up 1



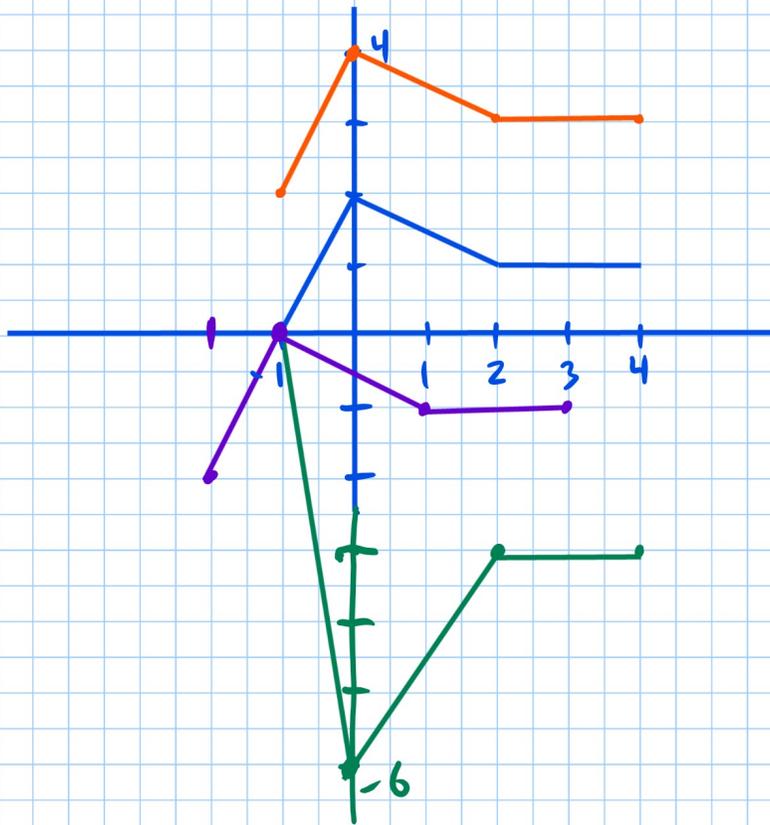
## Reflecting

The graph of  $y = -f(x)$  is the graph of  $f(x)$  reflected about the  $x$ -axis.

## Stretching and Shrinking

$y = cf(x)$  is a vertical stretch if  $c > 1$

and a vertical shrink if  $0 < c < 1$



$$y = f(x) + 2$$

$$y = -3f(x)$$

↑  
multiply y by -3

$$(-1, 0) \rightarrow (-1, 0)$$

$$(0, 2) \rightarrow (0, -6)$$

$$(2, 1) \rightarrow (2, -3)$$

$$(4, 1) \rightarrow (4, -3)$$

$$y = f(x+1) - 2$$

left 1 down 2