

Section 2.3 Properties of Functions

Average Rate of Change from c to x is

$$\frac{\Delta y}{\Delta x} = \frac{f(x) - f(c)}{x - c}$$

difference quotient

ex: Find the avg. rate of change of $f(x) = 2x^2 - 3x$ from 1 to x .

$$\frac{f(x) - f(1)}{x - 1} = \frac{\overbrace{(2x^2 - 3x)}^{f(x)} - \overbrace{(2 \cdot 1^2 - 3 \cdot 1)}^{f(1)}}{x - 1}$$

$$\begin{array}{r} \cancel{-1} \quad \cancel{2} \\ \cancel{-3} \end{array} \quad \begin{array}{r} x \quad -1 \\ 2x \quad 2x^2 \quad -2x \\ -1 \quad -1x \quad 1 \end{array}$$

$$\begin{aligned} &= \frac{2x^2 - 3x + 1}{x - 1} \\ &= \frac{(2x - 1) \cancel{(x - 1)}}{\cancel{x - 1}} \\ &= 2x - 1 \end{aligned}$$

Even, Odd, or Neither

1) A function is even if $f(-x) = f(x)$
Even functions have y-axis symmetry.

ex: $f(x) = 4 - x^2$

$$\begin{aligned} f(-x) &= 4 - (-x)^2 \\ f(-x) &= 4 - x^2 \\ f(-x) &= f(x) \text{ so } f \text{ is even} \end{aligned}$$

2) A function is odd if $f(-x) = -f(x)$

Odd functions have origin symmetry

$$f(x) = x^3$$

$$f(-x) = (-x)^3$$

$$f(-x) = -x^3$$

opposites

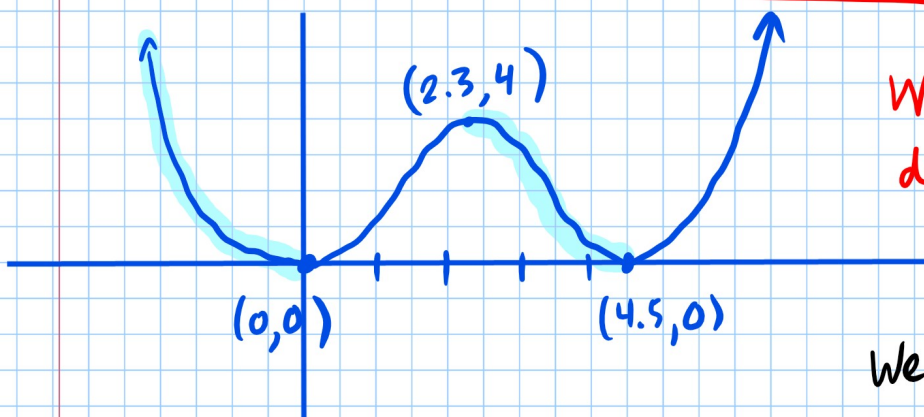
so $f(-x) = -f(x)$ so f is odd

3) A function is neither even nor odd if
 $f(-x) \neq f(x)$ and $f(-x) \neq -f(x)$ No symmetry

ex: $f(x) = x^2 - 4x$

$$f(-x) = (-x)^2 - 4(-x)$$

$$f(-x) = x^2 + 4x \quad \text{Neither}$$



We say this function
decreases on $(-\infty, 0)$ and
 $(2.3, 4.5)$

We say this function
increases on $(0, 2.3)$
and $(4.5, \infty)$

Local minima: $(0, 0), (4.5, 0)$

Local maximum: $(2.3, 4)$

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